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*of* ENGINEERING

# Word Embeddings

2/04/26

# Background: Word Representations

# Motivation

- Core question in understanding cultural and language evolution: how do words change meaning over time?



How can we represent meaning of a word?

# Motivation

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- Can we use language analysis to identify and measure stereotypes?
- Example from last week:
  - Using PMI scores, Wikipedia articles about women tend to talk personal life more
  - Might we expect words like “family”, and “marriage” to be women-associated?

How can we measure “associations” between words?

# How might we represent words?

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“Lexical Semantics”

- Dictionary definition
- Lemma and word forms
- Senses

# How might we represent words?

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**pepper** [pep-er] [SHOW IPA](#)  

See synonyms for: [pepper](#) / [peppered](#) / [peppering](#) on [Thesaurus.com](#)

*noun*

1. a pungent condiment obtained from various plants of the genus *Piper*, especially from the dried berries, used whole or ground, of the tropical climbing shrub *P. nigrum*.
2. any plant of the genus *Piper*.: Compare [pepper family](#).

A sense or “concept” is the meaning component of a word.

# How might we represent words?

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“Lexical Semantics”

- Dictionary definition
- Lemma and word forms
- Senses
- Relationships between words or senses
- Taxonomic relationships
- Word similarity, word relatedness

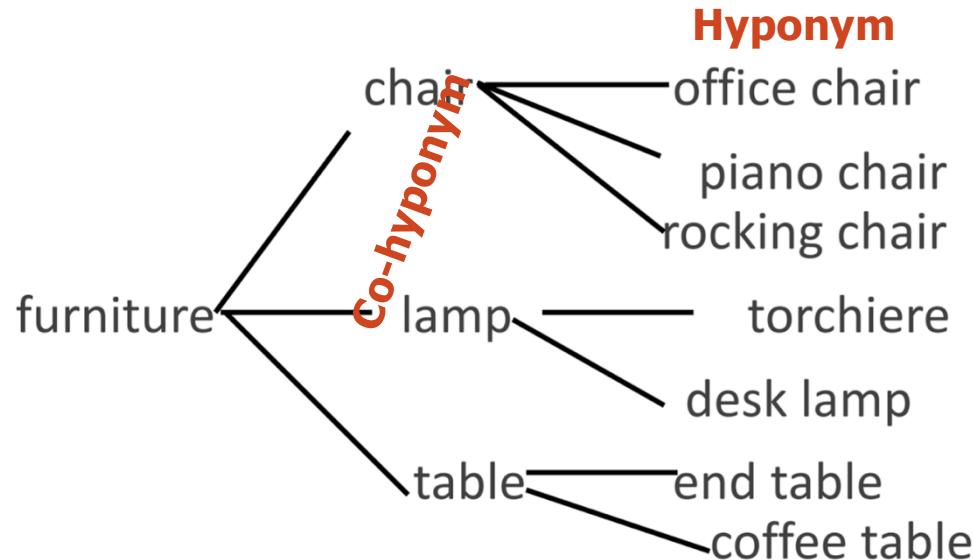
# Relations between words

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- **Synonyms** have the same meanings in some or all contexts
  - Couch / sofa, car / automobile
  - [Note that there are no examples of perfect synonymy]
- **Antonyms** senses that are opposite with respect to one feature of meaning
  - Dark / light, short / long, slow / fast
  - [Otherwise they are very similar]
  - [Antonyms can define a binary opposition or be at opposite ends of a scale]

# Relations between words

- **Hypernym / Hyponym** (superordinate / subordinate)
  - One sense is a hyponym of another if the first sense is more specific, denoting a subclass of the other



# How might we represent words?

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# Annotated Resources for Lexical Semantics

- <https://wordnet.princeton.edu/>
- (python packages)

WordNet Search - 3.1  
- [WordNet home page](#) - [Glossary](#) - [Help](#)

Word to search for:

Display Options:

Key: "S:" = Show Synset (semantic) relations, "W:" = Show Word (lexical) relations  
Display options for sense: (gloss) "an example sentence"

**Noun**

- S: (n) **pepper**, [common pepper](#), [black pepper](#), [white pepper](#), [Madagascar pepper](#), [Piper nigrum](#) (climber having dark red berries (peppercorns) when fully ripe; southern India and Sri Lanka; naturalized in northern Burma and Assam)
  - [part meronym](#)
  - [member holonym](#)
  - [substance meronym](#)
  - [direct hypernym](#) / [inherited hypernym](#) / [sister term](#)
- S: (n) [capsicum](#), **pepper**, [capsicum pepper plant](#) (any of various tropical plants of the genus Capsicum bearing peppers)
- S: (n) **pepper**, [peppercorn](#) (pungent seasoning from the berry of the common pepper plant of East India; use whole or ground)
- S: (n) **pepper** (sweet and hot varieties of fruits of plants of the genus Capsicum)

**Verb**

- S: (v) **pepper** (add pepper to) "pepper the soup"
- S: (v) **pepper**, [pelt](#) (attack and bombard with or as if with missiles) "pelt the speaker with questions"

# How might we represent words?

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“Lexical Semantics”

- Dictionary definition
- Lemma and word forms
- Senses
- Relationships between words or senses
- Taxonomic relationships
- Word similarity, word relatedness
- Semantic frames and roles
- Connotation and sentiment

# How to represent a word

- Until the ~2010s, in NLP words == atomic symbols
- **One-hot** representations in vector space:

1	0	0	0	0	0	1	0	0	0
0	0	0	0	1	0	0	0	0	0
0	1	0	0	0	0	0	0	0	0
0	0	0	1	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	1
0	0	1	0	0	0	0	0	1	0
...	...	...	...	...	...	...	...	...	...
0	0	0	0	0	0	1	0	0	0

$w$  = the drinks were strong but the tacos were bland

V

0	0	...	0	0	0	0	1	tacos
0	0	...	0	1	0	0	0	burritos
0	0	...	0	0	1	0	0	drinks
0	0	...	0	0	0	0	1	leader
0	1	...	0	0	0	0	0	president
0	0	...	1	0	0	0	0	bland

# How to represent a word

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- **One-hot** representations in vector space:

1	0	0	0	0	0	1	0	0	0
0	0	0	0	1	0	0	0	0	0
0	1	0	0	0	0	0	0	0	0
0	0	0	1	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	1
0	0	1	0	0	0	0	0	1	0
...	...	...	...	...	...	...	...	...	...
0	0	0	0	0	0	1	0	0	0

$w$  = the drinks were strong but the tacos were bland

Good things:

- Useful for coding *identity*
- Can do matrix operations:
  - Feed into machine learning models
  - Matrix decompositions

# How to represent a word

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- **One-hot** representations in vector space:

1	0	0	0	0	0	1	0	0	0
0	0	0	0	1	0	0	0	0	0
0	1	0	0	0	0	0	0	0	0
0	0	0	1	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	1
0	0	1	0	0	0	0	0	1	0
...	...	...	...	...	...	...	...	...	...
0	0	0	0	0	0	1	0	0	0

$w = \begin{matrix} \text{the} \\ \text{drinks} \\ \text{were} \\ \text{strong} \\ \text{but} \\ \text{the} \\ \text{tacos} \\ \text{were} \\ \text{bland} \end{matrix}$

Bad things:

- Sparse representations that scale with vocabulary size
- “tacos” is orthogonal to “burritos”
- How can we encode word *similarity* (not just identity)?

# Encoding word similarity

- How can we encode word similarity (not just identity) in word representations?
- Consider encountering a new word: *tezgüino*
  - A bottle of *tezgüino* is on the table
  - Everybody likes *tezgüino*
  - Don't have *tezgüino* before you drive
  - We make *tezgüino* out of corn

term	context			
	1	2	3	4
tezgüino	1	1	1	1
loud	0	0	0	0
motor oil	1	0	0	1
tortillas	0	1	0	1
choices	0	1	0	0
wine	1	1	1	0

# Word-word co-occurrence matrix

Apples are green and red.

Red apples are sweet.

Green oranges are sour

-	apples	are	green	and	red	sweet	oranges	sour
apples	2	2	1	1	2	1	0	0
are	2	3	1	1	2	1	1	1
green	1	1	2	1	1	0	1	1
and	1	1	1	1	1	0	0	0
red	2	2	1	1	2	1	0	0
sweet	1	1	0	0	1	1	0	0
oranges	0	1	1	0	0	0	1	1
sour	0	1	1	0	0	0	1	1

# Distributional hypothesis

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- These representations encode **distributional** properties of each word.
- The **distributional hypothesis**: words with similar meaning are used in similar contexts.

“The meaning of a word is its use in the language.” [Wittgenstein 1943]

“If A and B have almost identical environments we say that they are synonyms.” [Harris 1954]

“You shall know a word by the company it keeps.” [Firth 1957]

# How to encode context



	1	2	3	4	...
term	1	1	1	1	
tezgüino	1	1	1	1	
loud	0	0	0	0	...
motor oil	1	0	0	1	
tortillas	0	1	0	1	...
choices	0	1	0	0	...
wine	1	1	1	0	

**sparse**

# How to encode context

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- **TF-IDF**
- **Word2Vec**
- Not covering other methods: e.g. Brown clusters, Matrix factorization



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# TF-IDF

# Encoding Context with TF-IDF

- Consider a matrix of word counts across documents: **term-document matrix**

Words like *the*, *it*, *they* are not very discriminative, we can do better than raw counts

	As You Like It	Twelfth Night	Julius Caesar	Henry V
battle	1	0	7	13
good	114	80	62	89
fool	36	58	1	4
wit	20	15	2	3

word vector

Bag-of-words document representation

# Encoding Context with TF-IDF

---

- TF-IDF incorporates two terms that capture these conflicting constraints:
  - **Term frequency (tf):** frequency of the word  $t$  in the document

$$tf_{t,d} = \log(count(t, d) + 1)$$

# Encoding Context with TF-IDF

- TF-IDF incorporates two terms that capture these conflicting constraints:
  - **Term frequency (tf):** frequency of the word  $t$  in a cluster (or “class”)

$$tf_{t,c} = \log(count(t, d) + 1)$$

- Document frequency (df): number of documents that a term occurs in
  - **Inverse document frequency (idf):**

$$idf_t = \log\left(\frac{N}{df_t}\right)$$

Higher for terms  
that occur in  
fewer documents

- (N) is the number of documents in the corpus

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Higher for terms  
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- **TF-IDF** combines these two terms:  $tf-idf_{t,d} = tf_{t,d} * idf_t$

# Encoding Context with TF-IDF

- Consider a matrix of word counts across documents: **term-document matrix**

We could use TF-IDF here instead of counts

	As You Like It	Twelfth Night	Julius Caesar	Henry V
battle	1	0	7	13
good	114	80	62	89
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wit	20	15	2	3

word vector

Bag-of-words document representation

# Notes about TF-IDF

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- Very useful way of creating *document embeddings*
  - Designed for and still excels at **document retrieval**
  - Often useful as features for classification models
- We could use variants of *log-odds with a Dirichlet prior ratios* or *topic models* to create document or word embeddings
- Word-embedding use cases of TF-IDF are not as common

# Dimensionality Reduction

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- TF-IDF representations are still sparse
  - Wikipedia: ~29 million English documents. Vocab: ~1 million words.
- Sparse vs. dense vectors:
  - Short vectors often easier to use as features in a classifier (fewer parameters).
  - Dense vectors may generalize better than storing explicit counts.
  - May better capture synonymy
  - In practice, they just work better [Baroni et al. 2014]
- How do we build dense vectors?



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# Word2Vec

# Word2Vec

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- Instead of counting how often each word  $w$  occurs near “corn”, train a classifier on a binary prediction task: Is  $w$  likely to show up near “corn”?
- Don’t actually care about performing this task, but we’ll take the learned classifier weights as the word embeddings
- Training is self-supervised: no annotated data required, just raw text!

# Word2Vec: Two Algorithms

- Context bag-of-words (CBOW): predict current word using context
  - $P(w_t | w_{t+1}, \dots, w_{t+k}, w_{t-1}, \dots, w_{t-k})$
- Skip-gram: predict each context word using current word
  - $P(w_{t+1}, \dots, w_{t+k}, w_{t-1}, \dots, w_{t-k} | w_t)$

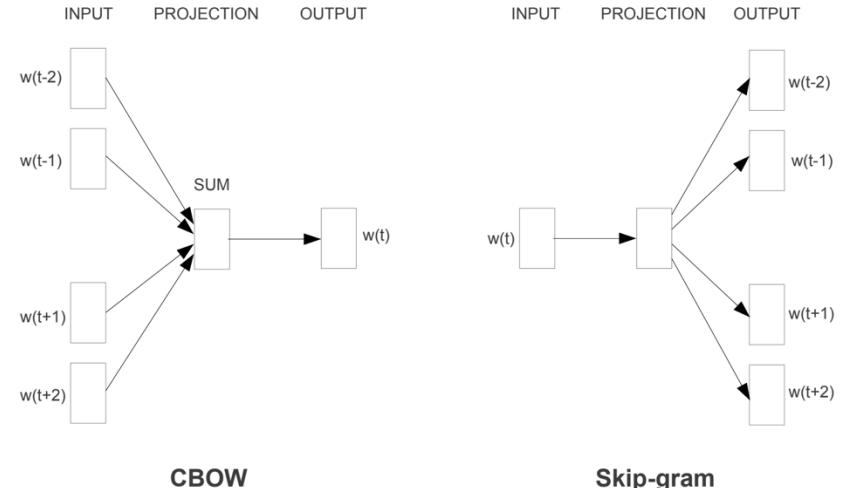


Figure 1: New model architectures. The CBOW architecture predicts the current word based on the context, and the Skip-gram predicts surrounding words given the current word.

# Skip-gram: Probabilities

... that Europe needs unified **banking** regulation to replace the hodgepodge ...

$w_{t-3} \quad w_{t-2} \quad w_{t-1} \quad w_t \quad w_{t+1} \quad w_{t+2} \quad \dots \quad w_{t+5}$

We want to train a model to output  $P(w_{t+j}|w_t)$ . We define:

$$P(w_{t+j}|w_t) = P(o | c) = \frac{\exp(u_o^T v_c)}{\sum_{i=1}^V \exp(u_i^T v_c)}$$

Dot product (similarity metric)  
Larger dot product = larger similarity  
softmax function

$o$  = index of outside (context) word

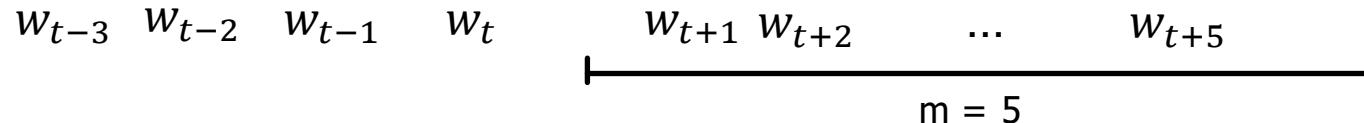
$c$  = index of center word ( $w_t$ )

$V$  = vocab size

$u$  = vector for word as outside (context)  
 $v$  = vector for word as center

# Skip-gram: How do we learn u and w?

... that Europe needs unified **banking** regulation to replace the hodgepodge ...



Data Likelihood: probability of any context word given center word (maximize)

[Note we're assuming conditional independent]  $\rightarrow L = \frac{1}{T} \prod_{t=1}^T \prod_{-m \leq j \leq m, j \neq 0} P(w_{t+j} | w_t, \theta)$

Objective Function: negative log probability (minimize)

$$L = - \frac{1}{T} \sum_{t=1}^T \sum_{-m \leq j \leq m, j \neq 0} \log P(w_{t+j} | w_t, \theta)$$

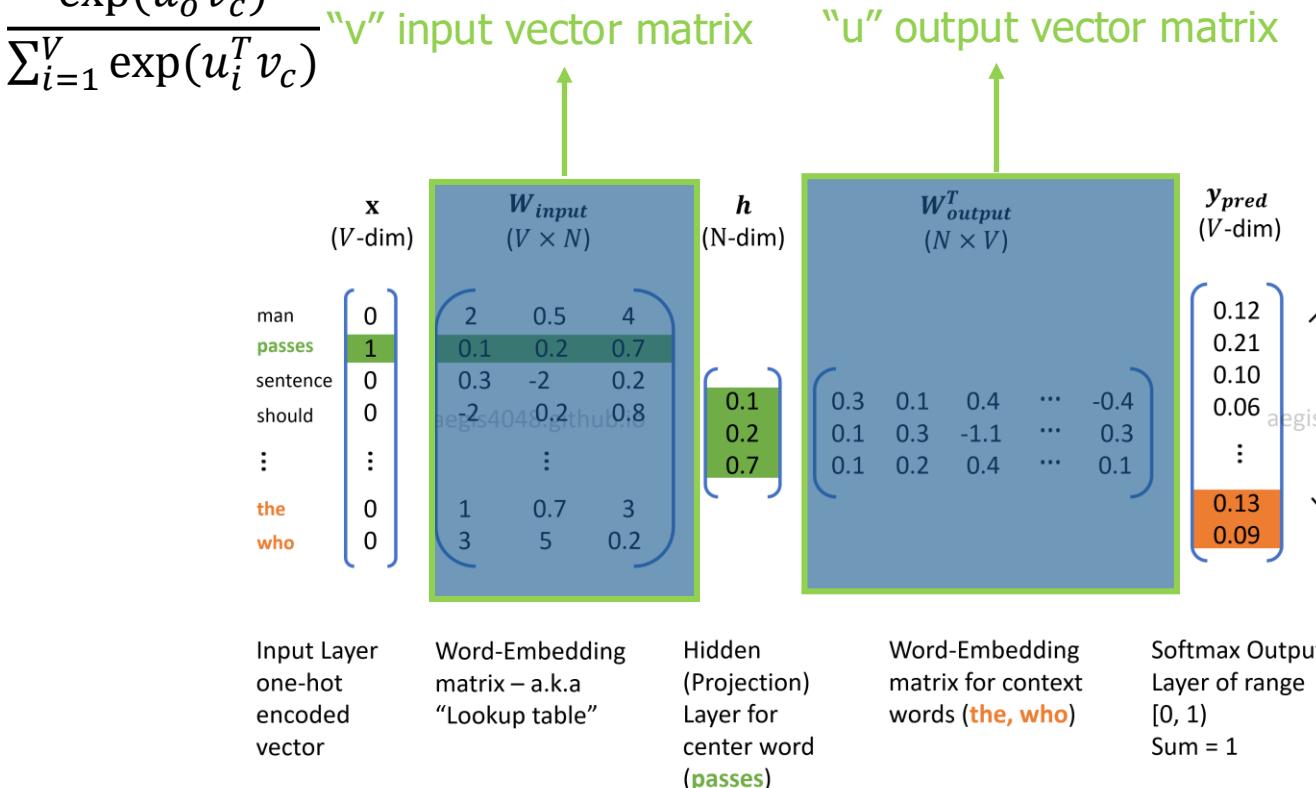
# Skip-gram: How do we learn u and w?

$$L = - \frac{1}{T} \sum_{t=1}^T \sum_{-m \leq j \leq m, j \neq 0} \log P(w_{t+j} | w_t, \theta)$$

$$P(w_{t+j} | w_t) = P(o | c) = \frac{\exp(u_o^T v_c)}{\sum_{i=1}^V \exp(u_i^T v_c)}$$

- Gradient-based estimation (e.g. stochastic gradient descent)
  - Start with uninformed guess for u and w (e.g. random)
  - Iteratively change u and w in the way that locally best-improves the guess
  - Computing gradients (e.g. derivatives) of the objective function with respect to u and w inform how to change them

$$\frac{\exp(u_o^T v_c)}{\sum_{i=1}^V \exp(u_i^T v_c)}$$



$N$  = number of dimensions in embeddings (parameter you choose)

At the end of training we've learned 2 sets of embeddings: we can average them or just keep one of them

# Skip-gram

$$\frac{\exp(u_o^T v_c)}{\sum_{i=1}^V \exp(u_i^T v_c)}$$

- Problem:
  - Denominator is computationally expensive!  $O(VK)$
  - Solutions:
    - Hierarchical softmax  $O(\log V)$
    - Negative Sampling  $O(1)$

# Skip-gram: Negative sampling

$$\frac{\exp(u_o^T v_c)}{\sum_{i=1}^V \exp(u_i^T v_c)}$$

Encourage center word and context word to have similar vectors

Encourage center word and all other words to have different vectors

- Intuition: we don't need to down-weight all other words at once, we can chose a small number of negative samples

# Skip-gram: Negative sampling

$$P(o \mid c) = \frac{\exp(u_o^T v_c)}{\sum_{i=1}^V \exp(u_i^T v_c)} \longrightarrow \frac{1}{1 + \exp(-u_o^T v_c)}$$

- New objective (single context word, k negative samples)

$$\log P(o_+ \mid c) + \sum_{i=1}^k \log(1 - P(o_i \mid c))$$

- (Problem changes from multiclass to binary)

# Choosing negative samples

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- Generally choose frequent words
- Could choose purely based on frequency  $P(w)$
- In practice,  $P_\alpha(w) = \frac{\text{count}(w)^\alpha}{\sum_w \text{count}(w)^\alpha}$  with  $\alpha = 0.75$  works well (gives rare words slightly higher probability)

# Recap

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- We want meaningful representations of words that we can use for corpus analytics (and other things)
- By defining a fake task, predicting context from a word (skip-gram) or a word from context (CBOW), we can learn meaningful vector
  - Our training objective specifically encourages words that co-occur together or occur in similar contexts to have similar vectors
- Actual implementation requires additional tricks for reducing computational complexity

# Pre-trained Word2Vec Embeddings

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- <https://code.google.com/archive/p/word2vec/>
- You can train embeddings on your own data
- Depending on your application, you can also start with embeddings trained on large data set

# Other word embeddings: GloVe [Pennington et al. 2014]

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- <https://nlp.stanford.edu/projects/glove/>
- “Global Vectors”
- Model is based on capturing global corpus statistics
- Incorporates ratios of probabilities from the word-word cooccurrence matrix (intuitions of count-based models) with linear structures used by methods like word2vec

# Other word embeddings: fasttext

## [Bojanowski et al. 2017]

- Word2vec can't handle unknown words and sparsity of rare word-forms (e.g. we should be able to infer "milking" from "milk" + "ing")
- Uses subword models, representing each word as itself plus a bag of constituent n-grams, with special boundary symbols < and > added to each word.
- Each word is represented by the sum of all of the embeddings of its constituent n-grams. Unknown words can be represented by just the sum of the constituent n-grams.

# Gensim: Python Package for working with word embeddings

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```
>>> from gensim.test.utils import common_texts
>>> from gensim.models import Word2Vec
>>>
>>> model = Word2Vec(sentences=common_texts, vector_size=100, window=5, min_count=1, workers=4)
>>> model.save("word2vec.model")
```

<https://radimrehurek.com/gensim/models/word2vec.html>

# Takeaways

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- Intuitive ideas behind representing words as vectors
- Distributional Hypothesis
- Basic ideas behind TF-IDF weighting
- Basic ideas behind Word2Vec
  - Difference between CBOW and Skip-gram
  - Practical challenges
- *Know where your embeddings came from and how they were made*

# Next Class

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- How do we know if our embeddings work?
- What do we do with them?

# Acknowledgements and Resources

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- Slide content drew heavily from Emma Strubell and Yulia Tsvetkov's slides:  
<http://demo.clab.cs.cmu.edu/11711fa20/slides/11711-04-word-vectors.pdf>
- Resources:
  - Lecture Notes from Stanford NLP class on word embeddings  
[https://web.stanford.edu/class/cs224n/readings/cs224n\\_winter2023\\_lecture1\\_notes\\_draft.pdf](https://web.stanford.edu/class/cs224n/readings/cs224n_winter2023_lecture1_notes_draft.pdf)
  - Efficient Estimation of Word Representations in Vector Space (original word2vec paper)  
<https://arxiv.org/pdf/1301.3781.pdf>
  - Distributed Representations of Words and Phrases and their Compositionality (negative sampling paper)  
[https://proceedings.neurips.cc/paper\\_files/paper/2013/file/9aa42b31882ec039965f3c4923ce901b-Paper.pdf](https://proceedings.neurips.cc/paper_files/paper/2013/file/9aa42b31882ec039965f3c4923ce901b-Paper.pdf)
  - Jurafsky and Martin textbook Chap 6: <https://web.stanford.edu/~jurafsky/slp3/6.pdf>