

Roll - 2106250

Subject - D.E.

Name - Seema Kumari. Assignment - 1

Date / /
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①. Data word - $D_1 D_2 D_3 D_4$
1000

Hamming Code - $P_1 P_2 D_3 P_4 D_5 D_6 D_7$
= $P_1 P_2 1 P_4 0 0 0$

For P_i in even parity must give 0.

$$P_1 \oplus D_3 \oplus D_5 \oplus D_7 = P_1 \oplus 1 \oplus 0 \oplus 0 \Rightarrow P_1 = 1$$

$$P_2 \oplus D_3 \oplus D_6 \oplus D_7 = P_2 \oplus 1 \oplus 0 \oplus 0 \Rightarrow P_2 = 1$$

$$P_4 \oplus D_5 \oplus D_6 \oplus D_7 = P_4 \oplus 0 \oplus 0 \oplus 0 \Rightarrow P_4 = 0$$

Hamming Code - 11100000

Received Hamming Code - 1100100
 $P_1 P_2 P_3 P_4 D_5 D_6 D_7$

$$P_1 \oplus 0 \oplus 1 \oplus 0 = 1$$

$$1 \oplus 1 \oplus 1 \oplus 0 = 1$$

$$0 \oplus 1 \oplus 1 \oplus 0 = 0$$

error is in 3rd position

Hamming Code with out error - 1100110

Data retrieved :- 0110

②.

$P+\bar{Q}$

$P+\bar{Q}$

$\bar{P}+Q$

$\bar{P}+Q$

	$R+\bar{S}$	$R+\bar{S}$	$\bar{R}+\bar{S}$	$\bar{R}+\bar{S}$
$P+\bar{Q}$	0	0	1	X
$P+\bar{Q}$	0	1	X	1
$\bar{P}+Q$	1	X	1	0
$\bar{P}+Q$	X	1	0	0

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02

$$(Q+S) (P+Q+R) (P+R+S) (\bar{P}+Q+\bar{R}) (\bar{P}+\bar{R}+S)$$

$$(Q+S) (Q+P\bar{R}+\bar{P}+R) (S+\bar{P}R+P\bar{R})$$

$$(Q+S+QS) (P\bar{R}+\bar{P}R)$$

$$(\bar{Q} \cdot \bar{S} \cdot QS) \cdot (P\bar{R} \cdot \bar{P}R) = f$$

(3) (i) BCD addition (749 + 858)

749

$$\begin{array}{r} 0000\ 0111\ 0100\ 1001 \\ + 0000\ 1000\ 0101\ 1000 \\ \hline \end{array}$$

$$\begin{array}{r} 0000\ 1111\ 1010\ 0001 \\ + 0110\ +0110\ +0110 \\ \hline \end{array}$$

$$1607 \rightarrow 0001\ 0110\ 0000\ 0111$$

ii) Subtraction (539 - 378)

539

0101 0011 1001

378

0011 0111 1000

1100 1000 0111 $\rightarrow 1's\ complement$

0001 1100 0000

0001 1100 0001

+ 1010

161 \rightarrow

0001 0110 0001

iii) $(-14) - (-6)$ using 2's Complement method

 $(-6) \text{ 2's Complement} \rightarrow 11111010$
 $+ (-14) \text{ 2's Complement} \rightarrow 10001010$

$$\begin{array}{r} 11111010 \\ + 10001010 \\ \hline \end{array}$$

= -8

$$-14 + (-6) = -8$$

(4) Gray codes belong to a class of codes called minimum change code in which they only one-bit code group changes when going one step to the next, this is an un-weighted code which means that there are no specific weights assigned to the bit positions. In the gray code, if we go from one decimal number to next only one bit of the gray code changes because of this feature, an amount of switching is minimized. ~~and~~ gray code actually follows adjacency property, between two successive gray codes there is only one bit change and in the binary code, there will be multiple value changes.

(5), given

U, V and W are boolean variables -

$$\begin{aligned}
 & U\bar{V} + UV + U\bar{W} \\
 \Rightarrow & U\bar{V} + UV + V(W + \bar{W}) \\
 \Rightarrow & U\bar{V} + UV + V(1) \\
 \Rightarrow & U\bar{V} + UV + V \\
 \Rightarrow & U(\bar{V} + V) + V \\
 \Rightarrow & U + V\bar{W} = U + V\bar{W}
 \end{aligned}$$

Hence proved

(6)

x	y	z
0	0	0
0	0	1
0	1	0
0	1	1
1	0	0
1	0	1
1	1	0
1	1	1

A	B	C
0	0	1
0	1	0
0	1	1
1	0	0
0	1	0
0	1	1
1	0	0
1	0	1

$$A = \sum m (3, 6, 7)$$

$$B = \sum m (1, 2, 4, 5)$$

$$C = \sum m (0, 2, 5, 7)$$

K-map for A

x \ yz	00	01	11	10
0			1	
1			1	1

$$A = yz$$

K-map for C:

x \ yz	00	01	11	10
0		1		1
1	1	1		

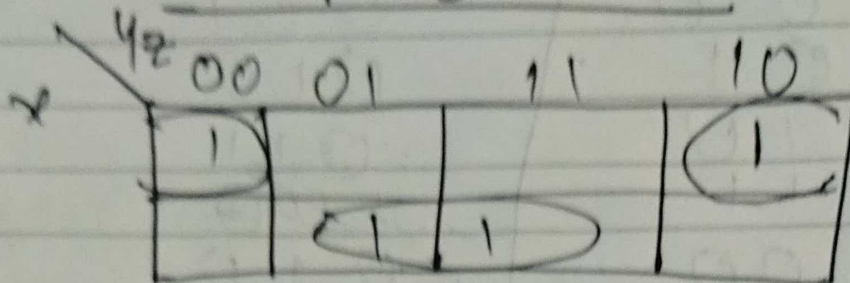
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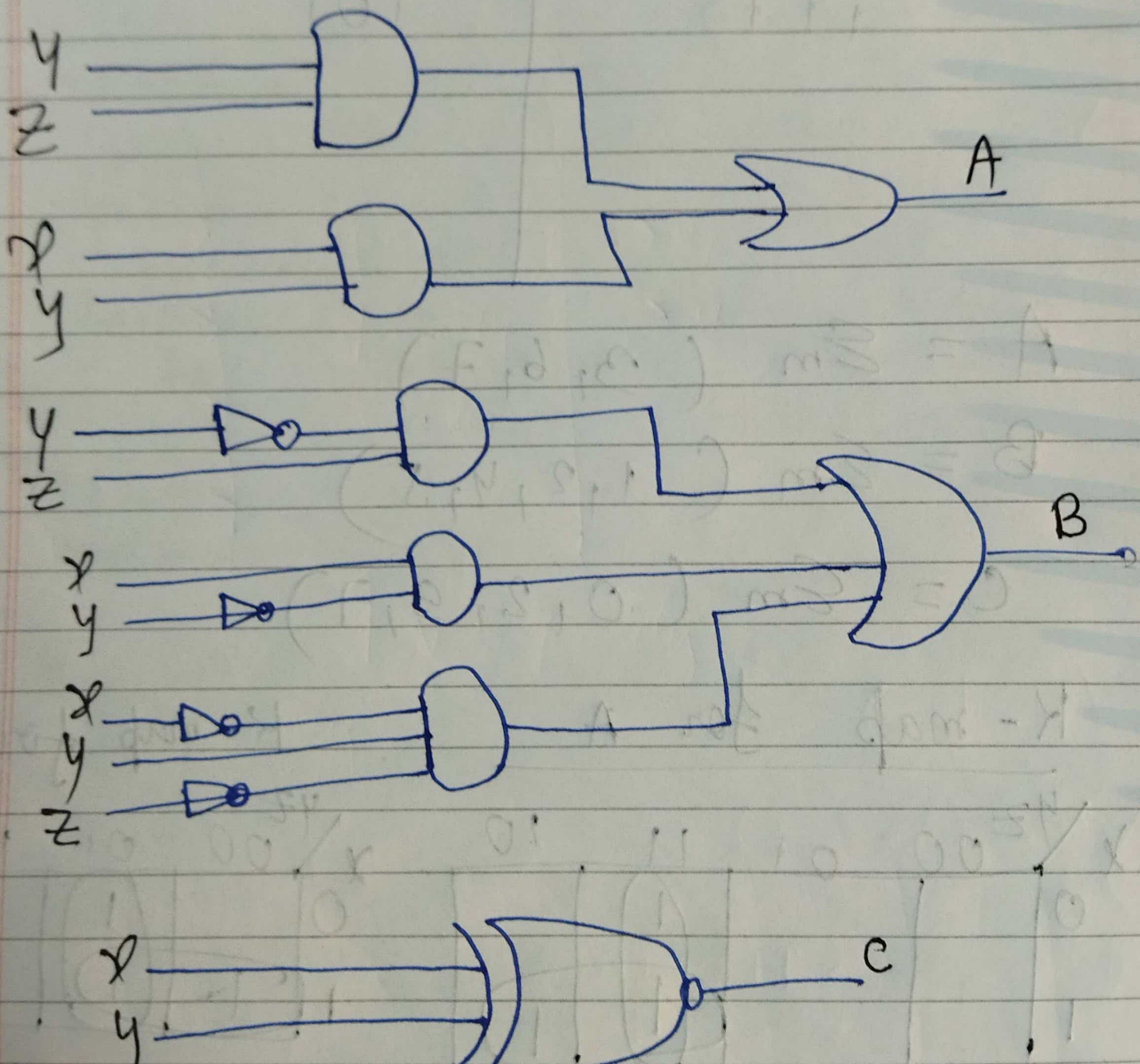
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K-map for c



Circuit



7.

A	B	C	Bx	Diff
0	0	0	0	0
0	0	1	1	1
0	1	0	1	1
0	1	1	1	0
1	0	0	0	1
1	0	1	0	0
1	1	0	0	0
1	1	1	1	1

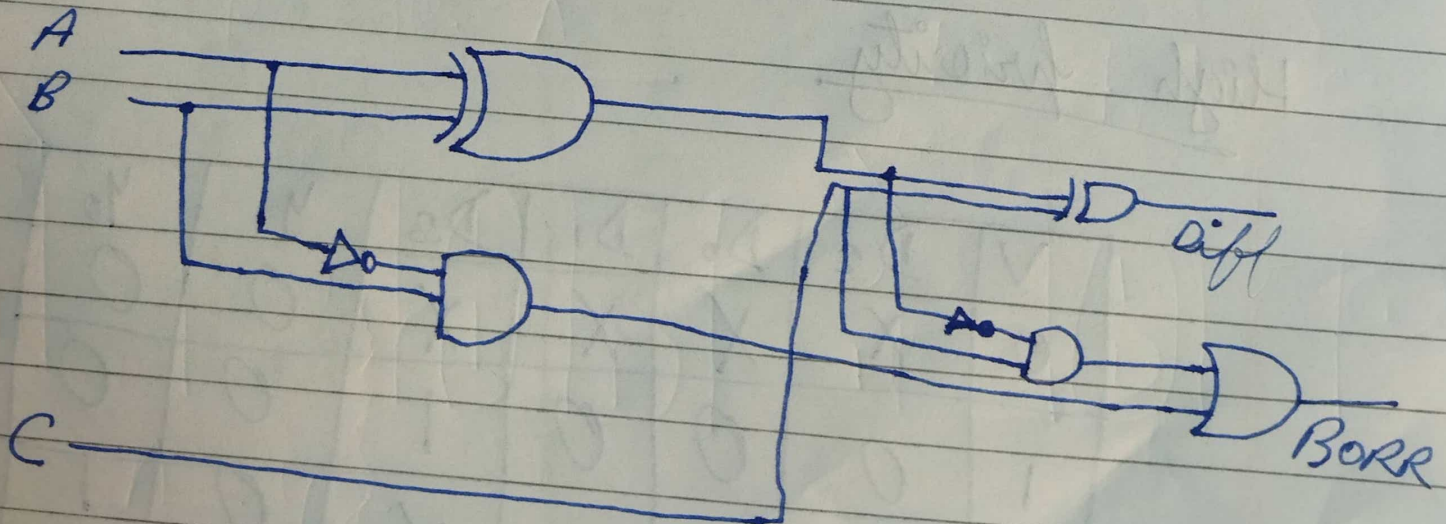
$$Bx = \sum m(1, 2, 3, 7)$$

$$Diff = \sum m(1, 2, 4, 7)$$

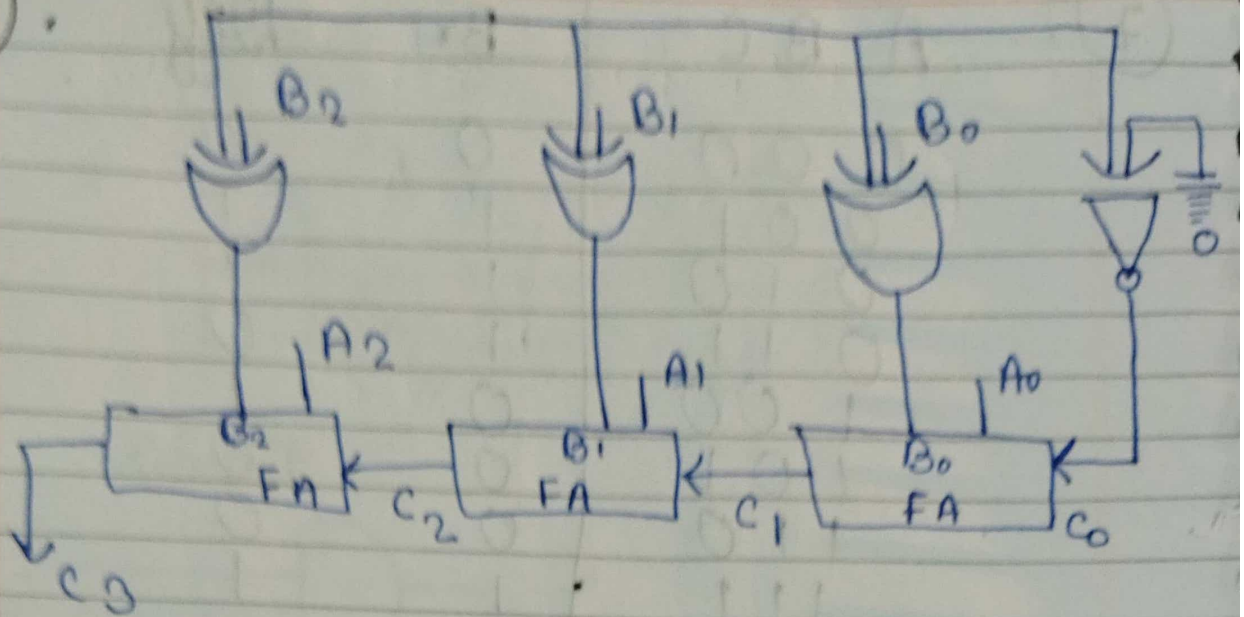
from K-map,

$$Bx = \bar{A}B + \bar{A}C + BC$$

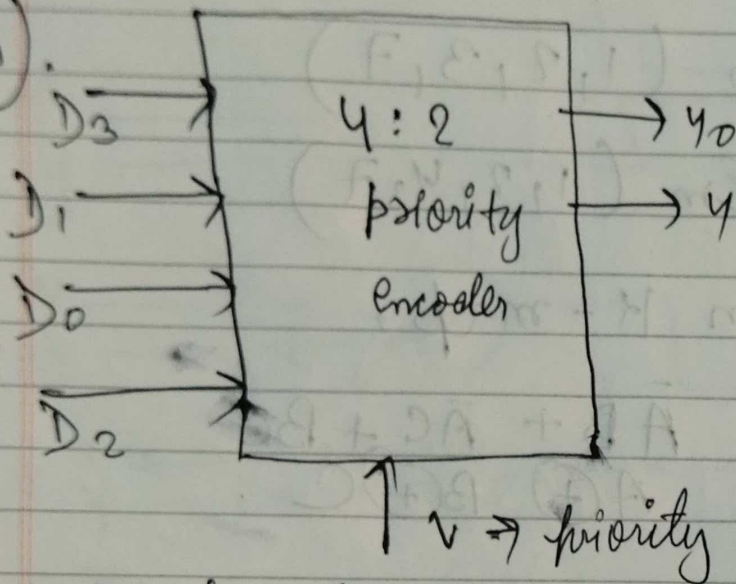
$$Diff = A \oplus B \oplus C$$



8.



9.



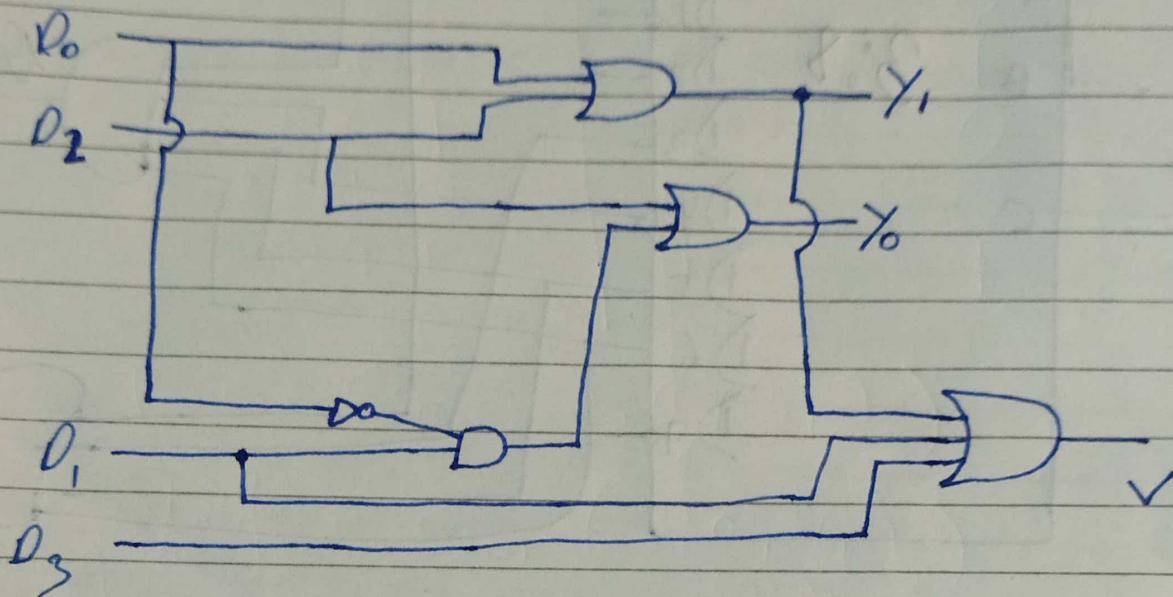
High priority

V	D ₂	D ₀	D ₁	D ₃	Y ₁	Y ₀
0	X	X	X	X	0	0
1	0	0	0	1	0	0
1	0	0	1	X	0	1
1	0	1	X	X	1	0
1	1	X	X	X	1	1

$$Y_0 = D_1 \bar{D}_0 \bar{D}_2 + D_2 \Rightarrow D_1 \bar{D}_0 + D_2$$

$$Y_1 = D_0 \bar{D}_2 + D_2 \Rightarrow D_0 + D_2$$

$$V = D_0 + D_1 + D_2 + D_3$$



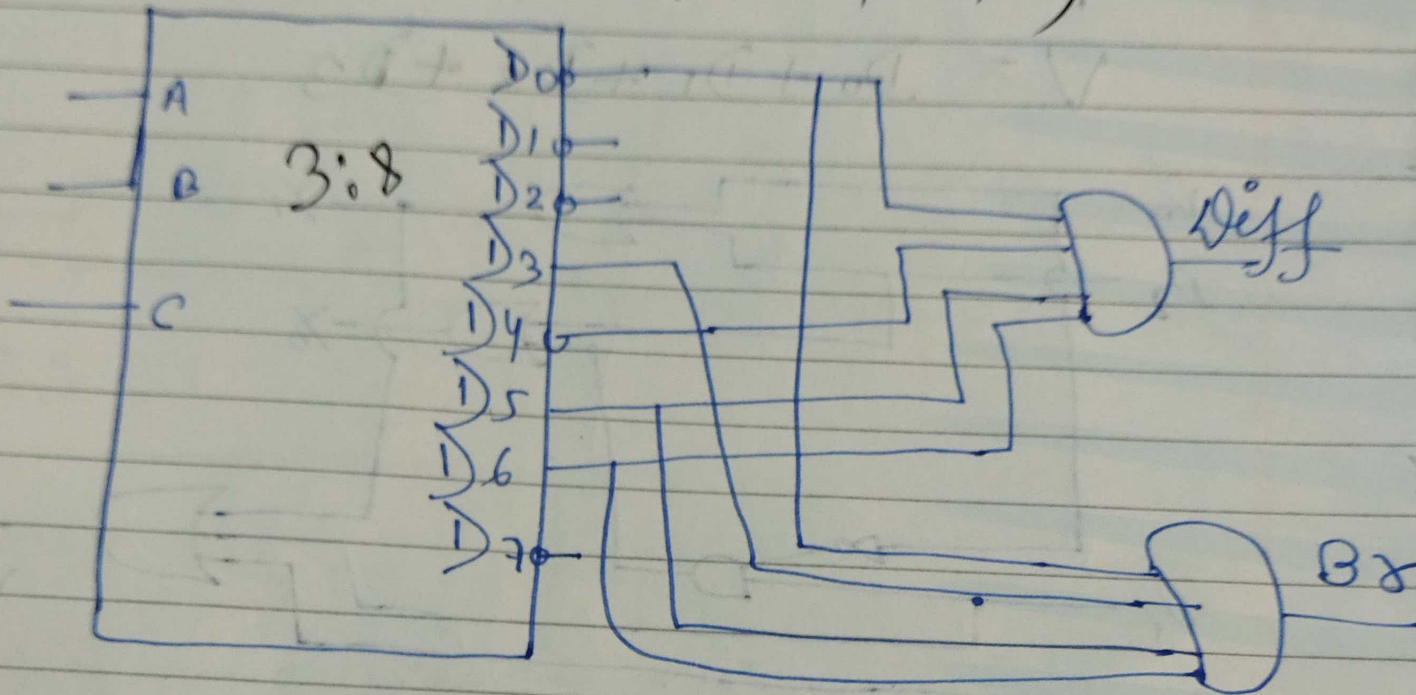
(10).

A	B	C	Diff	B _x
0	0	0	0	0
0	0	1	1	1
0	1	0	1	1
0	1	1	1	0
1	0	0	0	1
1	0	1	0	0
1	1	0	0	0
1	1	1	1	1

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$$W_{diff} = \pi_m (0, 4, 5, 6)$$

$$B_x = \pi_m (0, 3, 5, 6)$$



10			
A	B	C	diff
0	0	0	0
0	0	1	0
0	1	0	0
0	1	1	0
1	0	0	1
1	0	1	0
1	1	0	0
1	1	1	0