

ASSIGNMENT 3

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Abstract—This document solves determinant of a matrix using its properties

Download all python codes from

https://github.com/anjanavasudevan/grad_schoolwork/tree/master/EE5609/Assignment3/code

and latex-tikz codes from

https://github.com/anjanavasudevan/grad_schoolwork/tree/master/EE5609/Assignment3/latex

$$\Rightarrow (a-b)(b-c) \begin{vmatrix} 0 & 0 & 1 \\ 0 & 1 & c \\ (a^2 - c^2) + b(a-c) & b^2 + bc + c^2 & c^3 \end{vmatrix} \quad (2.0.5)$$

$$\Rightarrow (a-b)(b-c) \begin{vmatrix} 0 & 0 & 1 \\ 0 & 1 & c \\ k & b^2 + bc + c^2 & c^3 \end{vmatrix} \quad (2.0.6)$$

Where

$$k = (a-c)(a+c) + b(a-c) \quad (2.0.7)$$

$$\Rightarrow (a-b)(b-c)(a-c) \begin{vmatrix} 0 & 0 & 1 \\ 0 & 1 & c \\ a+b+c & b^2 + bc + c^2 & c^3 \end{vmatrix} \quad (2.0.8)$$

$$= (a-b)(b-c)(a-c)(-1)(a+b+c) \quad (2.0.9)$$

$$= (a-b)(b-c)(c-a)(a+b+c) \quad (2.0.10)$$

1 QUESTION No. 16 (II)

By using properties of determinants, show that:

$$\begin{vmatrix} 1 & 1 & 1 \\ a & b & c \\ a^3 & b^3 & c^3 \end{vmatrix} = (a-b)(b-c)(c-a)(a+b+c) \quad (1.0.1)$$

2 ANSWER

Using column operations to simplify the equation, we get:

$$\begin{vmatrix} 1 & 1 & 1 \\ a & b & c \\ a^3 & b^3 & c^3 \end{vmatrix} \xrightarrow{C_1 \rightarrow C_1 - C_2} \begin{vmatrix} 0 & 1 & 1 \\ a-b & b & c \\ a^3 - b^3 & b^3 & c^3 \end{vmatrix} \quad (2.0.1)$$

$$\begin{vmatrix} 0 & 1 & 1 \\ a-b & b & c \\ a^3 - b^3 & b^3 & c^3 \end{vmatrix} \xrightarrow{C_2 \rightarrow C_2 - C_3} \begin{vmatrix} 0 & 0 & 1 \\ a-b & b-c & c \\ a^3 - b^3 & b^3 - c^3 & c^3 \end{vmatrix} \quad (2.0.2)$$

$$(a-b)(b-c) \begin{vmatrix} 0 & 0 & 1 \\ 1 & 1 & c \\ a^2 + ab + b^2 & b^2 + bc + c^2 & c^3 \end{vmatrix} \quad (2.0.3)$$

$$\xrightarrow{C_1 \rightarrow C_1 - C_2} (a-b)(b-c) \begin{vmatrix} 0 & 0 & 1 \\ 0 & 1 & c \\ a^2 + ab - bc - c^2 & b^2 + bc + c^2 & c^3 \end{vmatrix} \quad (2.0.4)$$