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Representation of 2D images



64x64 x 3

- These 2D images are represented in matrix.
- dimensions=(n_h, n_w, n_c)
- n_h =height of image
- n_w =width of image
- n_c =number of channels
- Single channel image: $n_c=1$

Convolution

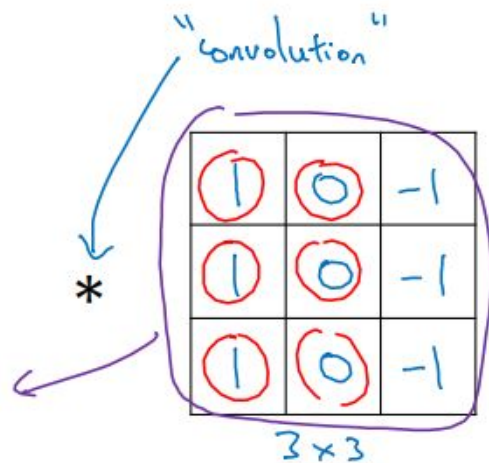
- We convolve an image using a kernel /filter.
- Convolve means
 - Place filter over a region of image
 - Multiply corresponding elements of image and filter.
 - And add it.
 - This value is O_{ij} .
- Parameters
 - Stride
 - Padding
 - Filter Size
 - Number of filters

Convolution

$$\rightarrow 3 \times 1 + 1 \times 1 + 2 \times 1 + 0 \times 0 + 5 \times 0 + 7 \times 0 + 1 \times -1 + 8 \times -1 + 2 \times -1 = -5$$

3	0	1	2	7	4
1	5	8	9	3	1
2	7	2	5	1	3
0	1	3	1	7	8
4	2	1	6	2	8
2	4	5	2	3	9

6x6



=

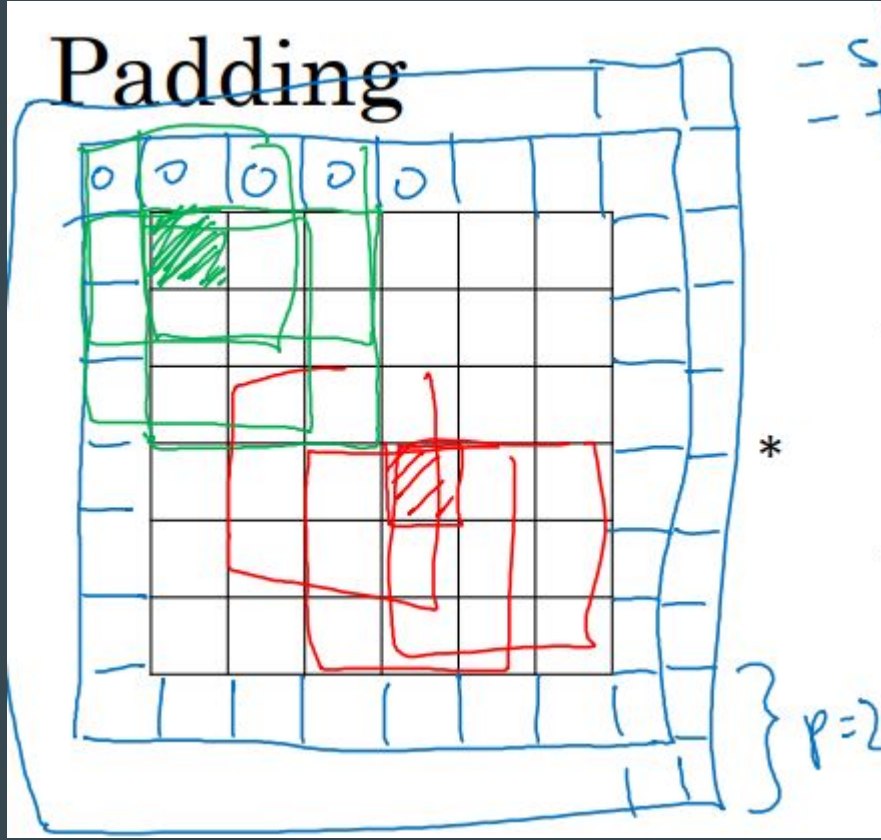
-5	-4	0	8
-10	-2	2	3
0	-2	-4	-7
-3	-2	-3	-16

4x4

Basic Convolution

- $n_{h/w}^l = (n_{h/w} - f) + 1$
- In the given example
 - $n_{h/w} = 6$
 - $f = 3$
 - $n^l = (6 - 3) + 1 = 4$

Padding

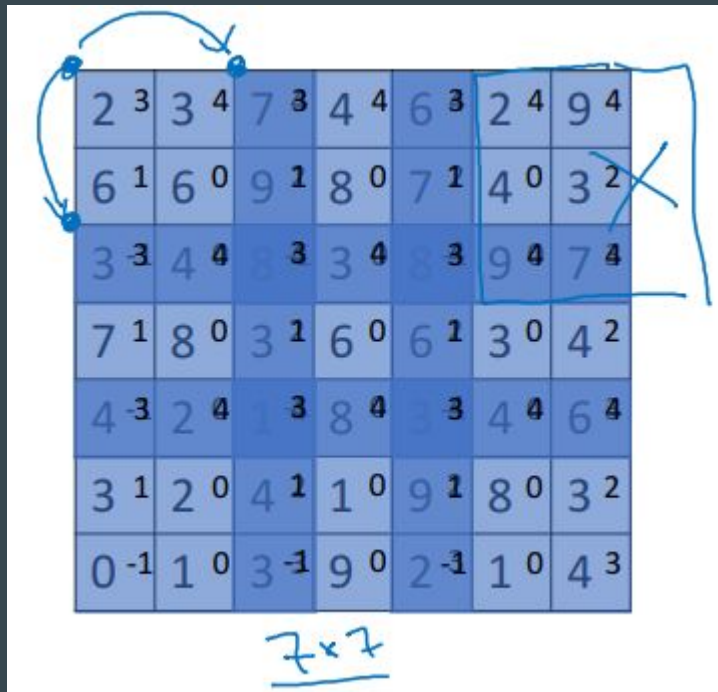


- Add extra boundary cells to the image
- For 1 layer of padding 2 cells are added to each row and column.
- We do to make input and output dimension to be same
- And a boundary pixels get involved in convolution less number of times compared to center pixels.

Padding

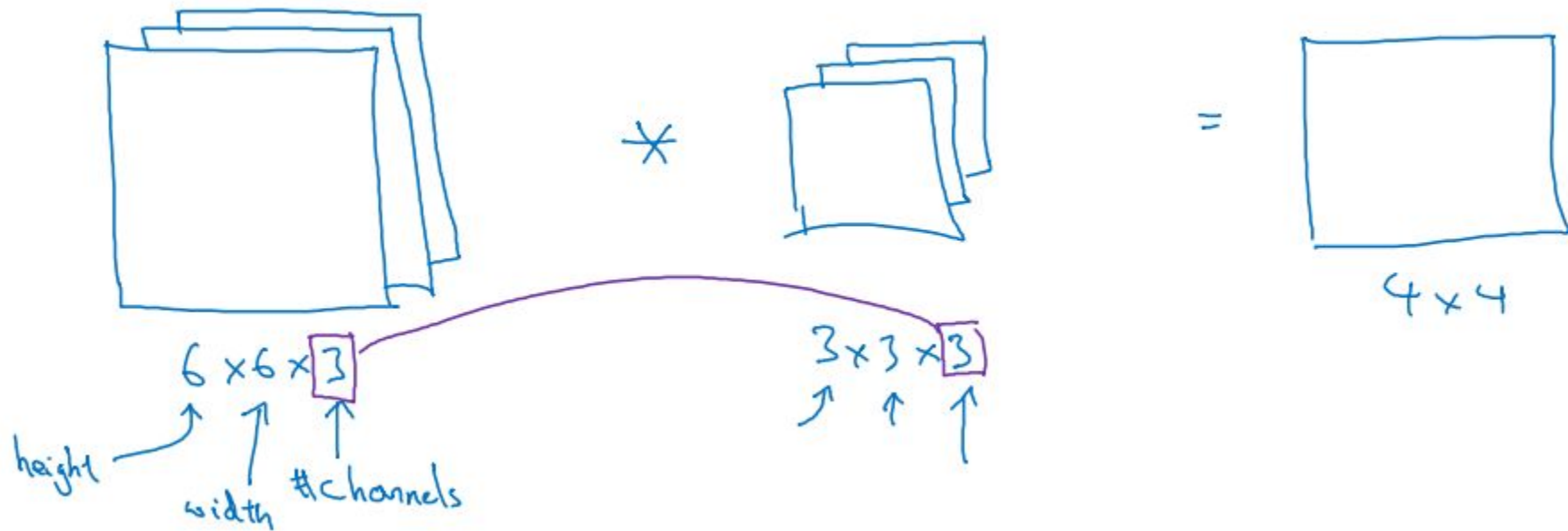
- Valid Convolution: No padding
- Same Convolution: Padding is done to make input size equals to output size.
 - $n+2p-f+1=n$
 - $p=(f-1)/2$

Stride



- We skip some possibilities of convolution.
- $n_{h/w}^l = (n_{h/w} + 2p - f) / s + 1$
- Example:
- stride=2
- Filter size=3
- $7*7 \rightarrow (7-3)/2+1 = (4*4)$

Multi Channel CNN

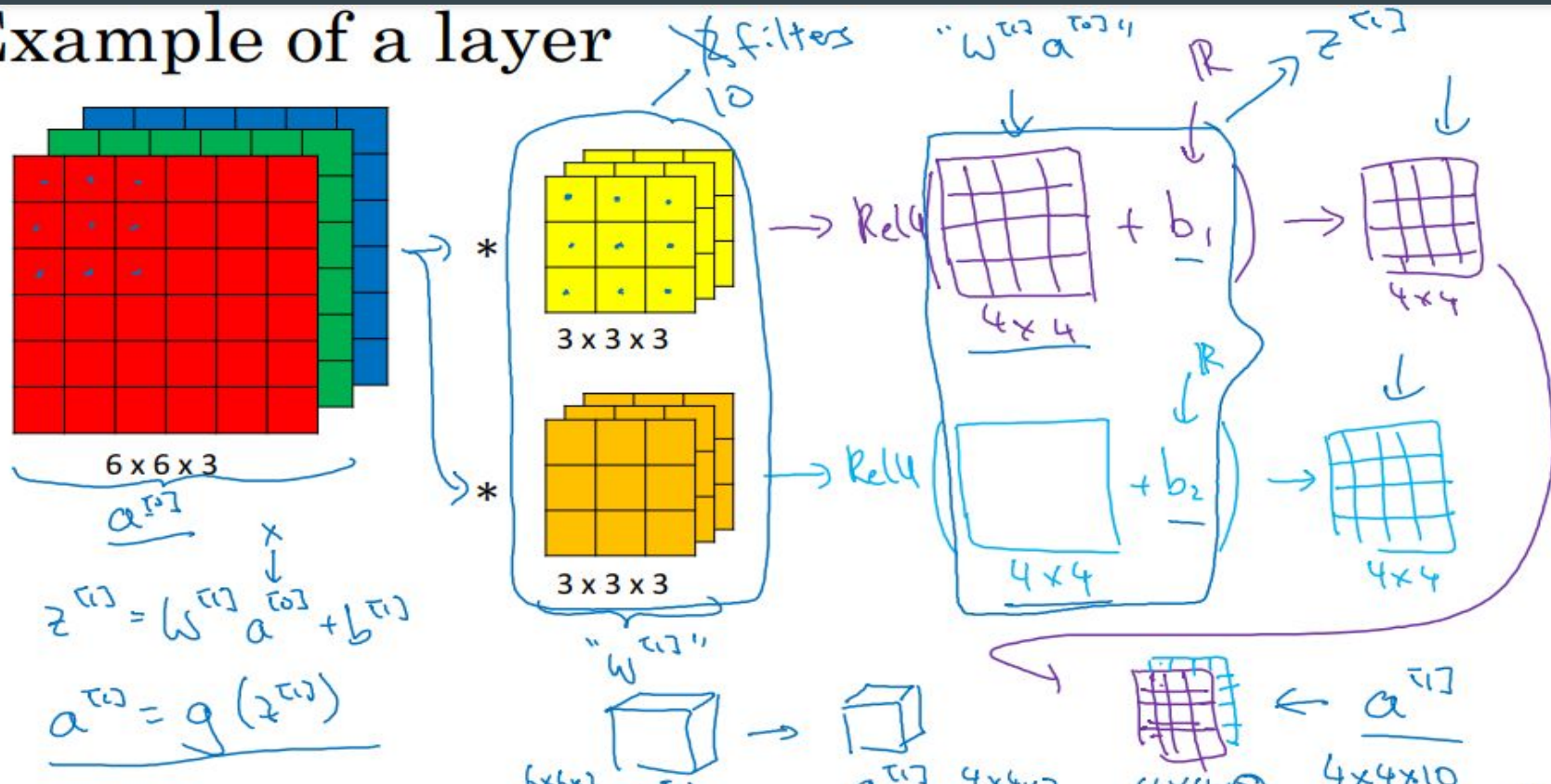


Multi Channel CNN

- Number of Filter channels must be equal to Number of Input channels.
- Single Filter produce a 2D feature map.
- $O_{ij} = \text{over a region}(\text{conv}(\text{img}_1, k_1) + \text{conv}(\text{img}_2, k_2) + \text{con}(\text{img}_3, k_3))$.
- Multiple Filters produce multiple feature maps.
- Each feature map is added with it's bias and applied non linearity function.
- And stack them and it's another conv layer.
- $n' = (n + 2p - f) / s + 1$
- Dimensions of output of convolution: (n'_h, n'_w, n'_c) .
- n_c = Number of filters in that layer.

Multi Channel CNN

Example of a layer



Summary of Notations

- Filter Size : $F^{[l]}$
- Padding : $P^{[l]}$
- Stride : $S^{[l]}$
- Number of Filters: $n_c^{[l]}$
- Input : $(n_h^{[l-1]}, n_w^{[l-1]}, n_c^{[l-1]})$
- Output : $(n_h^{[l]}, n_w^{[l]}, n_c^{[l]})$
- Each Filter : $(F^{[l]}, F^{[l]}, n_c^{[l-1]})$
- Weights: (filtersize, filtersize, number of channels, Number of filters)
-

$n \times n$ image $f \times f$ filter

padding p stride s

Output Size:

$$\left\lfloor \frac{n+2p-f}{s} + 1 \right\rfloor \times \left\lfloor \frac{n+2p-f}{s} + 1 \right\rfloor$$

Pooling Layer

- Commonly used max pooling.
- Used to
 - Reduce the size of representation.
 - Detect features effectively.
- This nothing but a filter over a region and taking value as max in that region.
- Hyperparameters of max pooling:
 - Filter size
 - Stride
 - Padding
- No Parameters to learn.
- Commonly used Hyperparams (f,s) : (2,2),(3,2)

Pooling

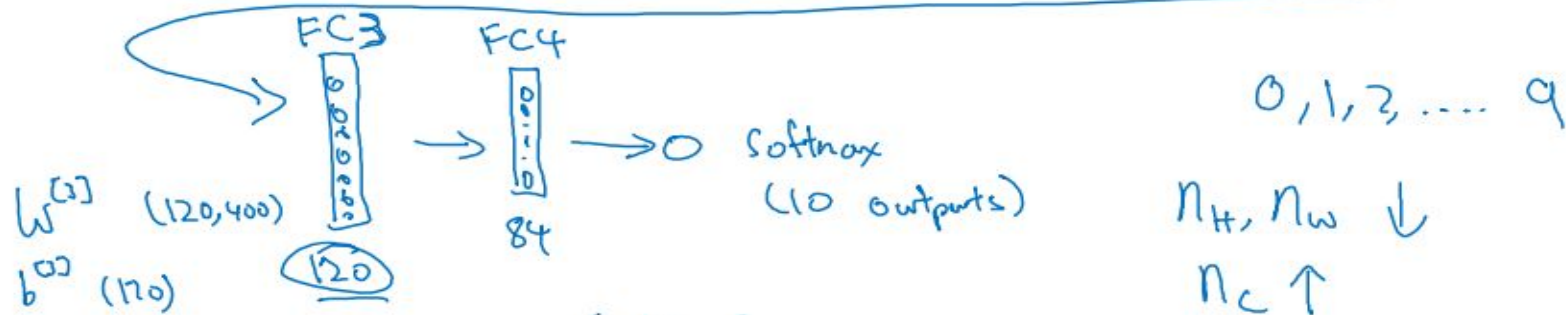
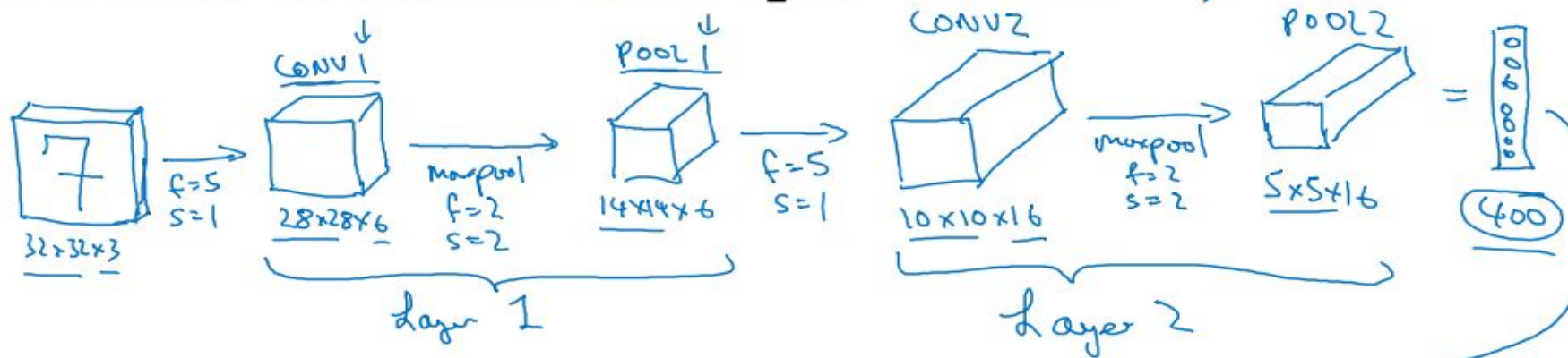
1	3	2	1
2	9	1	1
1	3	2	3
5	6	1	2

Advantages of CNN over Traditional NN

- Parameter Sharing: same parameters are used to for all regions
- Sparsity of Connections : each output node depend only on few nodes of input layer instead of depending on all nodes.

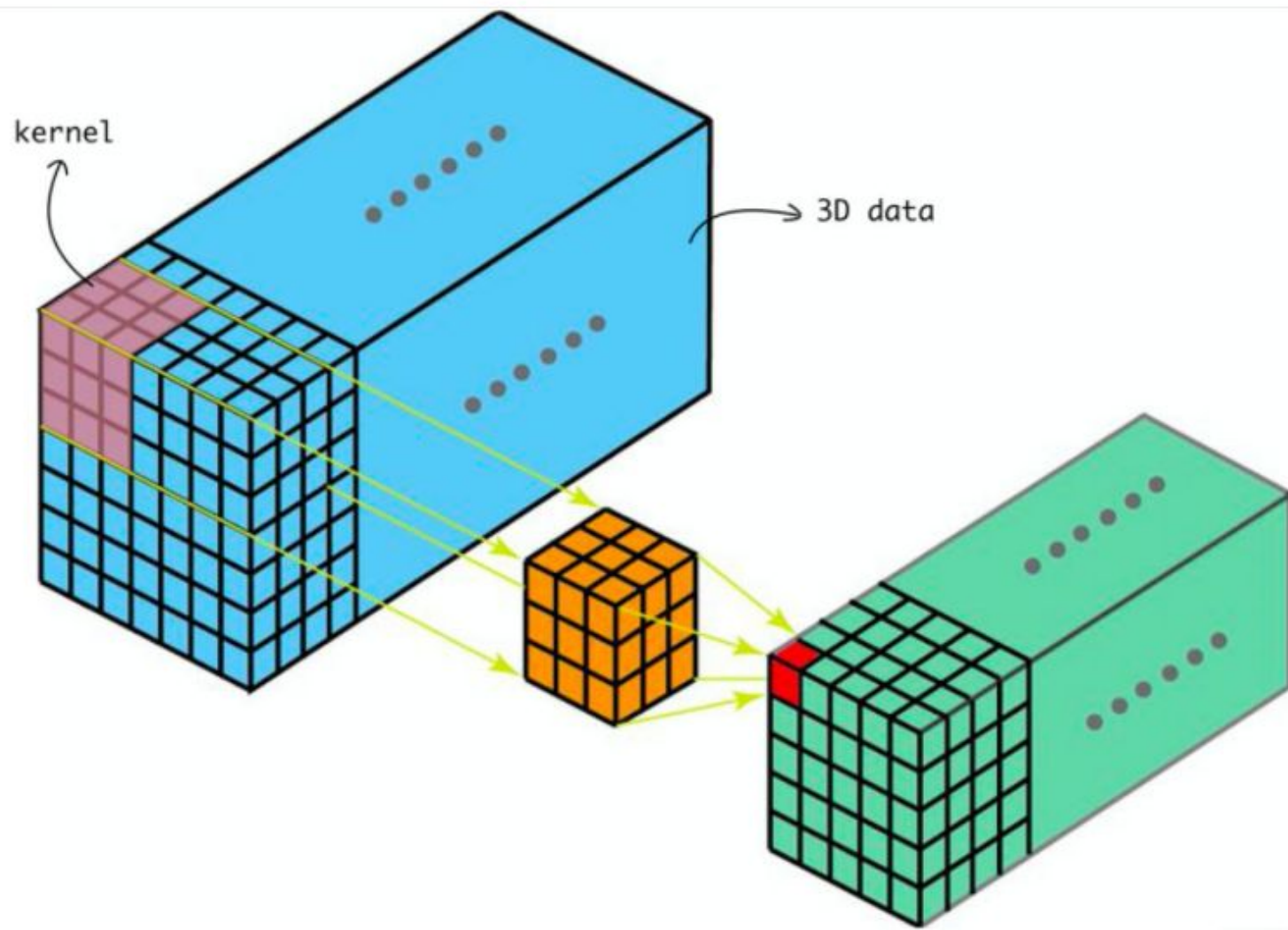
Example Model

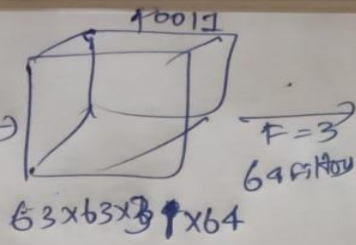
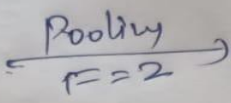
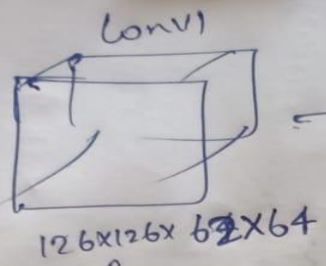
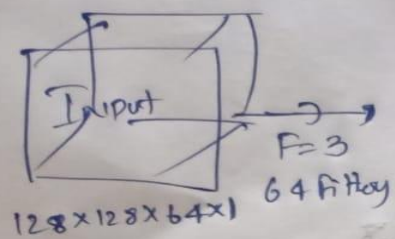
Neural network example (LeNet-5)



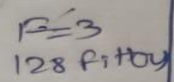
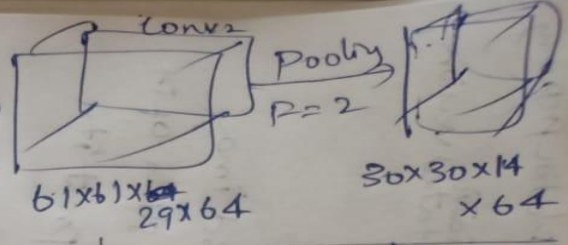
3D CNN (Single Channel)

- Each channel consists of 3D data.
- Input Image : (height,width,depth,# of in_channels)
- Kernel size : (F,F,depth',# of in_channels)
- Weights size : (F,F,depth',# of in_channels,# of filters)
- Output size : (height',width',depth',# of filters)
- Mostly height and width are same but depth may not be.
- Same for kernel also
- Convolution Process:
 - Left to right
 - Top to Bottom
 - Go in
- Output of Each filter is 3D data.

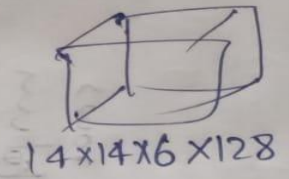
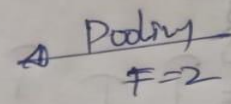
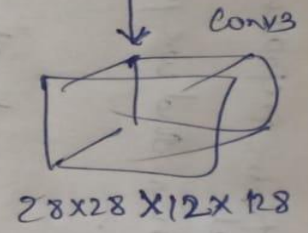




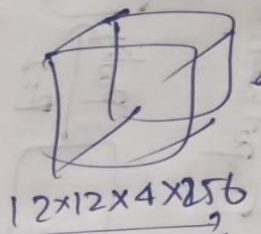
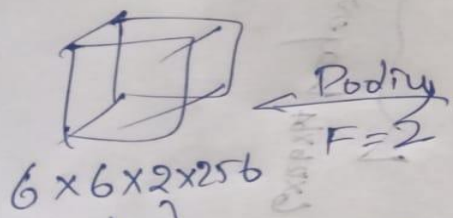
Layer 1



Layer 2



Layer 3



Layer 4

