# Transfer Learning

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### Outline

Outline



- 1 Motivation
- 2 Historical points
- 3 Definition
- 4 Case studies



## Outline

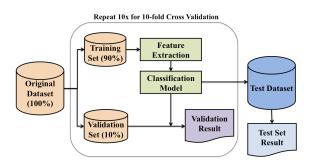


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# Standard Supervised Learning Task

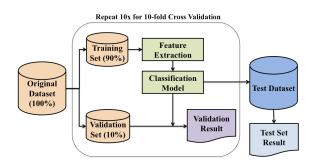






# Standard Supervised Learning Task



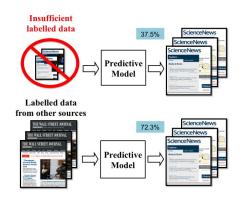


■ Most ML tasks assume the training/test data are drawn from the same data space and the same distribution



# NLP tasks: POS, NER, Category labelling



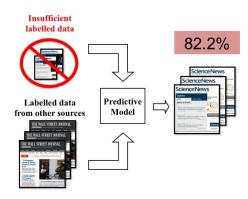


Modified from Gao et al.'s presentation in KDD '08



## Combine and get better result





Modified from Gao et al.'s presentation in KDD '08



#### Motivation

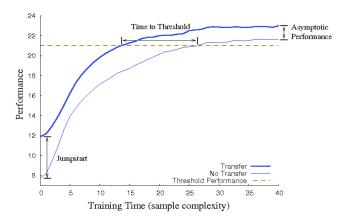


- Traditional ML tasks assume the training/test data are drawn from the same data space and the same distribution
- Insufficient labelled data result in poor prediction performance
  - Lots of (un-)related existing data from various sources
- Start from scratch is always time-consuming
- Transfer knowledge from other sources may help!



# Motivation (Taylor et.al JMLR '09)







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# Psychology and Education



■ In 1901, Thorndike and Woodworth explored how individuals transfer similar characteristics shared by different contexts



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## Psychology and Education



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- In 1992, Perkins and Salomon published "Transfer of Learning" which defined different types of transfer





- In 1901, Thorndike and Woodworth explored how individuals transfer similar characteristics shared by different contexts
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- examples:
  - Skill learning:  $C/C + + \rightarrow Python$
  - Language acquisition:  $German \rightarrow English$



## Machine Learning

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# Machine Learning

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 Explanation-Based Neural Network Learning: A Lifelong Learning Approach [Thrun PhD '95, NIPS '96]



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## Machine Learning



- Explanation-Based Neural Network Learning: A Lifelong Learning Approach [Thrun PhD '95, NIPS '96]
- Multitask Learning [Caruana ICML '93 & '96, PhD '97]



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### Machine Learning



- Explanation-Based Neural Network Learning: A Lifelong Learning Approach [Thrun PhD '95, NIPS '96]
- Multitask Learning [Caruana ICML '93 & '96, PhD '97]
- Workshops
  - Learning to Learn: Knowledge Consolidation and Transfer in Inductive Systems [NIPS '95]
  - Inductive Transfer: 10 Years Later [NIPS '05]
  - Structural Knowledge Transfer for Machine Learning [ICML '06]
  - Transfer Learning for Complex Tasks [AAAI '08]
  - Lifelong Learning [AAAI '11]
  - Theoretically Grounded Transfer Learning [ICML '13]
  - Workshop: Second Workshop on Transfer and Multi-Task Learning: Theory meets Practice [NIPS '14]
  - ...



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#### **Notations**

- $\blacksquare$  Domain  $\mathcal{D}$ 
  - 1 Data space  $\mathcal{X}$
  - 2 Marginal distribution P(X), where  $X \in \mathcal{X}$
- Task  $\mathcal{T}$  (Given  $\mathcal{D} = {\mathcal{X}, P(X)}$ )
  - 1 Label space  $\mathcal{Y}$
  - **2** Learn a  $f: X \to Y$  to approach the underlying P(Y|X), where  $X \in \mathcal{X}$  and  $Y \in \mathcal{Y}$





Assume we have only one source S and one target T:

#### Definition

Transfer Learning (TL): Given a source domain  $\mathcal{D}_S$  and learning task  $\mathcal{T}_S$ , a target domain  $\mathcal{D}_T$  and learning task  $\mathcal{T}_T$ , transfer learning aims to help improve the learning of the target predictive function  $f_T(\cdot)$  in  $\mathcal{D}_T$  using the knowledge in  $\mathcal{D}_S$  and  $\mathcal{T}_S$ , where

$$\mathcal{D}_S \neq \mathcal{D}_T$$
 (either  $\mathcal{X}_S \neq \mathcal{X}_T$  or  $P_S(X) \neq P_T(X)$ )

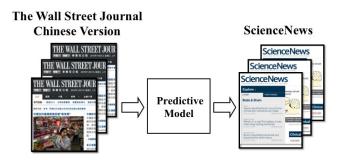
or 
$$\mathcal{T}_S \neq \mathcal{T}_T$$
 (either  $\mathcal{Y}_S \neq \mathcal{Y}_T$  or  $P(Y_S|X_S) \neq P(Y_T|X_T)$ )



## Example: Category labelling

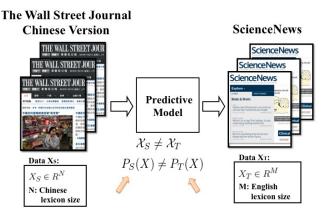
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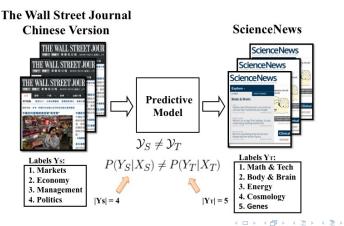








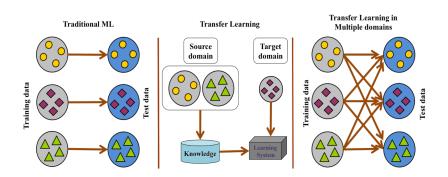




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# ML v.s. TL (Langley '06, Yang et al. '13)







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### Transfer in practice



The rest of the talk will give you an intuition, with examples, on:

- when to transfer
- what to transfer
- and how to transfer

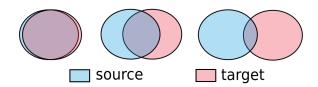


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#### When to transfer: Domain relatedness



Transfer learning is applicable when there exists relatedness



- Standard machine learning assume source = target
- Transferring knowledge from unrelated domain can be harmful
  - Negative transfer [Rosenstein et al NIPS-05 Workshop]
- (Ben-David et al.) proposed a bound of target domain error

#### Reference

Ben-David et al. Analysis of Representation for Domain Adaptation. NIPS '06



# When to transfer (Ben-David et al.)



In standard binary classification supervised learning task:

- Given  $X, Y = \{0,1\}$  and samples from P(x,y), we aim to learn  $f: X \to [0,1]$  which captures P(y|x)
- Often we decompose the problem into:
  - **1** determine a feature mapping  $\Phi: X \to Z$
  - **2** learn a hypothesis  $h: Z \to \{0,1\}$  on dataset  $\{\Phi(x), y\}$

In transfer learning scenario:

#### Theorem (Simplified version of Thm. 1&2)

Given  $X = X_S = X_T$  and  $P_S(x), P_T(x)$  the distributions of the source and target domain. Let  $\Phi: X \to Z$  be a fixed mapping function and  $\mathcal H$  be a hypothesis space. For any hypothesis  $h \in \mathcal H$  trained on source domain:

$$\epsilon_{\mathcal{T}}(h) \leq \epsilon_{\mathcal{S}}(h) + d_{\mathcal{H}}(\tilde{P}_{\mathcal{S}}, \tilde{P}_{\mathcal{T}}) + \epsilon_{\mathcal{S}}(h^*) + \epsilon_{\mathcal{T}}(h^*)$$

where  $\tilde{P}_S$ ,  $\tilde{P}_T$  are induced distributions on Z wrt.  $P_S$  and  $P_T$ ,  $h^* = \arg\min_{h \in \mathcal{H}} (\epsilon_S(h) + \epsilon_T(h))$  is the best hypothesis by joint training.

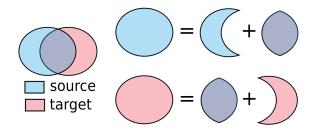
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### Domain adaptation



Approach 1: mixture of general & specific component



Can we learn hypotheses for both the general and specific components?

#### Reference:

Daume III. Frustratingly easy domain adaptation. ACL '07
Daume III et al. Co-regularization Based Semi-supervised Domain Adaptation.
NIPS '10



Binary classification problem:

- $X_S = X_T \subset \mathbb{R}^d$ ,  $Y_S = Y_T = \{-1, +1\}$
- Goal: obtain classifier  $f_T: X_T \to Y_T$
- lacksquare in SVM context: learn a hypothesis  $h_T \in \mathcal{R}^d$

#### However:

- too little training data available on  $(X_T, Y_T)$  for robust training
- also  $P(x_S) \neq P(x_T)$  and  $P(x_S, y_T) \neq P(x_S, y_T)$
- lacktriangleright ...so directly apply a trained hypothesis  $h_s$  returns bad results

How to use  $x_S, y_S \sim P(x_S, y_S)$  to improve learning of  $h_T$ ?





#### EasyAdapt algorithm

■ define two mappings  $\Phi_S, \Phi_T : \mathcal{R}^d \to \mathcal{R}^{3d}$ :

$$\Phi_S(x_S) = (x_S, x_S, 0), \quad \Phi_t(x_T) = (x_T, 0, x_T)$$

- training: learn a hypothesis  $h = (w^g, w^s, w^t) \in \mathcal{R}^{3d}$  on transformed dataset  $\{(\Phi_S(x_S), y_S)\} \cup \{(\Phi_T(x_T), y_T)\}$
- test: apply  $h_T = w^g + w^t$  on  $x_T$



Transfer Learning



Use unlabelled data to improve training:

• want  $h_S$  and  $h_T$  to agree on unlabelled data  $x_U$ :

$$h_S \cdot x_U = h_T \cdot x_U \Leftrightarrow w^s \cdot x_U = w^t \cdot x_U \Leftrightarrow h \cdot (0, x_U, -x_U) = 0$$

lacksquare so we define mapping  $\Phi_U:\mathcal{R}^d o\mathcal{R}^{3d}$  for unlabelled data

$$\Phi_{U}(x_{U}) = (0, x_{U}, -x_{U}) \tag{1}$$

■ and train the hypothesis h on augmented and transformed dataset  $\{(\Phi_S(x_S), y_S)\} \cup \{(\Phi_T(x_T), y_T)\} \cup \{(\Phi_U(x_U), 0)\}$ 

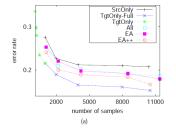


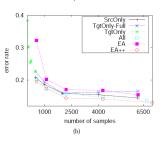
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# EA++ (Daume III et al.)



- (a) DVD → BOOKS (proxy A-distance=0.7616),
- (b) KITCHEN → APPAREL (proxy A-distance=0.0459).





- SOURCE/TARGETONLY(-FULL): trained on source/target (full) labelled samples
- ALL: trained on combined labelled samples
- EA/EA++: trained in augmented feature space (and unlabelled target data)



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#### Feature transfer



Approach 2: shared lower-level features





- DNN first layer learns Gabor filters or color blobs when trained on images
- instances in source/target domain share the same lower-level features?

#### Reference:

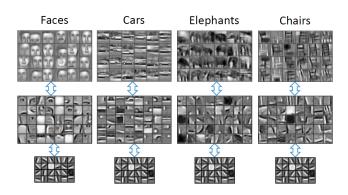
Yosinski et al. How transferable are features in deep neural networks? NIPS '14.



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### Feature transfer<sup>1</sup>





Lee et al. Convolutional deep belief networks for scalable unsupervised learning of hierarchical representations. ICML  $^\prime 09$ 

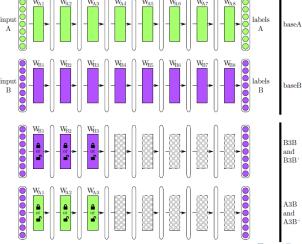
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<sup>&</sup>lt;sup>1</sup>adapt from Ruslan Salakhutdinov's tutorial in MLSS'14 Beijing → ⋅ ϶ → ϶ → ໑ < ૦

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# Feature transfer (Yosinski et al.)



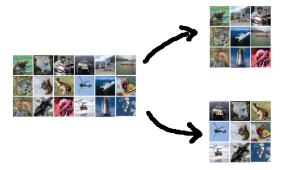


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Test 1 (similar datasets): random A/B splits of the ImageNet dataset

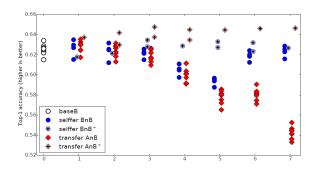


(similar source and target domain training/testing instances)





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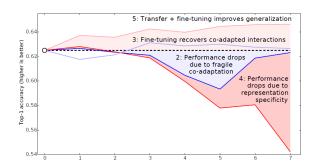


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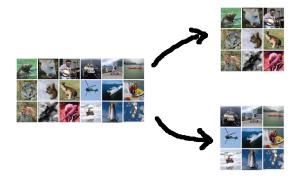


(similar source and target domain training/testing instances)





Test 2 (very different datasets): man-made/natural object split

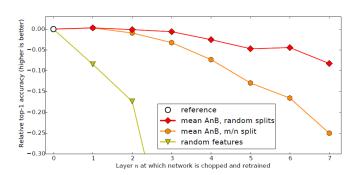


(dissimilar source and target domain training/testing instances)





Test 2 (very different datasets): man-made/natural object split



(dissimilar source and target domain training/testing instances)



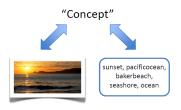
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#### Joint representation



Approach 3: joint feature representation



- data has many domain specific characteristics
- however might be related in high level?
- our brain might work like this as well

#### Reference:

Srivastava and Salakhutdinov. Multimodal Learning with Deep Boltzmann Machines. NIPS '12, JMLR 15 (2014).

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### Joint representation (Srivastava et al.)

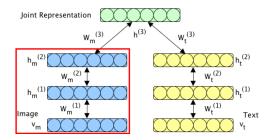


#### MIR Flickr Dataset http://press.liacs.nl/mirflickr/



- For images
  - 1M datapoints, 25K labelled instances in 38 classes, 10K for training, 5K for validation and 10K for testing
  - inputs are the concatenation of PHOW and MPEG-7 features
- For texts
  - use word count vectors on 2K frequently used tags (very sparse)





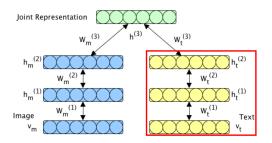
for images: 2-layer deep Boltzmann machine (DBM) with Gaussian input units  $(v_{mi} \in \mathbb{R}, \text{ abbrev. } W_m^{(k)}(i,j) \text{ as } W_{ii}^{(k)})$ 

$$P(v_m, h_m^{(1)}, h_m^{(2)}) \propto$$

$$\exp\left(-\sum_{i}\frac{(v_{mi}-b_{i})^{2}}{2\sigma_{i}^{2}}+\sum_{i,j}\frac{v_{mi}}{\sigma_{i}}W_{ij}^{(1)}h_{mj}^{(1)}+\sum_{j,l}h_{mj}^{(1)}W_{jl}^{(2)}h_{ml}^{(2)}\right)$$

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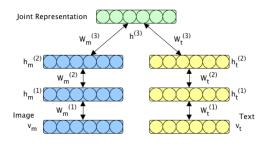


for texts: 2-layer DBM with replicated softmax model ( $v_{ti}$  counts the occurrence of word i, abbrev.  $W_t^{(k)}(i,j)$  as  $W_{ii}^{(k)}$ 

$$P(v_t, h_t^{(1)}, h_t^{(2)}) \propto$$

$$\exp\left(-\sum_{i=1} v_{ti}b_i + \sum_{i,j} v_{ti}W_{ij}^{(1)}h_{mj}^{(1)} + \sum_{j,l} h_{tj}^{(1)}W_{ji}^{(2)}h_{tl}^{(2)}\right)$$





combining domain specific models to a multimodal DBM:

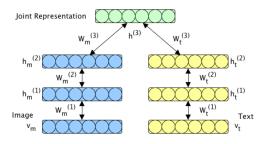
$$P(v_m, v_t, h; \theta) \propto$$
  
 $\exp\left(-E(h_m^{(2)}, h_t^{(2)}, h_t^{(3)}) - E(v_m, h_m^{(1)}, h_m^{(2)}) - E(v_t, h_t^{(1)}, h_t^{(2)})\right)$ 



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#### Joint representation (Srivastava et al.)





- first pre-train domain specific DBMs with CD, then co-train the joint model with PCD
- use mean-field variational approximation when computing hidden unit moments driven by data





#### Results:

Model	MAP	${ m Prec@50}$
Random	0.124	0.124
SVM (Huiskes et al., 2010)	0.475	0.758
LDA (Huiskes et al., 2010)	0.492	0.754
DBM	$0.526 \pm 0.007$	$0.791 \pm 0.008$
DBM (using unlabelled data)	$0.585 \pm 0.004$	$\textbf{0.836} \pm 0.004$

#### Figure: Classification with data from both image and text domain

Model	MAP	Prec@50
Image LDA (Huiskes et al., 2010)	0.315	-
Image SVM (Huiskes et al., 2010)	0.375	-
Image DBN	$0.463 \pm 0.004$	$0.801 \pm 0.005$
Image DBM	$0.469 \pm 0.005$	$0.803 \pm 0.005$
Multimodal DBM (generated text)	$0.531\pm0.005$	$0.832\pm0.004$

Figure: Classification with data from image domain only



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### Joint representation (Srivastava et al.)



#### Results:

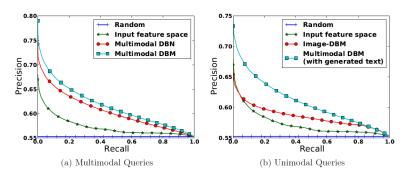


Figure: Retrieval results for multi/image domain queries



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#### Conclusions



In this talk, we showed that

- transfer learning adapts knowledge from other sources to improve target task performance
- domains related to each other in different ways

#### In the future:

- manage large scale data that do not lack in size but may lack in quality
- manage data which may continuously change over time



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### Open Questions<sup>2</sup>



- what are the limits of existing multi-task learning methods when the number of tasks grows while each task is described by only a small bunch of samples ("big T, small n")?
- what is the right way to leverage over noisy data gathered from the Internet as reference for a new task?
- how can an automatic system process a continuous stream of information in time and progressively adapt for life-long learning?
- can deep learning help to learn the right representation (e.g., task similarity matrix) in kernel-based transfer and multi-task learning?
- How can similarities across languages help us adapt to different domains in natural language processing tasks?
- ..

# Thank you



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#### Reference



- 1 Pan and Yang. A Survey on Transfer Learning. IEEE TKDE 2010
- 2 Pan and Yang. Transfer Learning. MLSS 2011
- 3 Taylor et al. Transfer Learning for Reinforcement Learning Domains: A Survey. JMLR 2010
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