

### 4.3

#2  $(A \vee B) \vee (A \wedge \neg B)$

If  $a = a$ , this is logically true

#3  $(A \vee B) \vee \neg(A \vee (B \wedge C))$

If  $a \neq a$ , this is logically false

### 4.19

If two sentences are tautologically equivalent, they are logically equivalent.

Thus,  $A \vee (B \wedge C)$  is logically equivalent to  $(A \wedge C) \vee (A \wedge B)$ , and not just taut equivalent. Tautological consequence is logical consequence. So now we know that  $A$  and  $B \vee \neg A$  logically imply  $A \wedge B$ .

However, logical consequence does not equal tautological consequence

$a = b$  is a logical consequence of  $b = a$ , but not  $a$ .

Likewise, Tautological equivalence implies TW equivalence, but not vice versa.

$[Cube(b) \wedge (LeftOf(a, b) \vee RightOf(a, b))] \wedge [Dodec(c) \wedge FrontOf(a, c)]$  may be TW equivalent but not Tautologically equivalent or logically equivalent.