# **Cutting Boards**

# Chinese Version Russian Version

Alice gives Bob a board composed of \$m \times n\$ wooden squares and asks him to find the minimum cost of breaking the board back down into individual \$1 \times 1\$ pieces. To break the board down, Bob must make cuts along its horizontal and vertical lines.

To reduce the board to squares,  $x_{n-1}$  vertical cuts must be made at locations  $x_1$ ,  $x_2$ ,  $x_{n-2}$ ,  $x_{n-1}$  and  $y_{m-1}$  horizontal cuts must be made at locations  $y_1$ ,  $y_2$ ,  $y_2$ ,  $y_4$ . Each cut along some  $x_i$  (or  $y_j$ ) has a cost,  $x_1$  (or  $x_1$ ). If a cut of cost  $x_2$  passes through  $x_1$  already-cut segments, the total cost of the cut is  $x_1$ .

The cost of cutting the whole board down into \$1 \times 1\$ squares is the sum of the cost of each successive cut. Recall that the cost of a cut is multiplied by the number of already-cut segments it crosses through, so each cut is increasingly expensive.

Can you help Bob find the minimum cost?

#### **Input Format**

The first line contains a single integer, \$T\$, denoting the number of test cases. The subsequent \$3T\$ lines describe each test case in \$3\$ lines.

For each test case, the first line has two positive space-separated integers, m and n, detailing the respective height (y) and width (x) of the board.

The second line has m-1 space-separated integers listing the cost,  $c_{y_j}$ , of cutting a segment of the board at each respective location from  $y_1$ ,  $y_2$ , dots,  $y_{m-2}$ ,  $y_{m-1}$ .

The third line has n-1 space-separated integers listing the cost,  $c_{x_i}$ , of cutting a segment of the board at each respective location from  $x_1$ ,  $x_2$ , \dots,  $x_{n-2}$ ,  $x_{n-1}$ .

**Note:** If we were to superimpose the \$m \times n\$ board on a 2D graph, \$x\_0\$, \$x\_n\$, \$y\_0\$, and \$y\_n\$ would all be edges of the board and thus not valid cut lines.

### Constraints

\$1 \le T \le 20\$ \$2 \le m,n \le 1000000\$ \$0 \le c\_{x\_i}, c\_{y\_j} \le 10^9\$

#### **Output Format**

For each of the \$T\$ test cases, find the minimum cost (\$MinimumCost\$) of cutting the board into \$1 \times 1\$ squares and print the value of  $$MinimumCost \ \% \ (10^9+7)$$ .

#### Sample Input

#### Input 00

```
1
2 2
2
1
```

#### Input 01

```
1
64
21314
412
```

#### **Sample Output**

#### **Output 00**

4

#### Output 01

42

## **Explanation**

**Sample 00:** We have a \$2 \times 2\$ board, with cut costs  $c_{y_1} = 2$  and  $c_{x_1} = 1$ . Our first cut is horizontal at  $y_1$ , because that is the line with the highest cost (\$2\$). Our second cut is vertical, at  $x_1$ . Our first cut has a \$TotalCost\$ of \$2\$, because we are making a cut with cost  $c_{y_1} = 2$  across \$1\$ segment (the uncut board). The second cut also has a \$TotalCost\$ of \$2\$, because we are making a cut of cost  $c_{x_1} = 1$  across \$2\$ segments. Thus, our answer is \$MinimumCost = ((2 \times 1) + (1 \times 2)) \ \% \ (10^9+7) = 4\$.

**Sample 01:** Our sequence of cuts is:  $\$y_5\$$ ,  $\$x_1\$$ ,  $\$y_3\$$ ,  $\$y_1\$$ ,  $\$x_3\$$ ,  $\$y_2\$$ ,  $\$y_4\$$  and  $\$x_2\$$ . Cut 1: Horizontal with cost  $\$c_{y_5} = 4\$$  across \$1\$ segment.  $\$TotalCost = 4 \times 2 = 4\$$ . Cut 2: Vertical with cost  $\$c_{x_1} = 4\$$  across \$2\$ segments.  $\$TotalCost = 4 \times 2 = 8\$$ . Cut 3: Horizontal with cost  $\$c_{y_3} = 3\$$  across \$2\$ segments.  $\$TotalCost = 3 \times 2 = 6\$$ . Cut 4: Horizontal with cost  $\$c_{y_1} = 2\$$  across \$2\$ segments.  $\$TotalCost = 2 \times 2 = 4\$$ . Cut 5: Vertical with cost  $\$c_{x_3} = 2\$$  across \$4\$ segments.  $\$TotalCost = 2 \times 4 = 8\$$ . Cut 6: Horizontal with cost  $\$c_{y_2} = 1\$$  across \$3\$ segments.  $\$TotalCost = 1 \times 3 = 3\$$ . Cut 7: Horizontal with cost  $\$c_{y_4} = 1\$$  across \$3\$ segments.  $\$TotalCost = 1 \times 3 = 3\$$ . Cut 8: Vertical with cost  $\$c_{x_3} = 1\$$  across \$6\$ segments.  $\$TotalCost = 1 \times 3 = 3\$$ .

When we sum the TotalCost for all minimum cuts, we get 4+8+6+4+8+3+3+6=42. We then print the value of  $42 \ (10^9 + 7)$ .