# Intro to ML Project 1 Report

#### Task-0

Environment: Windows 10

• Time Spent: 1 Week

• Programming Language: R

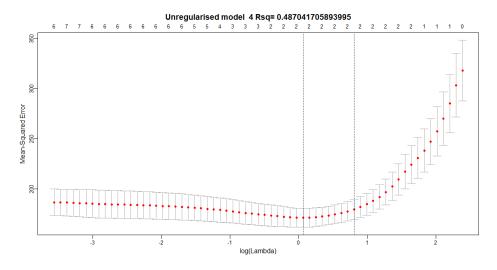
Libraries Used: Glmnet, caTools, ggplot2

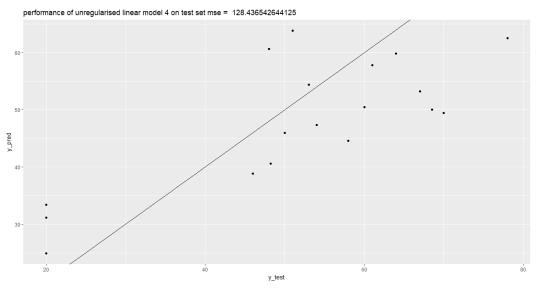
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### Task-1

#### Unregularized Regression

- The mean R-squared for 10 iterations is 0.517 with SD of 0.029 and the mean MSE is 209 with SD of 51.
- MSE of models 1 to 10 on test set:
   274.9655, 196.7950, 284.0492, 128.4365, 173.1720, 187.8367, 233.6112, 251.6670, 206.4925, 157.6003
- R-square values of models 1 to 10 on training set:
   0.5778609, 0.5271576, 0.5377060, 0.4870417, 0.4867348, 0.5039519, 0.5271875, 0.5341908, 0.5058729, 0.4850152
- Best Unregularised Model is model 4 as it has min MSE on the test set.





#### Regularized Regression: Ridge

- The mean R-squared for 10 iterations is 0.477 with SD of 0.048 and the mean MSE is 206 with SD of 50.
- MSE of models 1 to 10 on test set:

260.1241, 198.7340, 287.2600, <mark>126.9197</mark>, 172.0712, 183.9118, 221.1980, 257.4454, 202.4738, 153.1231

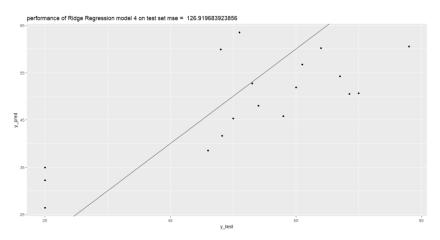
R-square values of models 1 to 10 on training set:

0.5464303, 0.4927091, 0.5184776, 0.4706722, 0.4545269, 0.4817757, 0.4720269, 0.5019988, 0.4785214, 0.362 7046

• Best regularized Ridge Model is model 4 as it has min MSE on the test set with regularization parameter 0.97.

# > cvfit\_lasso\$lambda.min [1] 0.9707253

• The performance of Ridge *regression* is better than Unregularised regression as evident by the lower average mean squared error of 206.



#### Regularized Regression: Lasso

- The mean R-squared for 10 iterations is 0.5 with SD of 0.031 and the mean MSE is 195 with SD of 47
- MSE of models 1 to 10 on test set:

244.3346, 195.0800, 271.7668, **129.3625**, 169.9484, 163.4074, 198.0553, 252.1878, 180.0836, 148.2110

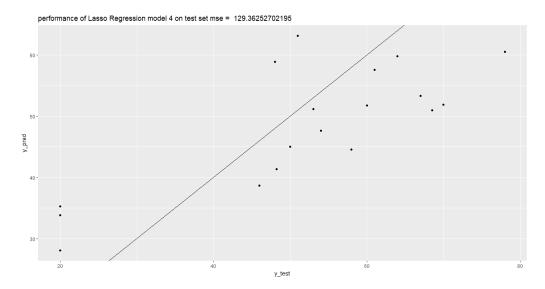
• R-square values of models 1 to 10 on training set:

0.5595370, 0.5164467, 0.5314832, 0.4755914, 0.4790928, 0.4860902, 0.5025553, 0.5208867, 0.4827065, 0.4555893

• Best regularized Lasso Model is model 4 as it has min MSE of 129 on the test set with regularization parameter 1.3.

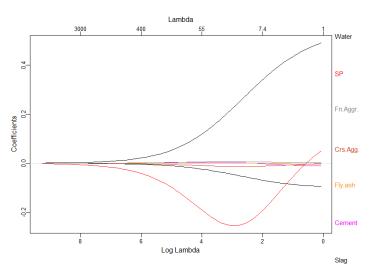
# > cvfit\_ridge\$Tambda.min [1] 1.313438

- The average performance of Lasso regression is better than Unregularised regression and Ridge Regression as evident by the lower average mean squared error of 195.
- Number of coefficients used by lasso are: 2, Slag and Water as evident below

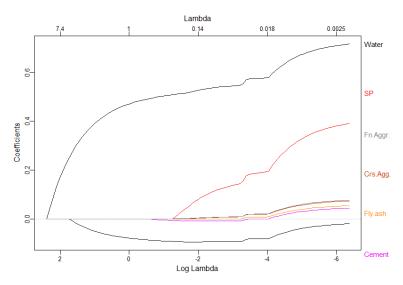


Task-2 Regularization Paths

# Ridge Model-4



### Lasso Model-4



# Extra Task

	X	X <sup>2</sup>	X <sup>3</sup>	Log X
mean.mse_unregularised	209.4626022	196.3988727	202.1088	214.6087
mean.mse_ridge	206.3261042	190.9561916	195.0809	208.3848
mean.mse_lasso	195.2437458	189.918766612805	191.7158	217.849
sd.mse_unregularised	51.01966845	28.59639913	34.42844	32.31776
sd.mse_ridge	50.73141443	31.72755623	30.38875	57.19006
sd.mse_lasso	47.08372171	28.46161358	28.48551	41.07474
mean.rsq_unregularised	0.517271919	0.56080336	0.543499	0.575996
mean.rsq_ridge	0.477984359	0.505799992	0.456478	0.470362
mean.rsq_lasso	0.500997907	0.538383639	0.521571	0.573876
sd.rsq_unregularised	0.029373273	0.017027908	0.020552	0.01809
sd.rsq_ridge	0.477984359	0.505799992	0.456478	0.470362
sd.rsq_lasso	0.500997907	0.538383639	0.521571	0.573876

### Analysis

- 1. Regularized Lasso model on an average gives minimum mean square error when X<sup>2</sup> is used as matrix of features instead of X.
- 2. The R-squared value of Unregularised model increases significantly when X<sup>2</sup> and Log X are used.
- 3. Standard Deviation in R-squared values in Unregularised regression is minimum in all cases.