
Natural Gradient Deep Q-learning

Ethan Knight*
ethan.h.knight@gmail.com
The Nueva School

Osher Lerner
osherler@gmail.com
The Nueva School

Abstract

This paper presents findings for training a Q-learning reinforcement learning model using natural gradient techniques. We compare the original deep Q-network (DQN) algorithm to its natural gradient counterpart (NGDQN). Measuring NGDQN and DQN performance both without target networks on classic controls environments, we find that NGDQN performs favorably to DQN, converging to significantly better policies faster and more frequently. These results indicate that natural gradient could be used in reinforcement learning applications to accelerate training and increase sample-efficiency.

1 Introduction

Natural gradient was originally proposed by Amari as a method to accelerate gradient descent 1998. Rather than exclusively using the loss gradient or including second-order (curvature) information, natural gradient uses the “information” found in the parameter space of the model.

Natural gradient has been successfully applied to several deep learning domains, specifically with supervised learning, and has been used more recently to accelerate the training of reinforcement learning systems. To motivate our approach, we hoped that using natural gradient would accelerate the training of a DQN, making our system more sample-efficient and thereby addressing one of the major problems in reinforcement learning. We also hoped that since natural gradient stabilizes training (e.g. natural gradient is relatively unchanged when changing the order of training inputs Pascanu and Bengio [2013]), a DQN trained with natural gradient could achieve good results without a target network and achieve more stable solutions in general.

In our experiments, we observed both effects. When training without a target network, NGDQN converged much faster and more frequently than our DQN baseline, and the solutions found by NGDQN tended to be stable (i.e. once NGDQN converged to a solution, it tended to remain stable).

This paper was inspired by the Requests for Research list published by OpenAI, which has listed the application of natural gradient techniques to Q-learning since June 2016 2016, 2018. This paper presents the first successful attempt to our knowledge: our method to accelerate the training of Q-networks using natural gradient.

2 Background

In reinforcement learning, an agent is trained to interact with an environment to maximize cumulative reward. Often, this environment is modeled as a Markov Decision Process, defined by a 5-tuple of states, actions, dynamics, rewards, and discount factor for the reward over time which defines the cumulative reward. The agent attempts to learn a policy π to maximize this reward. At a state s , an agent takes an action a to land at state s' , receiving a reward r .

*Contributor statement and acknowledgements near end of paper

2.1 Q-learning

Q-learning is a model-free reinforcement learning technique which works by gradually learning an action-value function called Q , originally proposed by Rummery and Niranjan, later used to play Atari games using deep learning by Mnih et al. 1994, 2013. For a state s , action a , and learning rate α , the function Q estimates the future reward, which is estimated using its current model’s best predicted outcome. Its update rule is given as follows:

$$Q_{k+1}(s, a) \leftarrow (1 - \alpha)Q_k(s, a) + \alpha \text{target} \quad (1)$$

If the agent has not yet reached the end of the task, given discount factor γ the target is defined as

$$\text{target} = \text{reward} + \gamma \max_{a'} Q_k(s', a') \quad (2)$$

At the final timestep, since there is no future reward, $\text{target} = \text{reward}$. In deep Q-learning, this mapping is learned by a neural network.

The policy π uses an ϵ -greedy policy where ϵ , the probability of the agent taking a random action (corresponding to exploration and exploitation), is gradually annealed over time.

A neural network can be described as a parametric function approximator that uses “layers” of units, each containing weights, biases and activation functions, called “neurons”. Each layer’s output is fed into the next layer, and the loss is backpropagated to each layer’s weights in order to adjust the parameters according to their effect on the loss.

For deep Q-learning, the neural network loss is defined as follows:

$$\mathcal{L}(\theta) = \mathbb{E} [(y - Q(s, a; \theta))^2] \quad (3)$$

where

$$y = \mathbb{E}_{s' \sim \epsilon} [r + \gamma \max_{a'} Q(s', a'; \theta) | s, a] \quad (4)$$

Notice that we take the mean-squared-error between the expected Q-value and actual Q-value. The neural network is optimized over the course of numerous iterations through some form of gradient descent. In the original DQN (deep Q-network) paper, an adaptive gradient method is used to train this network Mnih et al. [2013].

Initially the training agent acts nearly randomly in order to explore potentially successful strategies. As the agent learns, it acts randomly less (this is sometimes called the “exploit” stage, as opposed to the “explore” stage). Mathematically, the probability of choosing a random action ϵ is gradually linearly annealed over the course of training.

Deep Q-networks use experience replay to train the Q-value estimator on a randomly sampled batch of previous experiences (essentially replaying past remembered events back into the neural network) Lin [1993]. This serves to smooth the learning process.

We combine these two approaches, using natural gradient to optimize an arbitrary neural network in Q-learning architectures.

3 Natural gradient

Gradient descent optimizes parameters of a model with respect to a loss function by “descending” down the loss manifold. To do this, we take the gradient of the loss with respect to the parameters, then travel in the opposite direction of that gradient Goodfellow et al. [2016]. Mathematically, gradient descent proposes the point given a learning rate of α and parameters θ : $\theta - \alpha \nabla_{\theta} \mathcal{L}(x, y; \theta)$.

A commonly used variant of gradient descent is stochastic gradient descent (SGD). Instead of calculating the entire gradient at a time, SGD uses a mini-batch of training samples: $\theta - \alpha \nabla_{\theta} \mathcal{L}(x_i, y_i; \theta)$. Our baselines use Adam, an adaptive gradient optimizer, which is a modification of SGD Kingma and Ba [2014].

However, this approach of gradient descent has a number of issues. For one, gradient descent will often become very slow in “plateaus” where the magnitude of the gradient is close to zero. Also, while

gradient descent takes uniform steps in the parameter space, this does not necessarily correspond to uniform steps in the output distribution. Natural gradient attempts to fix these issues by incorporating the inverse Fisher information matrix, a concept from statistical learning theory Amari [1998].

Essentially, the core problem is that Euclidean distances in the parameter space do not give enough information about the distances between the corresponding outputs, as there is not a strong enough relationship between the two Foti [2013]. Kullback and Leibler define a more expressive distribution-wise measure, as follows 1951.

$$KL(P|Q) = \int_{-\infty}^{\infty} p(x) \log \frac{p(x)}{q(x)} dx \quad (5)$$

However, since $KL(P|Q) \neq KL(Q|P)$, we define symmetric KL divergence, also known as Jensen-Shannon (JS) divergence, as follows Foti [2013]:

$$KL(P|Q) := \frac{1}{2} (KL(P|Q) + KL(Q|P)) \quad (6)$$

To perform gradient descent on the manifold of functions given by our model, we use the Fisher information metric on a Riemannian manifold. Since symmetric KL divergence behaves like a distance measure in infinitesimal form, a Riemannian metric is derived as the Hessian of the divergence of symmetric KL divergence Pascanu and Bengio [2013]. We give Pascanu and Bengio’s definition: given some probability density function p , input vector z , and parameters θ 2013:

$$\mathbf{F}_\theta = \mathbb{E}[(\nabla \log p_\theta(z))^T (\nabla \log p_\theta(z))] \quad (7)$$

Finally, to achieve uniform steps on the output distribution, we use Pascanu and Bengio’s derivation of natural gradient given a loss function \mathcal{L} 2013:

$$\nabla \mathcal{L}_N = \nabla \mathcal{L} \mathbf{F}_\theta^{-1} \quad (8)$$

Taking the second-order Taylor expansion Pascanu and Bengio [2013] gets:

$$KL(p_\theta|p_{\theta+\Delta\theta}) \approx \frac{1}{2} \Delta\theta^T \mathbf{F}_\theta \Delta\theta \quad (9)$$

Using this approximation and solving the Lagrange multiplier for minimizing the loss of parameters updated by $\Delta\theta$ (approximated by a first order Taylor series) under a the constraint of a constant symmetric KL distance, one can derive the following equations for the information matrices.

As the output probability distribution is dependent on the final layer activation, Pascanu and Bengio [2013] give the following derivation for a layer with a linear activation (interpreted as a conditional Gaussian distribution), as follows:

$$p_\theta(t|x) = \prod_{i=1}^o \mathcal{N}(t_i|y(x, \theta)_i, \beta^2) \quad (10)$$

Thus, the Fisher information can be derived where \mathbf{J}_y corresponds to the Jacobian of the output vector y and β to the standard deviation as in Pascanu and Bengio [2013]:

$$\mathbf{F}_{\text{linear}} = \beta^2 \mathbb{E}_{X \sim \tilde{q}} [\mathbf{J}_y^T \mathbf{J}_y] \quad (11)$$

4 Related work

We borrow heavily from Pascanu and Bengio’s approach, using their natural gradient for deep neural networks formalization and implementation in our method 2013.

Next, we look at work on a different method of natural gradient descent by Desjardins et al. [2015]. In this paper, we propose an algorithm called “Projected Natural Gradient Descent” (PRONG), which also considers the Fisher information matrix in its derivation. While our paper does not explore this approach, it could be an area of future research, as PRONG is shown to converge better on multiple data-sets, such as CIFAR-10 Desjardins et al. [2015].

Additional methods of applying natural gradient to reinforcement learning using reinforcement learning algorithms such as policy gradient and actor-critic are explored in Kakade [2001] and Peters et al. [2005]. In both works, the natural variants of their respective algorithms are shown to perform favorably compared to their non-natural counterparts. Details on theory, implementation, and results are in their respective papers.

Insights into the mathematics of optimization using natural conjugate gradient techniques are provided in the work of Honkela et al. [2015]. These methods allow for more efficient optimization in high dimensions and nonlinear contexts.

The Natural Temporal Difference Learning algorithm applies natural gradient to reinforcement learning systems based on the Bellman error, although Q-learning is not explored Tesauro [1995]. The authors use natural gradient with residual gradient, which minimizes the MSE of the Bellman error and apply natural gradient to SARSA. Empirical experiments show that natural gradient again outperforms standard methods in all tested environments.

Finally, to our knowledge, the only one other published or publicly available version of natural Q-learning was created by Barron et al. 2016. In this work, the authors re-implemented PRONG and verified its effectiveness at MNIST. However, when the authors attempted to apply it to Q-learning they got negative results, with no change on CartPole and worse results on GridWorld.

5 Methods

In our experiments, we use a standard method of Q-learning to act on the environment. Lasagne Dieleman et al. [2015], Theano Theano Development Team [2016], and AgentNet Yandex [2016] complete the brunt of the computational work. Because our implementation of natural gradient modified from Pascanu and Bengio 2013 fits an X to a mapping y , rather than directly back-propagating a loss the model uses a target value change similar to that described in (10). We also decay the learning rate by multiplying it by a constant factor every iteration.

As the output layer of our Q-network has a linear activation function, we use the parameterization of the Fisher information matrix for linear activations, which determines the natural gradient. For this, we refer to equation 11.

The MinRes-QLP Krylov Subspace Descent Algorithm Choi et al. [2011] solves the change in parameters, as in Pascanu and Bengio [2013]. Our implementation runs on the OpenAI Gym platform which provides several classic control environments, such as the ones shown here, as well as other environments such as Atari Brockman et al. [2016]. The current algorithm takes a continuous space and maps it to a discrete set of actions.

In Algorithm 1, we adapt Mnih et al.’s Algorithm 1 and Pascanu and Bengio’s Algorithm 2 2013, 2013. Because these environments do not require preprocessing, we have omitted the preprocessing step, however this can easily be re-added. In our experiments, Δ_α was chosen somewhat arbitrarily to be $1 - 7e^{-5}$, and α was selected according to our grid-search (see: Hyperparameters).

6 Experiments

6.1 Overview

To run Q-learning models on OpenAI gym, we adapt Pascanu and Bengio’s implementation 2013. For the baseline, we use OpenAI’s open-source Baselines library Dhariwal et al. [2017], which allows reliable testing of tuned reinforcement learning architectures. As is defined in Gym, performance is measured by taking the best 100-episode reward over the course of running.

We run a grid search on the parameter spaces specified in the Hyperparameters section, measuring performance for all possible combinations. Because certain parameters like the exploration fraction are not used in our implementation of NGDQN, we grid search those parameters as well. As we wish to compare “vanilla” NGDQN to “vanilla” DQN, we do not use target nets, model saving, or any other features, such as prioritized experience replay.²

² The DQN performance shown may be worse than DQN performance one might find when comparing to other implementations. The discrepancy is that DQN is often used with target networks, whereas in this case,

Algorithm 1 Natural Gradient Deep Q-Learning with Experience Replay

Require: Initial learning Rate α_0
Require: Learning rate decay $\Delta\alpha$
Require: Function `update_damping`
Initialize replay memory \mathcal{D} to capacity N
Initialize action-value function Q with random weights
 $\alpha \leftarrow \alpha_0$
for $episode = 1, M$ **do**
 Initialize sequence with initial state s_1
 for $t = 1, T$ **do**
 With probability ϵ select a random action a_t , otherwise select action $a_t = \max_a Q^*(s_t, a; \theta)$
 Execute action a_t in emulator and observe reward r_t and state s_{t+1}
 Store transition (s_t, a_t, r_t, s_{t+1}) in memory \mathcal{D}
 Sample random minibatch of n transitions (s_j, a_j, r_j, s_{j+1}) from \mathcal{D}
 $y_j \leftarrow \begin{cases} r_j & \text{for terminal } s_{j+1} \\ r_j + \gamma \max_{a'} Q(s_{j+1}, a'; \theta) & \text{for non-terminal } s_{j+1} \end{cases}$
 $g \leftarrow \frac{\partial \mathcal{L}}{\partial \theta}$
 $d \leftarrow \text{update_damping}(d)$
 $g_{\text{norm}} \leftarrow \sqrt{\sum \frac{\partial \mathcal{L}}{\partial \theta}^2}$
 Define G such that $G(v) = (\frac{1}{n} \mathbf{J}_Q v) \mathbf{J}_Q$
 Solve $\arg\min_x \|(G + d\mathbf{I})x - \frac{\partial \mathcal{L}}{\partial \theta}\|$ with
 MinresQLP Choi et al. [2011]
 $g_{\text{natural}} \leftarrow g_{\text{norm}} x$
 $\theta \leftarrow \theta - \alpha g_{\text{natural}}$
 $\alpha \leftarrow \Delta_\alpha \alpha$
 end for
end for

Following this grid search, we take the best result performance for each environment from both DQN and NGDQN, and run this configuration 10 times, recording a moving 100-episode average and the best 100-episode average over the course of a number of runs.

These experiments reveal that natural gradient compares favorably to standard adaptive gradient techniques. However, the increase in stability and speed comes with a trade-off: due to the additional computation, natural gradient takes longer to train when compared to adaptive methods, such as the Adam optimizer Kingma and Ba [2014]. Details of this can be found in Pascanu and Bengio’s work 2013.

Below, we describe the environments, summarizing data taken from <https://github.com/openai/gym> and information provided on the wiki: <https://github.com/openai/gym/wiki>.

6.2 CartPole-v0

The classic control task CartPole involves balancing a pole on a controllable sliding cart on a frictionless rail for 200 timesteps. The agent “solves” the environment when the average reward over 100 episodes is equal to or greater than 195. However, for the sake of consistency, we measure performance by taking the best 100-episode average reward.

The agent is assigned a reward for each timestep where the pole angle is less than ± 12 deg, and the cart position is less than ± 2.4 units off the center. The agent is given a continuous 4-dimensional space describing the environment, and can respond by returning one of two values, pushing the cart either right or left.

we do not use target nets for either NGDQN or DQN. The reason for this is that we want to compare NGDQN to DQN on the original DQN algorithm presented in Algorithm 1 of Mnih et al. 2013. We plan to expand our analysis to include target networks in future work.

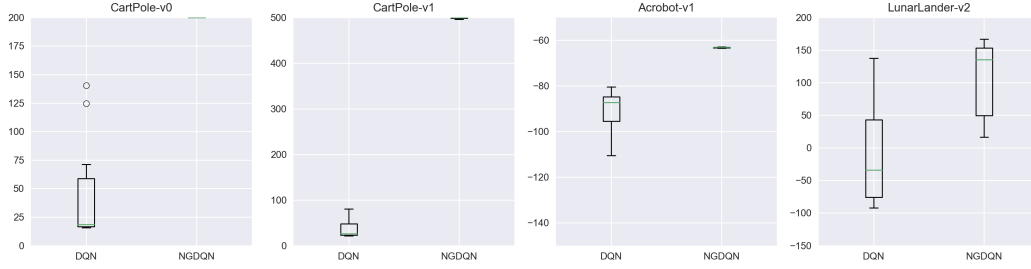


Figure 1: Average best 100-episode run over 10 trials with IQR²

6.3 CartPole-v1

CartPole-v1 is a more challenging environment which requires the agent to balance a pole on a cart for 500 timesteps rather than 200. The agent solves the environment when it gets an average reward of 450 or more over the course of 100 timesteps. However, again for the sake of consistency, we again measure performance by taking the best 100-episode average reward. This environment essentially behaves identically to CartPole-v0, except that the cart can balance for 500 timesteps instead of 200.

6.4 Acrobot-v1

In the Acrobot environment, the agent is given rewards for swinging a double-jointed pendulum up from a stationary position. The agent can actuate the second joint by returning one of three actions, corresponding to left, right, or no torque. The agent is given a six dimensional vector describing the environments angles and velocities. The episode ends when the end of the second pole is more than the length of a pole above the base. For each timestep that the agent does not reach this state, it is given a -1 reward.

6.5 LunarLander-v2

Finally, in the LunarLander environment, the agent attempts to land a lander on at a particular location on a simulated 2D world. If the lander hits the ground going too fast, the lander will explode, or if the lander runs out of fuel, the lander will plummet toward the surface. The agent is given a continuous vector describing the state, and can turn its engine on or off. The landing pad is placed in the center of the screen, and if the lander lands on the pad, it is given reward. The agent also receives a variable amount of reward when coming to rest, or contacting the ground with a leg. The agent loses a small amount of reward by firing the engine, and loses a large amount of reward if it crashes. Although this environment also defines a solve point, we use the same metric as above to measure performance.

7 Results

NGDQN and DQN were run against these four experiments, to achieve the following results summarized in Figure 1. The hyperparameters can be found in the the Hyperparameters section.

The code for this project can be found at <https://github.com/hyperdo/natural-gradient-deep-q-learning>. It currently includes the baselines, and we plan to post the NGDQN code as well very soon. It uses a fork of OpenAI Baselines to allow for different activation functions: <https://github.com/hyperdo/baselines>. Each environment was run for a number of episodes (see Hyperparameters), and as per Gym standards, the best 100 episode performance was taken.

In all experiments, natural gradient converges faster and significantly more consistently than the DQN benchmark, indicating its robustness in this task compared to the standard adaptive gradient optimizer used in the Baseline library (Adam). The success across all tests indicates that natural

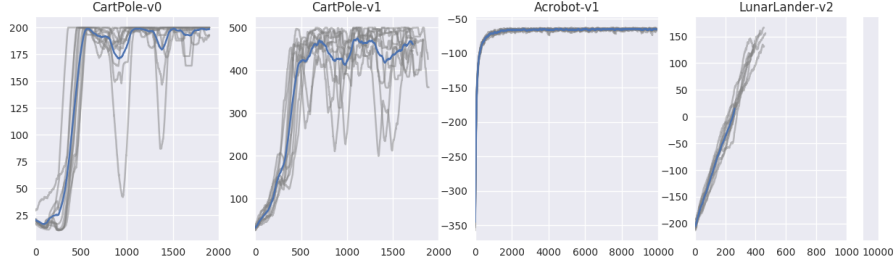


Figure 2: NGDQN performance over 10 trials with average line³

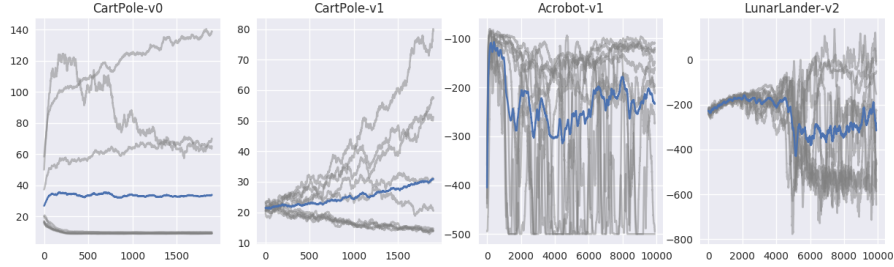


Figure 3: DQN performance over 10 trials with average line

gradient generalizes well to diverse control tasks, from simpler tasks like CartPole, to more complex tasks like LunarLander.³

8 Conclusions

In this paper, natural gradient methods are shown to accelerate and stabilize training for common control tasks. This could indicate that Q-learning’s instability may be diminished by naturally optimizing it, and also that natural gradient could be applied to other areas of reinforcement learning.

Contributions & Acknowledgements

Here, a brief contributor statement is provided, as recommended by Sculley et al. 2018.

Primary author led the research and wrote the first draft of the paper, as well as all the code for this project. Additionally, experiments were run by primary author on Sherlock. Secondary author verified all of the code for correctness and was instrumental in editing the paper. Secondary author was also important in the derivation and understanding of KL divergence and the natural gradient, and in his reaching out to fellow academics.

Thanks to Jen Selby for providing valuable insight and support, and for reviewing the paper and offering her suggestions over the course of the writing process. Also, thanks to Leonard Pon for his instruction, advice, and generous encouragement, especially during Applied Math, where the first part of this project took place.

References

Shun-Ichi Amari. Natural gradient works efficiently in learning. *Neural computation*, 10(2):251–276, 1998.

³The LunarLander-v2 task for NGDQN was not completed, as the Sherlock cluster where the environments were run does not permit GPU tasks for over 48 hours. Therefore, each of the 10 trials was run for 48 hours, and then was stopped.

- Alex Barron, Todor Markov, and Zack Swafford. Deep q-learning with natural gradients, Dec 2016. URL <https://github.com/todor-markov/natural-q-learning/blob/master/writeup.pdf>.
- Greg Brockman, Vicki Cheung, Ludwig Pettersson, Jonas Schneider, John Schulman, Jie Tang, and Wojciech Zaremba. Openai gym. *CoRR*, abs/1606.01540, 2016. URL <http://arxiv.org/abs/1606.01540>.
- Sou-Cheng T. Choi, Christopher C. Paige, and Michael A. Saunders. MINRES-QLP: A krylov subspace method for indefinite or singular symmetric systems. *SIAM Journal on Scientific Computing*, 33(4):1810–1836, 2011. doi: 10.1137/100787921. URL <http://web.stanford.edu/group/SOL/software/minresqlp/MINRESQLP-SISC-2011.pdf>.
- Guillaume Desjardins, Karen Simonyan, Razvan Pascanu, and Koray Kavukcuoglu. Natural neural networks. In C. Cortes, N. D. Lawrence, D. D. Lee, M. Sugiyama, and R. Garnett, editors, *Advances in Neural Information Processing Systems 28*, pages 2071–2079. Curran Associates, Inc., 2015. URL <http://papers.nips.cc/paper/5953-natural-neural-networks.pdf>.
- Prafulla Dhariwal, Christopher Hesse, Oleg Klimov, Alex Nichol, Matthias Plappert, Alec Radford, John Schulman, Szymon Sidor, and Yuhuai Wu. Openai baselines. <https://github.com/openai/baselines>, 2017.
- Sander Dieleman, Jan Schlüter, Colin Raffel, Eben Olson, Søren Kaae Sønderby, Daniel Nouri, Daniel Maturana, Martin Thoma, Eric Battenberg, Jack Kelly, Jeffrey De Fauw, Michael Heilman, Diogo Moitinho de Almeida, Brian McFee, Hendrik Weideman, Gábor Takács, Peter de Rivaz, Jon Crall, Gregory Sanders, Kashif Rasul, Cong Liu, Geoffrey French, and Jonas Degraeve. Lasagne: First release, August 2015. URL <http://dx.doi.org/10.5281/zenodo.27878>.
- Nick Foti. The natural gradient, Jan 2013. URL <https://hips.seas.harvard.edu/blog/2013/01/25/the-natural-gradient/>.
- Ian Goodfellow, Yoshua Bengio, and Aaron Courville. *Deep Learning*. MIT Press, 2016. <http://www.deeplearningbook.org>.
- Antti Honkela, Matti Tornio, Tapani Raiko, and Juha Karhunen. Natural conjugate gradient in variational inference. 2015. URL <https://www.hiit.fi/u/ahonkela/papers/Honkela07ICONIP.pdf>.
- Sham Kakade. A natural policy gradient. In Thomas G. Dietterich, Suzanna Becker, and Zoubin Ghahramani, editors, *Advances in Neural Information Processing Systems 14 (NIPS 2001)*, pages 1531–1538. MIT Press, 2001. URL <http://books.nips.cc/papers/files/nips14/CN11.pdf>.
- Diederik P. Kingma and Jimmy Ba. Adam: A method for stochastic optimization. *CoRR*, abs/1412.6980, 2014. URL <http://arxiv.org/abs/1412.6980>.
- S. Kullback and R. A. Leibler. On information and sufficiency. *Ann. Math. Statist.*, 22(1):79–86, 03 1951. doi: 10.1214/aoms/1177729694. URL <http://dx.doi.org/10.1214/aoms/1177729694>.
- Long-Ji Lin. Reinforcement learning for robots using neural networks. 01 1993.
- Volodymyr Mnih, Koray Kavukcuoglu, David Silver, Alex Graves, Ioannis Antonoglou, Daan Wierstra, and Martin A. Riedmiller. Playing atari with deep reinforcement learning. *CoRR*, abs/1312.5602, 2013. URL <http://arxiv.org/abs/1312.5602>.
- OpenAI. Requests for research: Initial commit, 2016. URL <https://github.com/openai/requests-for-research/commit/03c3d42764dc00a95bb9fab03af08dedb4e5c547>.
- OpenAI. Requests for research, 2018. URL <https://openai.com/requests-for-research/#natural-q-learning>.
- Razvan Pascanu and Yoshua Bengio. Natural gradient revisited. *CoRR*, abs/1301.3584, 2013. URL <http://arxiv.org/abs/1301.3584>.

Jan Peters, Sethu Vijayakumar, and Stefan Schaal. *Natural Actor-Critic*, pages 280–291. Springer Berlin Heidelberg, Berlin, Heidelberg, 2005. ISBN 978-3-540-31692-3. doi: 10.1007/11564096_29. URL https://doi.org/10.1007/11564096_29.

G. A. Rummery and M. Niranjan. On-line q-learning using connectionist systems. Technical report, 1994.

D. Sculley, Jasper Snoek, Alex Wiltschko, and Ali Rahimi. Winner’s curse? on pace, progress, and empirical rigor. *ICLR 2018 (under review)*, Feb 2018. URL <https://openreview.net/forum?id=rJWFOFywF>.

Gerald Tesauro. Temporal difference learning and td-gammon. *Commun. ACM*, 38(3):58–68, March 1995. ISSN 0001-0782. doi: 10.1145/203330.203343. URL <http://doi.acm.org/10.1145/203330.203343>.

Theano Development Team. Theano: A Python framework for fast computation of mathematical expressions. *arXiv e-prints*, abs/1605.02688, May 2016. URL <http://arxiv.org/abs/1605.02688>.

Yandex. Agentnet, 2016. URL <https://github.com/yandexdataschool/AgentNet>.

Appendix A: Hyperparameters

Both NGDQN and DQN had a minimum epsilon of 0.02 and had a γ of 1.0 (both default for Baselines). The NGDQN model was tested using an initial learning rate of 1.0. For NGDQN, the epsilon decay was set to 0.995, but since there wasn’t an equivalent value for the Baselines library, the grid search for Baselines included an exploration fraction (defined as the fraction of entire training period over which the exploration rate is annealed) of either 0.01, 0.1, or 0.5. Likewise, to give baselines the best chance of beating NGDQN, we also searched a wide range of learning rates, given below.

Environment	# of Episodes Ran For	Layer Configuration
CartPole-v0	2000	[64]
CartPole-v1	2000	[64]
Acrobot-v1	10,000	[64, 64]
LunarLander-v2	10,000	[256, 128]

Best grid searched configuration used in both the DQN and NGDQN experiments:

Environment	Natural Gradient DQN (NGDQN)					Baseline DQN				
	Learning Rate	Adapt Damping	Batch Size	Memory Length	Activation	Learning Rate	Exploration fraction	Batch Size	Memory Length	Activation
CartPole-v0	0.01	No	128	50,000	Tanh	1e-07	0.01	128	2500	Tanh
CartPole-v1	0.01	Yes	128	50,000	Tanh	1e-08	0.1	32	50,000	Tanh
Acrobot-v1	1.0	No	128	50,000	Tanh	1e-05	0.01	128	50,000	ReLU
LunarLander-v2	0.01	No	128	50,000	ReLU	1e-05	0.01	128	2500	Tanh

NGDQN hyperparameter search space (total # of combos: 48):

Hyperparameter	Search Space
Learning Rate	[0.01, 1.0]
Adapt Damping	[Yes, No]
Batch Size	[32, 128]
Memory Length	[500, 2500, 50000]
Activation	[Tanh, ReLU]

DQN hyperparameter search space (total # of combos: 360):

Hyperparameter	Search Space
Learning Rate	[1e-08, 1e-07, 1e-06, 5e-06, 1e-05, 5e-05, 0.0001, 0.0005, 0.005, 0.05]
Exploration Fraction	[0.01, 0.1, 0.5]
Batch Size	[32, 128]
Memory Length	[500, 2500, 50000]
Activation	[Tanh, ReLU]