

# Naive Bayes

# Introduction

- ▶ **Naive Bayes** is a Conditional Probability Based Algorithm
- ▶ The features provided to us are independent and do not affect each other
- ▶ Naive Bayes is a classification algorithm suitable for binary & multiclass classification.
- ▶ The calculation of the likelihood of different class values involves multiplying a lot of numbers together.
- ▶ When new data comes, the algorithm updates the probabilities of the model. This can be helpful if the data changes frequently
- ▶ The assumption taken for numerical variables is Normal Distribution

# Features of Naive Bayes

- ▶ It's a classification algorithm
- ▶ Purely based on Conditional Probability
- ▶ Quick calculation time
- ▶ Gives Probabilistic Outputs
- ▶ It requires lesser data compared to other algorithms

# How Naive Bayes Works

Bayes' theorem is stated mathematically as the following equation:

Conditional Probability: Bayes' Theorem

$$P(A|B) = \frac{P(B|A) P(A)}{P(B)}$$

- Basically, we are trying to find probability of event A, given the event B is true. Event B is also termed as **evidence**.
- $P(A)$  is the **priori** of A (the prior probability, i.e. Probability of event before evidence is seen). The evidence is an attribute value of an unknown instance(here, it is event B).
- $P(A|B)$  is a posteriori probability , i.e. probability of event after evidence is seen.

# Bayes Equation Derivation

1  $\rightarrow P(A/B) = P(A \cap B) / P(B)$

2  $\rightarrow P(B/A) = P(B \cap A) / P(A)$

1 can be written as  $\rightarrow P(A \cap B) = P(A/B) * P(B) \rightarrow 3$

2 can be written as  $\rightarrow P(B \cap A) = P(B/A) * P(A) \rightarrow 4$

**Equating 3 and 4**

$$P(A/B) * P(B) = P(B/A) * P(A)$$

Hence,

$$P(A/B) = (P(B/A) * P(A)) / P(B)$$

$P(A/B) \rightarrow$  Posterior Probability

$P(B/A) \rightarrow$  Likelihood Probability

$P(A) \rightarrow$  Class Prior Probability

$P(B) \rightarrow$  Predictor's Prior Probability

# How Naive Bayes Works

Play	Counts	Probability	
Yes	9	$2/3$	0.642857
No	5	$1/3$	0.357143
Total	14	100%	100%

Outlook	YES	NO	P(YES)	P(NO)
Sunny	2	3	$2/9$	$3/5$
Overcast	4	0	$4/9$	0
Rainy	3	2	$1/3$	$2/5$
Total	9	5	100%	100%

Temperature	YES	NO	P(YES)	P(NO)
Hot	2	2	$2/9$	$2/5$
Mild	4	2	$4/9$	$2/5$
Cool	3	1	$1/3$	$1/5$
Total	9	5	100%	100%

Humidity	YES	NO	P(YES)	P(NO)
High	3	4	$1/3$	$4/5$
Normal	6	1	$2/3$	$1/5$
Total	9	5	100%	100%

Wind	YES	NO	P(YES)	P(NO)
FALSE	6	2	$2/3$	$2/5$
TRUE	3	3	$1/3$	$3/5$
Total	9	5	100%	100%

# Model Evaluation Metrics

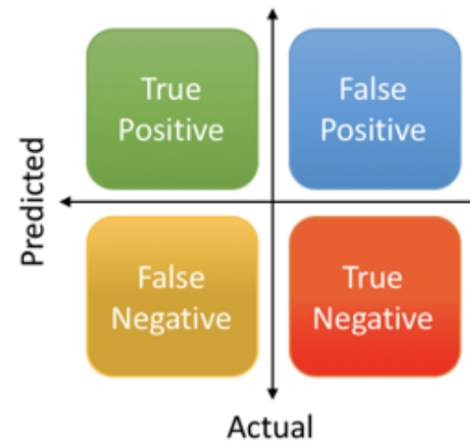
The various metrics used to evaluate the results of the prediction are :

- 1.Accuracy
- 2.Precision
- 3.Recall
- 4.Area Under ROC Curve

$$\text{Precision} = \frac{\text{True Positive}}{\text{Actual Results}} \quad \text{or} \quad \frac{\text{True Positive}}{\text{True Positive} + \text{False Positive}}$$

$$\text{Recall} = \frac{\text{True Positive}}{\text{Predicted Results}} \quad \text{or} \quad \frac{\text{True Positive}}{\text{True Positive} + \text{False Negative}}$$

$$\text{Accuracy} = \frac{\text{True Positive} + \text{True Negative}}{\text{Total}}$$



# Naive Bayes-Cons

- The main limitation of Naive Bayes is the assumption of independent predictor features.
- If there is a new category in test dataset compared to Training, it assigns a probability of ZERO
- Data Scarcity leads to an issue
- Since continuous features are involved, the algorithm does binning on top of it so loss of information exists
- The assumption of Independent Variables does not practically exists