

Solution 2.3

June 21, 2017

We need to show that variance of the sum of random variables = sum of the variance of random variables + the covariave of the random variables.

$$\begin{aligned}\text{var}[X+Y] &= E[(X+Y - \mu_x - \mu_y)^2] \\ &= E[((X - \mu_x) + (Y - \mu_y))^2] \\ &= E[(X - \mu_x) + (Y - \mu_y) + 2(X - \mu_x)(Y - \mu_y)] \\ &= \text{var}[X] + \text{var}[Y] + 2\text{cov}[X, Y]\end{aligned}$$