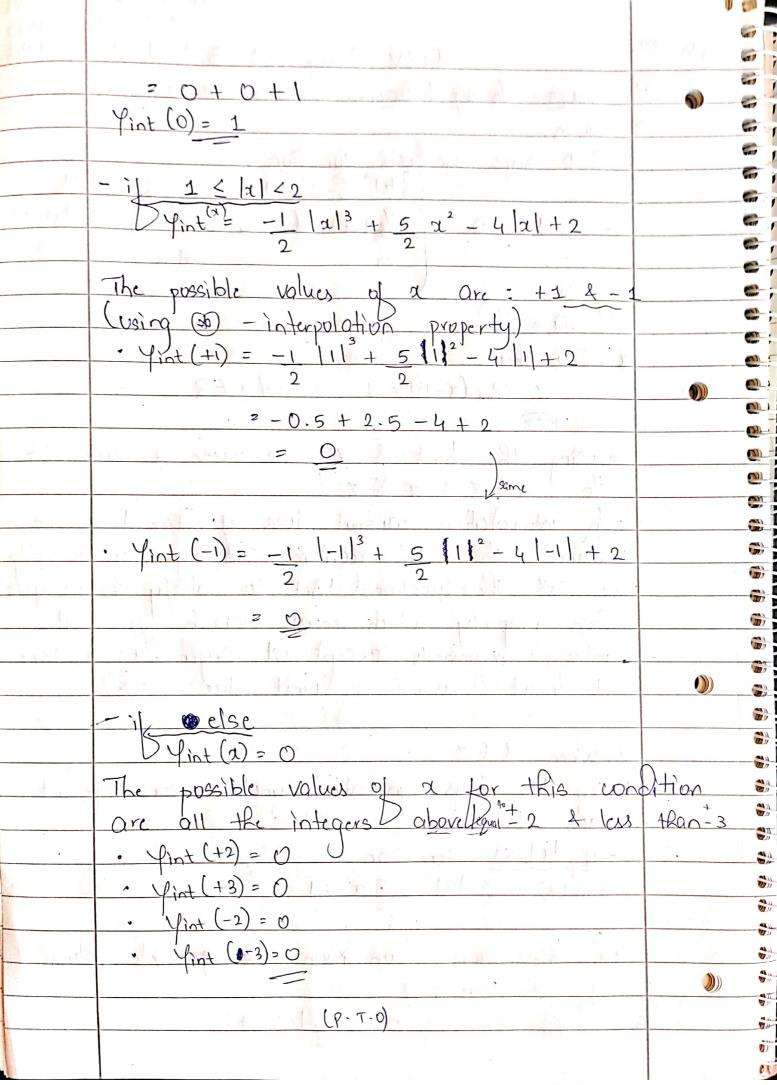
Anika Fuchs: 2580781 Ankit Agrowal: 2581532 IPCV Assignment 5 Akstay Joshi: 2581346 11/06/20 Keys Interpolation: Given, |w| (a = -1/2)6) To Show; Yack) = 1 Yack > using the hint & try to make a case distinction bly atzez & z & z · In interpolation without loss of generality we assume that the regular sampling step is unity
we ask the function I fint to satisfy the interpola
- from property which must vanish for all
integer arguments except at Origin (Set z). Here it Umust Value a unit value - @ 0 1 When I EZ Using the Kuys synthesis function for different values of α .

Values of α . $-illa|\alpha| = 3 |\alpha|^3 - 5 |\alpha|^2 + 1$ 2for the above condition the possible values $\frac{1}{1.6} = \frac{1}{2} = \frac{$

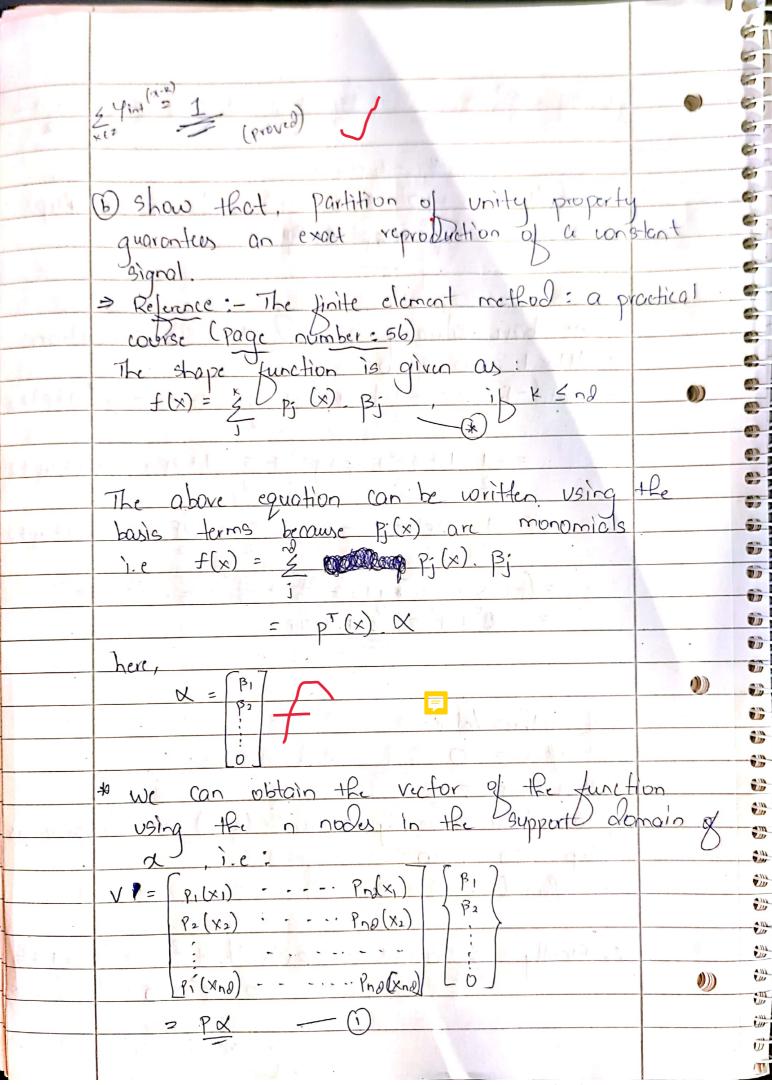


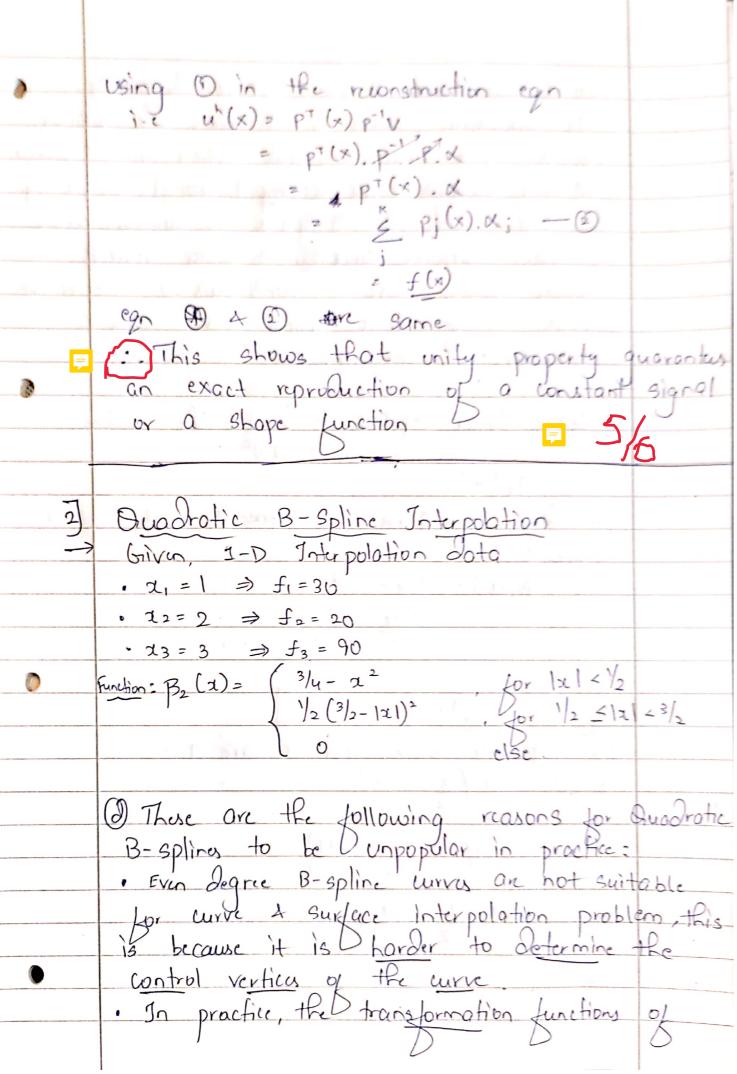
: & Yin (x-k) = 1+ 0+0+0+0+0+0 = 1 (42 ER) (II) when 2 & Z since a down't belong to z, the evolution positions of the Keys function cannot be computed as the privious case.

Let a be the center of the function, now to the distance of a too the next Integer Cacross either directions, let us assume a i.e K-a=p (assumption) Repeating the same stys as In case i $-i \int |x| < 1$ $y = 3/2 |x|^3 - 5 x^2 + 1$ $\sqrt{|\chi(3)|} = \frac{3}{3} |3 - \chi - \chi|^3 - \frac{5}{2} (3 - \chi - \chi)^2 + 1$ $= \frac{3}{3} + 3 - p)^3 - \frac{5}{3} (3 - p)^2 + 1$ $=\frac{3}{1}|P-3|^3+\frac{5}{5}(P+3)^2+1$ = $3(p^3 + -3p^2(3) + 3p(3)^2 - (3)^2) + 5(p^2 + 9 + 6p) + 1$ (P.T.0)

		6
	• $fint(1-k)^2 = \frac{3}{2} \left(1-k-\alpha\right)^3 + \frac{5}{2} \left(1-k-\alpha\right)^2 + 1$	0
	$= \frac{3}{2} 1-P ^3 - \frac{5}{2} (1-P)^2 + 1$	6)
4	$= 3(+1+3p^{2}-3p+1)-5(1-2p+p^{2})+1$	6) - 6) 6)
21 1	$\frac{2}{2} \frac{3+9p^2-9p+1}{2} \frac{-5+10p-5p^2+1}{2}$	6) 6)
1.91	$= \left(\frac{3-5+9p^2-5p^2-9p+10p+1}{2 2}\right)$	6) 6) 6)
3.73	$\frac{2}{2} - \chi + \frac{\mu^2 p^2}{2} + \frac{p}{2} + \chi$	0
	$= 2 p^2 + P_2$	6)
	· fint (0-(K-x))= 3 0-K-x 3- 5 (0-K-x)2+1	(i) (ii) (iii)
	$\frac{2}{2 \cdot 3 \cdot -P ^3 - 5 \cdot (-P)^2 + 1}$	(i)
	$= .3p^{3} + 5p^{2} + 1$	1)) 65
	2 - 12	
	$\frac{-i}{\Rightarrow y_{int}(x) = -1/2 x ^3 + 5/2^2 - 4 x + 2}$	975 975 4110 1010
_ 11A	$fint (2-(k-x)) = -1 2-p ^3 + \frac{5}{2} (2-p)^2 - 4(2-2)$	1
	$= -\frac{1(8+6p^2-12p^2-p^3)+5(4-4p^2-12p^2-p^3)}{2}$	+ ρ ²) 4 - in
	4(2-p)+2	017 077

9	
3	
3	$\frac{1}{2} - \frac{3}{4} + \frac{15}{2} + \frac{15}{2} + \frac{15}{2} + \frac{10}{2} - \frac{10}{200} + \frac{50^2}{2} - \frac{10}{2}$
3	7 2 2 2 2
3	
	08-4P+2
	$= (-4 - 8 + 2 + 10) + p_{2}^{3} - 3p^{2} + 5p^{2} + (6p - 10p) + 4p)$
	3 - 2
3	D + P3 Tagp2
3	
Jan day	and the state of the state of the state of
3	+ we have already covered (1-P) in condition
3	
3	tal<1, 50 now
3	-4 + 5 + 5 + 5 + 5 + 5 + 5 + 2
3	2 2
3	2), [[1,0,2,-2], [1,0,2]
3	$= -1\left(1+3p^2+3p+p^3\right)+5\left(1+2p+p^2\right)+4+4p+2$
9	a later and a late
	$\begin{array}{cccccccccccccccccccccccccccccccccccc$
	2 2 2 2 2 2
3	$ = (-0.5 + 2.5 + 4 + 2 - \frac{3p^{2}}{2} + \frac{5p^{2}}{2} - \frac{p^{3}}{2} - \frac{3p}{2} + 5p) $ $ = (-0.5 + 2.5 + 4 + 2 - \frac{3p^{2}}{2} + \frac{5p^{2}}{2} - \frac{p^{3}}{2} - \frac{3p}{2} + 5p) $ $ = (-0.5 + 2.5 + 4 + 2 - \frac{3p^{2}}{2} + \frac{5p^{2}}{2} - \frac{p^{3}}{2} - \frac{3p}{2} + 5p) $
3	2(-0.5+2.5 + 4+2 - 5 + 5 - 5 - 2 + 31)
3	2 P + P - 1 /2 + 3.5 P
3	
3	
3 9	
3	- ik others /clsc
3	- if others/clsc Yint = 0
	10.1(2-0) = 0
3	· yint (3-p) = 0 * we have already covered (2-p) in the previous
-	+ we have already would (2-1) ire provious
3	stup, 50 now:
3	, fint (-2-p) = 0
3	
3	:. Finally, $\leq \frac{1}{2} \int_{-0.5}^{1} p^2 + \frac{3p^3}{2} + \frac{5p^2}{2} + \frac{1}{2} + \frac{p^3}{2} + \frac{5p^3}{2} + \frac{5p^3}{2} + \frac{1}{2} + \frac{p^3}{2} + \frac{1}{2} + \frac{1}{2} + \frac{p^3}{2} + \frac{1}{2} + \frac{1}{$
3	, Finally, & Jint (2 1) - 21 + 12 2 2 1 23 - p3/12
3	
3	$= (2p^{2} + 2.5p^{2} - 0.5p^{2} - 2p^{12} + \frac{3p^{2}}{2} - \frac{p^{3}}{2} + \frac{p^{3}}{2}$
3	= (2P+2.5p-0.5p-2Y+ 12-12+P+p3
	+ 1





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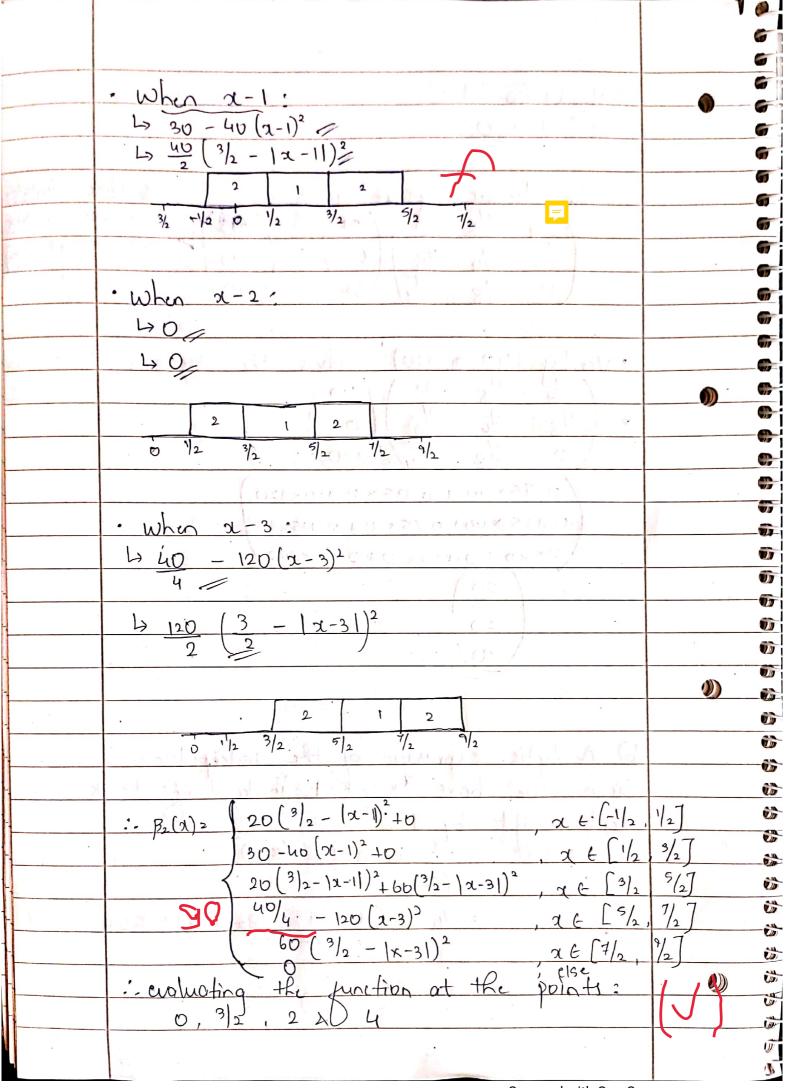
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3

	even 2022 Degree B-splines before differently.	18 18
	The quadratic curve in B-splins are planar	D
	· W Even though the computational compexity	- G
	of both cubic & B-splins is similar, cubic	
	Displines produce smoother & better results! Cubic splines have a confirous 200 Derivative	
rail news in	continous 1st Derivotive.	
Isapia	The Lagrangian Andrews .	On On
	a) setup linear system & verily the system with (c, c, c, c) = (40, 0, 120)	<u>an</u>
	=>-1/2/2	A(M)
	In this condition the possible values of a	VIIII
	50 , $\beta_2(0) = \frac{3}{4} - (0)^2$	VIII)
	= 3/4 man + 4 . a = 1	Uni
		all)
·······································	The possible values for a are 1	
	$\beta_{2}(1) = 1/(3 - x)^{2}$	em.
etchici	$\frac{1}{2} \left(\frac{2}{2} \right) = \frac{1}{2} \left(\frac{2}{2} \right)^2$	
1.11	$\frac{2}{2}\left(\frac{3}{2}\right)$	
1910	2 1/2 (1/2)2	(III)
	2 1/	
	18.	er v
The Part of the last of		15

	- if (other lelse)
3	$\beta_2(2) = 0$
9	Pž ()
	The linear system is Used unline calculator
4	(3/ 1/0 m) (c1) (30) to perform motrix
3	(1/2 3/1, 1/2) 2 20 20 THE TOTAL TO
	0 1/8 3/4/ (3/ 90)
<u>.</u>	
3	· Verify (40,0,120) T solves the system.
3 .	(b/4 1/8 b) (40)
3	2 (18 3/4 18 0
3	0 1/8 3/4/120/
2	
	0.125 × 40+ 0.75 × 0 + 0.125 × 120 0×40+0.125 × 0+0.75 × 120
3	(20)
3	20
9	90/
9	
9	
9	B) Analytic expression of the interpolant. Given, we have $2k = k-1$ instead of $2k = k$ i.e
9	Given, we have $2k = K-1$ instead of $2k = K$ i.e
9	$\frac{1}{2} \frac{1}{2} \frac{1}$
9	$\int T(x) = \int_{2}^{3} C_{K} \beta(x-(K-1))$
9	$= 40 \beta_{2}(x-1) + 0 \beta_{2}(x-2) + 120 \beta_{2}(x-3)$
1 -	$= 40 \beta_2 (\lambda_1) + 0 \beta_2 (\lambda_2)$
	(P.T-0)
7	



)	• $I(0) = 20(3/2 - x-1)^2$	
	$\frac{7}{20}\left(\frac{3}{2}-\frac{ 0-1 }{2}\right)^2$	
	² 20 (0.25)	
		*
	I(0)=5 $I(1)$ $T(3 2)=20$	
	I(2) = 20 $I(4) = 15$	7
: 2	© Evaluate the function at 0,3/2,2 +4 + compare with results of 6	
24 24 1	$f(x) = 40x^2 - 130x + 120$	
	$f(0) = 40(0)^{2} - 130(0) + 120 = 120$	
	$f(3 2) = 40(3/2)^{2} - 130(3/2) + 120 = 15$	
	- when $x=2$ - $4(2) = 40(2)^2 - 130(2) + 120 = 20$ - when $x=4$	
	$f(u) = 40(u)^{3} - 130(u) + 120 = 240$	
	5/6	

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