

## Fractional Knapsack:

### OUTPUT:

```
===== Emergency Relief Supply Distribution =====
Enter number of relief items: 5

Enter details for each item:
(Name Weight Value Divisible[1 for Yes, 0 for No])
Item 1: Food 30 120 1
Item 2: Water 20 100 1
Item 3: Medicine 10 200 0
Item 4: Blanket 15 90 0
Item 5: Sanitizer 5 50 1

Enter boat weight capacity (kg): 50

--- Selected Items for Transport ---
Item          Taken(kg)   Value      Type
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Medicine       10           200       Whole
Sanitizer       5            50       Divisible
Blanket        15            90       Whole
Water          20           100       Divisible

Total Utility Value: 440.00
Total Weight Loaded: 50.00 / 50.00 kg

Operation Summary: Relief supplies successfully optimized for transport.
```

### Definition:

The **Fractional Knapsack Problem** is a classic **optimization problem** in computer science where the goal is to maximize the total value of items in a knapsack of limited capacity. Unlike the 0/1 Knapsack, **items can be broken into fractions**, allowing partial selection to fully utilize the knapsack.

### Key Concepts:

1. **Weight ( $w_i$ )** – How heavy the item is.
2. **Value ( $v_i$ )** – Utility or importance of the item.
3. **Value-to-weight ratio ( $v_i/w_i$ )** – Determines item priority for selection.

### Algorithm (Greedy Approach):

1. Calculate the **value-to-weight ratio** for each item.

2. **Sort items** in descending order of ratio.
3. Start adding items to the knapsack:
  - If the item fits entirely, take it.
  - If it doesn't fit, take a **fraction** that fills the remaining capacity.
4. Continue until the knapsack is full.

**Time Complexity:**

- Sorting:  **$O(n \log n)$**
- Selection:  **$O(n)$**
- **Total:**  $O(n \log n)$

**Applications:**

- Resource allocation with limited capacity
- Emergency supply distribution
- Financial portfolio optimization
- Cargo loading optimization