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Subject - ML Assignment (I+II)

1. Info gain:-

$$I(p, n) = -\frac{p}{S} \log_2 \frac{p}{S} - \frac{n}{S} \log_2 \frac{n}{S}$$

$$S = (p+n)$$

$$\Sigma(n) = \sum_{i=1}^v \frac{p_i + n_i}{p+n} I(p_i, n_i)$$

$$\text{Gain}(n) = I(p, n) - E(A)$$

$$S = ST + A + C = 10$$

$$\begin{aligned} \text{Info gain} &= - \left[\frac{3}{10} \log_2 \frac{3}{10} + \frac{3}{10} \log_2 \frac{3}{10} + \frac{4}{10} \log_2 \frac{4}{10} \right] \\ &= - \left[0.6 \times \left(\frac{-0.522}{0.301} \right) + (0.4) (-0.397) \right] \\ &\quad 0.0301 \end{aligned}$$

$$\boxed{\text{Info gain} = 1.562}$$

• finding splitting attr. (attr. with highest gain)

1. Score threat :-

	ST	A	C
Yes	2	1	2
No	1	2	2

$$\begin{aligned} (\text{Info gain})_P &= \text{Entropy}(ST) \\ (\text{Info gain})_P &= \text{Entropy}(S) \end{aligned}$$

E (Score threat)

$$I(\text{Yes}) = - \left[\frac{2}{5} \log_2 \frac{2}{5} + \frac{1}{5} \log_2 \frac{1}{5} + \frac{2}{5} \log_2 \frac{2}{5} \right]$$

$$\begin{aligned} I(\text{Yes}) &= 1.52 \\ I(\text{No}) &= 1.52 \end{aligned} \quad \left. \begin{aligned} E(\text{Score threat}) &= 0.5 \times 1.52 + 0.5 \times 1.52 \\ &= 1.52 \end{aligned} \right\}$$

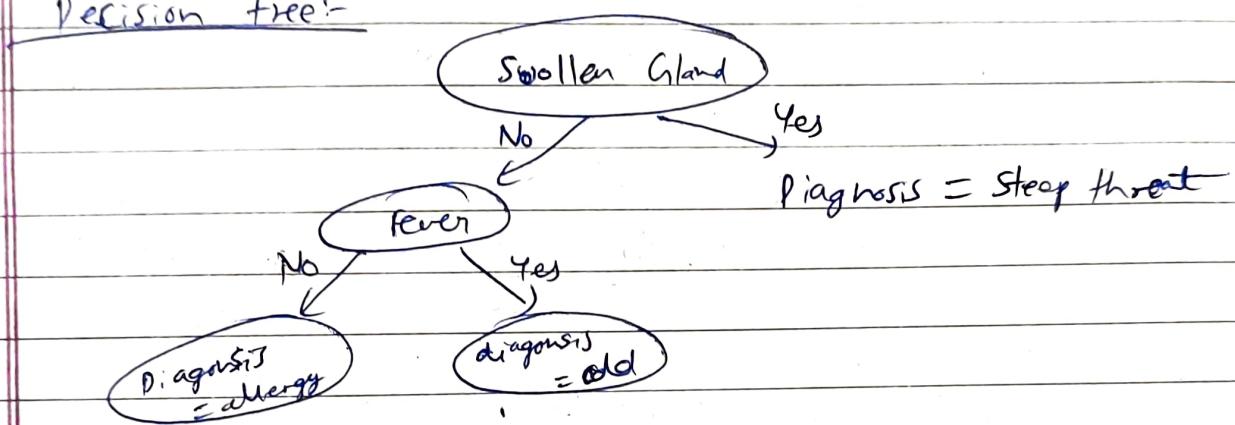
$$\text{Gain} = 1.562 - 1.52$$

$$\boxed{\text{Gain} = 0.05}$$

Gain of each attr.

attr.	gain
sore throat	0.05
fever	0.72
Swollen Gland	0.88
Congestion	0.45
Headache	0.05

Decision tree:-



2. Posilini example (Japan, Honda, blue, 1980, economy)
initialize G to a singleton that includes everything

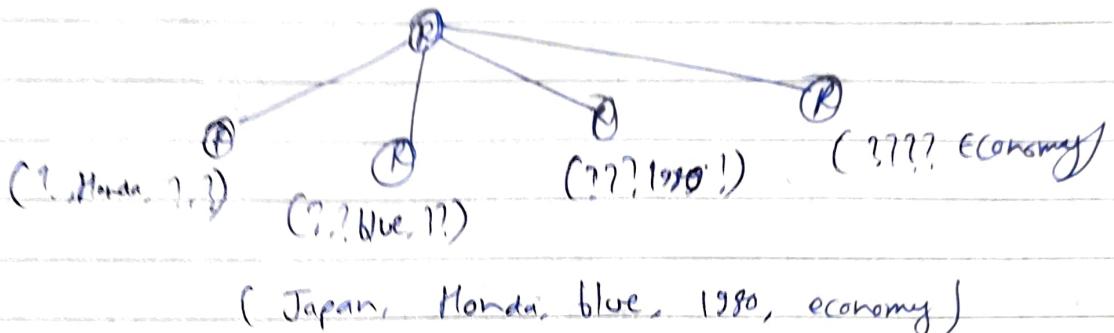
(?) (? , ? , ? , ?)

(Japan, honda, blue, 1980, economy) (?)

These models represent the most general and the most specific heuristics one might learn.

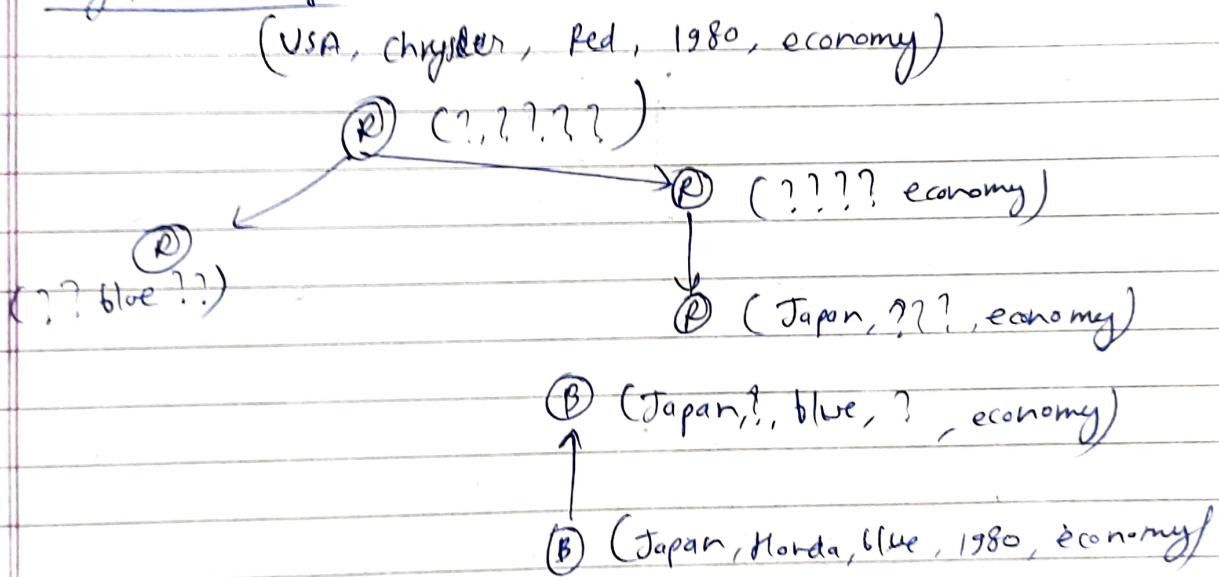
The actual ~~heuristic~~ "Japanese Economy or" probably is between them somewhere within the solution space.

Negative Example: (Japan, Toyota, Green, 1970, sports)



Refinement occurs by generalising S or specialising C, until the heuristic hopefully converges to one that works well.)

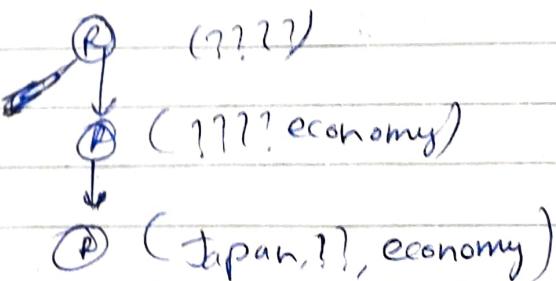
Negative example:



positive example: (Japan, Honda, white, 1980, economy)

Prove Cn to exclude description inconsistent with positive example.

Generate S to include positive example.

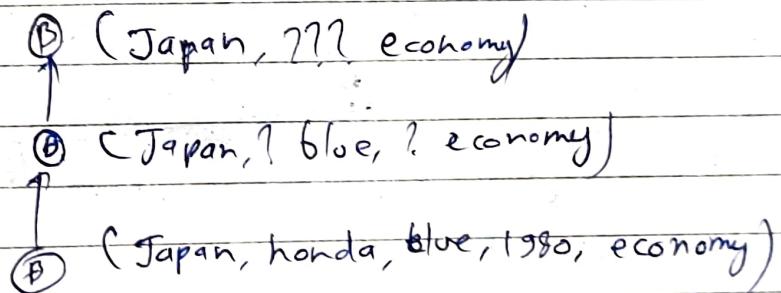
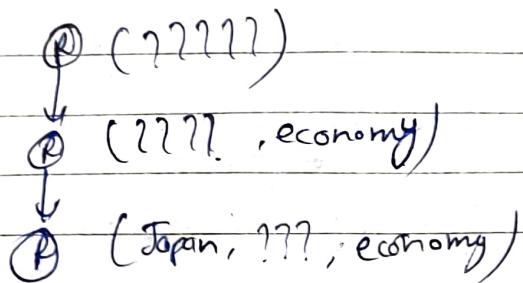
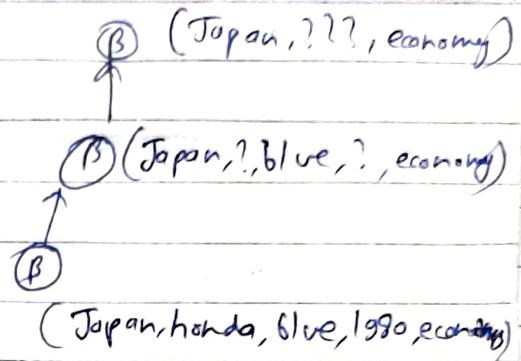


$G \& S$ are singleton sets

and $S = G$

converged

No more data, so algorithm stops.



3. Genetic Algorithm:

A genetic algo. is a search heuristic that is inspired by Darwin's theory of natural evolution. The algorithm reflects the process of natural selection where the fittest individuals are selected for reproduction in order to produce offspring of the next generation.

$$\text{equality } "a + 2b + 3c + 4d" = 30$$

Step-1 :- Initialisation

We define no. of chromosomes in the population are 6.

$$c[1] = [a, b, c, d] = [12, 05, 23, 08]$$

$$c[2] = [a, b, c, d] = [02, 21, 18, 03]$$

$$c[3] = [a, b, c, d] = [10, 04, 13, 14]$$

$$c[4] = [a, b, c, d] = [20, 01, 10, 06]$$

$$c[5] = [a, b, c, d] = [01, 04, 13, 19]$$

$$c[6] = [a, b, c, d] = [20, 05, 17, 01]$$

Step-2) Evaluation:

$$E_{obj}[1] = \text{Abs}(12 + 2 \times 0.5 + 3 \times 23 + 4 \times 08 - 30) = 93$$

$$E_{obj}[2] = \text{Abs}(02 + 2 \times 21 + 3 \times 18 + 4 \times 03 - 30) = 86$$

$$E_{obj}[3] = \text{Abs}(10 + 2 \times 04 + 3 \times 13 + 4 \times 14 - 30) = 83$$

$$E_{obj}[4] = \text{Abs}(20 + 2 \times 1 + 3 \times 10 + 4 \times 6 - 30) = 46$$

$$E_{obj}[5] = \text{Abs}(1 + 2 \times 4 + 3 \times 13 + 4 \times 19 - 30) = 94$$

$$E_{obj}[6] = \text{Abs}(20 + 2 \times 05 + 3 \times 17 + 4 \times 01 - 30) = 55$$

Step-3) Selection

$$\text{Fitness}[1] = 0.0106$$

$$\text{Fitness}[2] = 0.0123$$

$$\text{Fitness}[3] = 0.0119$$

$$\text{Fitness}[4] = 0.0213$$

$$\text{Fitness}[5] = 0.0105$$

$$\text{Fitness}[6] = 0.0179$$

$$\text{total} = 0.0106 + 0.0123 + 0.0119 + 0.0213 + 0.0105 + 0.0179$$

$$= 0.0845$$

$$P[i] = \text{Fitness}[i] / \text{total}$$

$$P[1] = 0.1254$$

$$P[2] = 0.1456$$

$$P[3] = 0.1408$$

$$P[4] = 0.2521$$

$$P[5] = 0.1243$$

$$P[6] = 0.2118$$

$$c[1] = 0.1254, \quad c[2] = 0.2710, \quad c[3] = 0.4119 \\ c[4] = 0.6639, \quad c[5] = 0.7882, \quad c[6] = 1.0$$

$$R[1] = 0.201, \quad R[2] = 0.284, \quad R[3] = 0.099 \\ R[4] = 0.822, \quad R[5] = 0.398, \quad R[6] = 0.501$$

Thus chromosomes in population become

$$c[1] = [02, 21, 19, 03], \quad c[2] = [10, 04, 13, 14] \\ c[3] = [12, 05, 23, 08], \quad c[4] = [20, 05, 17, 01] \\ c[5] = [10, 04, 13, 14], \quad c[6] = [20, 01, 10, 06]$$

begin

$K \leftarrow 0$

while ($K < \text{population}$) do

$R[K] = \text{random}(0-1);$

if ($R[K] < p_c$) then

select chromosome [K] as parent;

end

$K = K + 1;$

end;

end;

Now we generate a random number R as the number of population

$$R[1] = 0.191, \quad R[2] = 0.259, \quad R[3] = 0.760 \\ R[4] = 0.006, \quad R[5] = 0.159, \quad R[6] = 0.340$$

parents $c[1], c[4]$ & $c[5]$ will be selected for crossover

$c[1] \times c[4]$

$c[1] \times c[5]$

$c[4] \times c[5]$

$$C[1] = [02, 05, 17, 01]$$

$$C[2] = [10, 04, 13, 14]$$

$$C[3] = [12, 05, 23, 08]$$

$$C[4] = [20, 04, 13, 14]$$

$$C[5] = [10, 04, 18, 03]$$

$$C[6] = [20, 01, 10, 06]$$

Step 5 Mutation :-

$$\text{Total gen} = 4 \times 6 = 24$$

$$\text{Best chromosome obtained} = [07, 05, 03, 01]$$

$$a=7, b=5, c=3, d=1$$

$$\Rightarrow a + 2b + 3c + 4d = 0$$

$$\Rightarrow 7 + 2 \times 5 + 3 \times 3 + 4 \times 1 = 30$$

4. Bayes theorem is a way to figure out conditional probability. Conditional probability is the probability of an event happening, given that it has some relationship to one or more other events.

$$P(A|B) = P(B|A) \cdot \frac{P(A)}{P(B)}$$

Problems in Applying :-

1. choice of Prior:- This is the usual carping for a reason coming up with a prior well that well reason and actually represents your best attempt at summarizing a prior is a great deal of work.

2. Computationally intensive :-

For large dataset with many variables, being estimated. It may very intensive in computation.

5. K-Nearest Neighbours (KNN) algorithm is a type of supervised ML algorithm which can be used for both classification as well as regression predictive problems.

- Lazy Learning Algorithm :-

KNN is lazy learning algorithms because it does not have a specialised training phase.

- Non parametric learning Algo. :-

KNN is also a non-parametric learning algorithm because it does not assume anything about the underlying data.

- Numerical :-

1. Determine $K = \text{nearest neighbour}$

use $K=3$

2. calculate distance

$$(7,7) \rightarrow (7-3)^2 + (7-7)^2 = 16$$

$$(7,4) \rightarrow (7-3)^2 + (7-4)^2 = 25$$

$$(3,4) \rightarrow (3-3)^2 + (4-7)^2 = 9$$

$$(1,4) \rightarrow (1-3)^2 + (4-7)^2 = 13$$

3. sort the distance & determine minimum distance.

4. Gather the category of the nearest neighbours.

5. Use simple majority of the category of nearest neighbours as the prediction value of query instance.

6. $x_1 = 3, x_2 = 7$ lies in good category.

6. Types of Neural Networks

1. Feed-forward Neural Network - Artificial Neuron

This neural network is one of the simplest forms of ANN, where the data or the input travels in one direction.

2. Radial basis function Neural Network -

It consider the distance of a point with respect to the center. RBF function have two layers. First where the feature are combined with the radial basis functions in the inner layer & output of these features.

3. Kohonen self organising Neural Network -

The objective of Kohonen map is to input vectors of arbitrary dimension to discrete map comprised of neurons.

4. Recurrent Neural Networks

The RNN work on the principle of savings the output of a layer and feeding them back to the input to help in predicting the outcome of the layer.

5. Convolutional neural Network

It is similar to feed forward neural network, where the neurons have learnable weights & biases.

7. The required perception had 3 inputs A, B, C. The constants 1. The values of A & B are 1 (true) or -1 (false)

A	B	$O = A \wedge B$
-1	-1	-1
-1	1	-1
1	-1	1
1	1	-1

The line crosses the A axis at 1 & B axis at -1.

The equation of the line is

$$\frac{A - O}{1 - O} = \frac{B - (-1)}{0 - (-1)} \Rightarrow A = B + 1$$

$$\Rightarrow \cancel{A - B = 1}$$

$\beta, 1, -1, 1$ are possible values for the weights w_1, w_2, w_3 . Using these values the output of the perception for $A=1, B=-1$, is -ve. Therefore we need to negate the weights and therefore we can conclude that $w_0 = -1, w_1 = 1, w_2 = 1$

8. The main Requirements of clustering algos:-

- Scalability
- dealing with diff. types of attributes
- discoverable clusters of arbitrary shapes
- minimal requirements for domain knowledge to determine input parameters.
- ability to deal with noise & others
- insensitivity to order of input records
- high dimensionality
- interpretability & usability.

9. The goal of a support vector machine is to find the optimal hyperplane which maximises the margin of the training data.

Calculating Margin :-

Given a particular hyperplane, we can compute the distance b/w the hyperplane and the closest data point. Once we have their values if we double it we will get what is called the margin.

That is why the objective of the sum is to find the operating hyperplane which maximises the margin of the training data.

10. Steps of machine learning:-

1. Data Collection → Quantity and Quality of the data indicate how accurate the model is.

2. Data Preparation → Arrange the data and prepare it for training.

3. choose Model - Different Algo are for different tasks choose the right one.

4. Train the Model:- The goal of training is to answer a question or make a prediction correctly.

5. Evaluate the Model: Uses some metric or combination of metrics to measure objective performance of the Model.

6 Parameter learning: Train model parameter to improve performance.

7. Make prediction:

using test set data a better approximation of how the model will perform in real world.

The checker problem:

T: playing checkers.

P: percent of games won against opponents

E: playing practice games against itself

target function V . Board $\rightarrow \mathbb{R}$

$$\hat{V} = w_0 + w_1 x_1(b) + w_2 x_2(b) + w_3 x_3(b) \\ + w_4 x_4(b) + w_5 x_5(b) + w_6 x_6(b)$$

Adjusting the weights.

$$E = \sum_{(b, V_{\text{train}}(b)) \in \text{learning example}} (V_{\text{train}}(b) - \hat{V}(b))^2$$

LMS Algo:-

$$1. \text{ compute error}(b) = V_{\text{train}}(b) - \hat{V}(b)$$

2. for each board feature x_i , update weight
 $w_i \leftarrow w_i + \eta \cdot \text{error}(b) \cdot x_i$

Find design for checkers system:

- ① The performance system \Rightarrow takes a new board as I/O
a trace of the game.
- ② The critic :- Takes the trace of game as Input & output
a set of training example of the target fn.
- ③ The generaliser :- Takes training example as input output
hypothesis that estimates the target.
- ④ Experiment generator :- It takes the current I/O a
new problem for the performance to expose.