

Economics Assignment

1.

$$\text{Max. } Z = 6x_1 + 8x_2$$

$$\text{Subject to } 30x_1 + 20x_2 \leq 300$$

$$5x_1 + 10x_2 \leq 110$$

$$x_1, x_2 \geq 0$$

Converting inequality to equality

$$Z_{\max} = 6x_1 + 8x_2 + 0s_1 + 0s_2$$

$$30x_1 + 20x_2 + s_1 = 300$$

$$5x_1 + 10x_2 + s_2 = 110$$

C_i	Basic Var.	Quantity	6 x_1	8 x_2	0 s_1	0 s_2
0	s_1	300	30	20	1	0
0	s_2	110	5	10	0	1
	Z_i	0	0	0	0	0
	$C_j - Z_j$		6	8	0	0

pivot column $\rightarrow x_2$

pivot ~~column~~ row $= \frac{300}{20} = 15, \frac{110}{10} = 11$

hence s_2 is replaced with x_2 .

C_i	Basic Var.	Quantity	6 x_1	8 x_2	0 s_1	0 s_2
0	s_1	80	20	0	1	-2
8	x_2	11	1/2	1	0	1/10
	Z_j	88	4	8	0	4/5
	$C_i - Z_j$		2	0	0	-4/5

Now s_1 is replaced with x_2 .

pivot = 20

C_i	Basic Var.	Quantity	6	8	0	0
			x_1	x_2	s_1	s_2
6	x_1	4	1	0	$1/20$	$-1/10$
8	x_2	9	0	1	$-1/40$	$3/20$
	Z_j	96	6	8	$1/10$	$3/5$
	$C_j - Z_j$		0	0	$-1/10$	$-3/5$

All $C_j - Z_j$ are either zero or negative. hence optimal solution is

$$x_1 = 4, x_2 = 9, Z_j = 96$$

2.

$$Z_{\min} = 5x_1 + 6x_2$$

$$2x_1 + 5x_2 \geq 1500 \text{ \& } 3x_1 + x_2 \geq 1200$$

$$2x_1 + 5x_1 + A_1 - s_1 = 1500$$

$$3x_1 + x_2 + A_2 - s_2 = 1200$$

$$Z_{\min} = 5x_1 + 6x_2 + MA_1 + MA_2 - 0s_1 - 0s_2$$

C_j	Var.	Qty.	5	6	M	M	0	0
			x_1	x_2	A_1	A_2	s_1	s_2
M	A_1	1500	2	5	1	0	-1	0
M	A_2	1200	3	1	0	1	0	-1
	Z_j	2700M	5M	6M	M	M	-M	-M
	$-(C_j - Z_j)$		5M-5	6M-6	0	0	-M	-M

(3)

Now A_1 is replaced with x_2 so A_1 is artificial variable which is replaced so it does not appear.

C_j	Var	C_j Qty.	5	6	M	0	0
			x_1	x_2	A_1	s_1	s_2
6	x_2	300	$2/5$	1	0	$-1/5$	0
M	A_1	900	$13/5$	0	1	$1/5$	-1
	Z_j	$900M + 1800$	$\frac{3}{5}M + \frac{12}{5}$	6	M	$-6/5 + M/5$	-M
	$Z_j - C_i$		$\frac{13}{5}M - \frac{13}{5}$	0	0	$-6/5 + M/5$	-M

Now A_1 is replaced with x_1 , A_1 gets eliminated.

C_j	Var.	C_j Qty.	5	6	0	0
			x_1	x_2	s_1	s_2
6	x_2	$2100/13$	0	1	$-1/13$	$2/13$
5	x_1	$4500/13$	1	0	$1/13$	$-5/13$
	Z_j	$35100/13$	5	6	$-1/13$	-1
	$Z_j - C_i$		0	0	$-1/13$	-1

all $(Z_j - C_i)$ values are either zero or -ve
hence optimal solution is reached -

$$x_1 = \frac{4500}{13}, \quad x_2 = \frac{2100}{13}, \quad Z_j = 2700$$