



Data Communication (CSX-208) Dr Samayveer Singh

Data Link Layer
Error Detection and
Correction

Error Detection and Correction

- Networks must be able to transfer data from one device to another with complete accuracy.
- Data can be corrupted during transmission.
- For reliable communication, errors must be detected and corrected.
- Error detection and correction are implemented either at the data link layer or the transport layer of the OSI model.
- Types of error: Single-bit error and burst Error

Single-bit error

- In a single-bit error, only 1 bit in the data unit has changed.

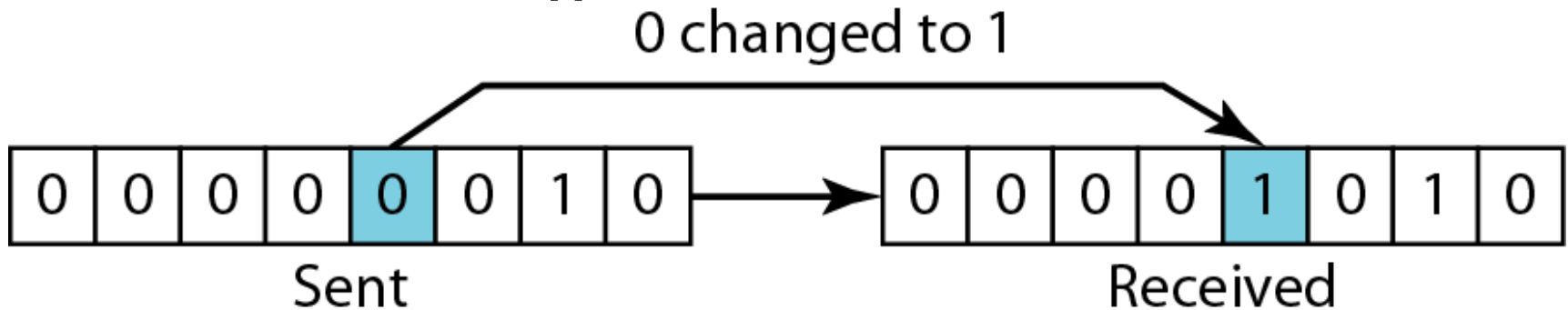


Figure: Single –bit error

Burst error

- A burst error means that 2 or more bits in the data unit have changed.

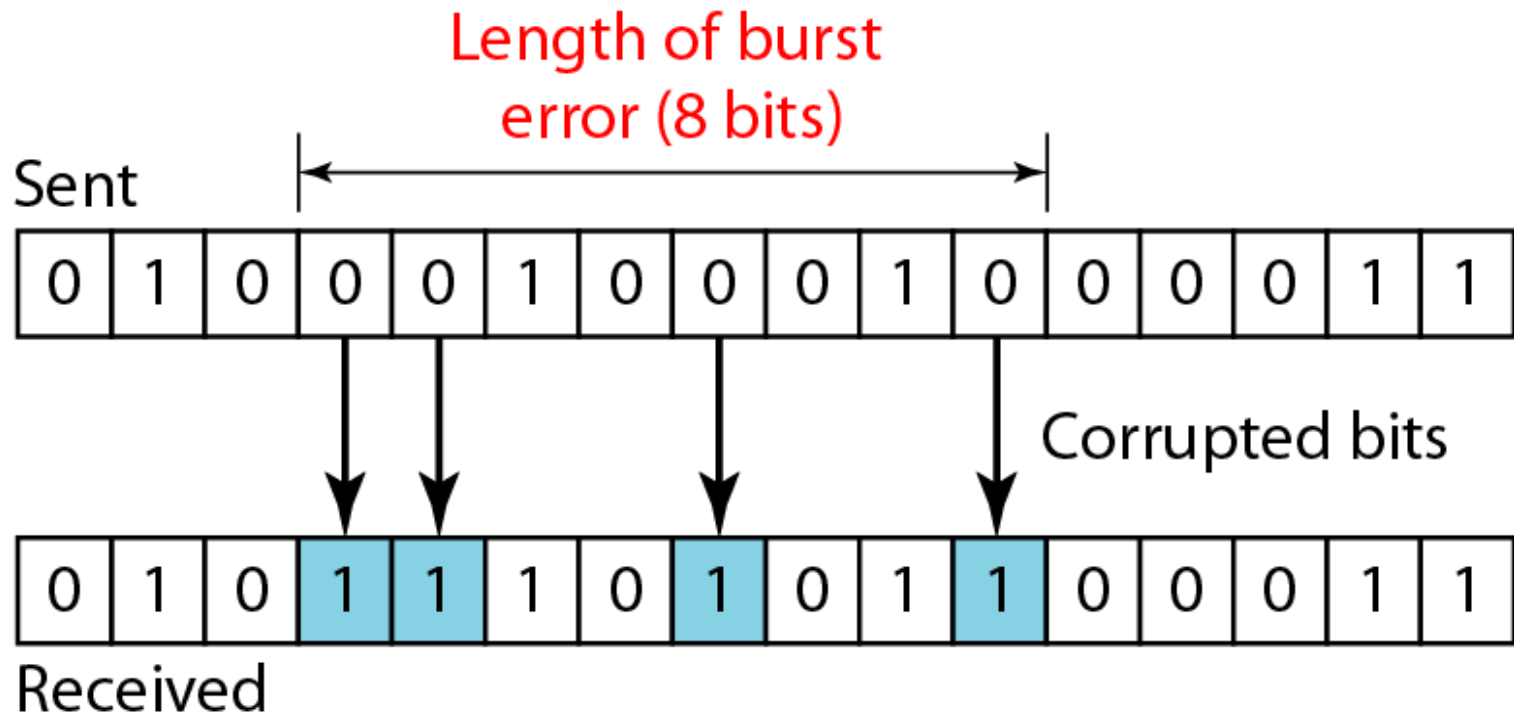


Figure: Burst error of length 8

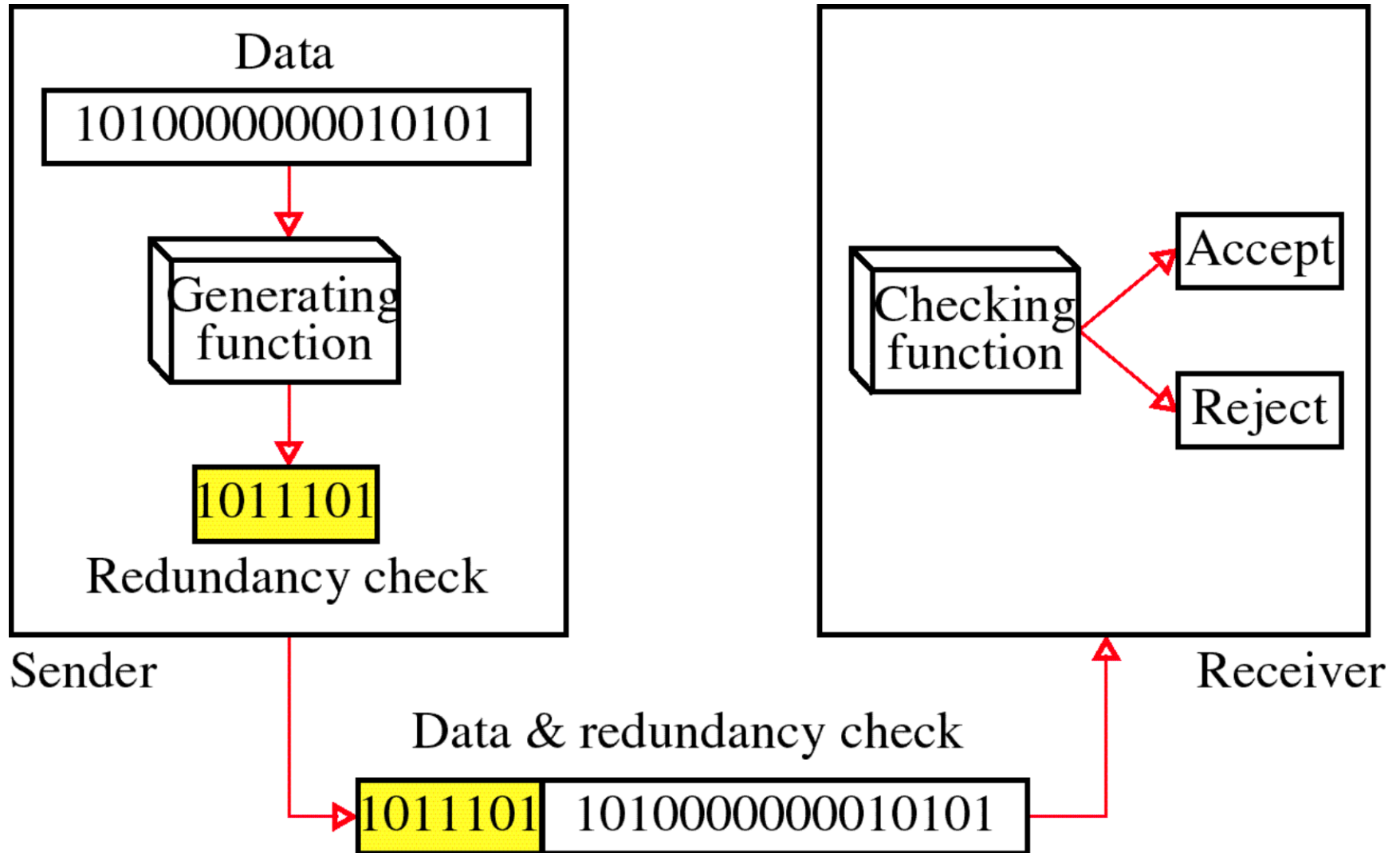
Example:

- ★ The number of bits affected depends on the data rate and duration of noise.
- ➔ If data is sent at rate = 1Kbps then a noise of 1/100 sec can affect 10 bits. $(1/100 * 1000)$
- ➔ If same data is sent at rate = 1Mbps then a noise of 1/100 sec can affect 10,000 bits. $(1/100 * 10^6)$

Error detection

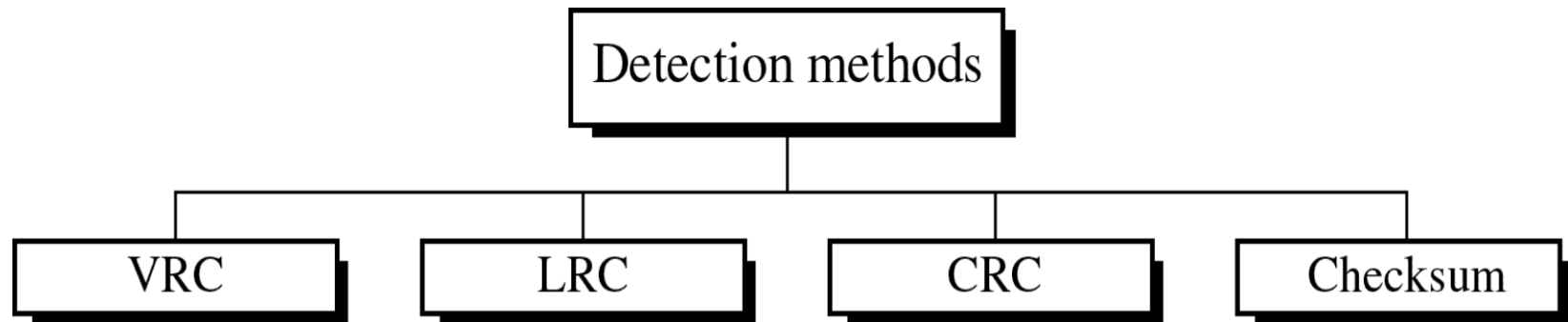
- Error detection means to decide whether the received data is correct or not without having a copy of the original message.
- Error detection uses the concept of redundancy, which means adding extra bits for detecting errors at the destination.

Redundancy

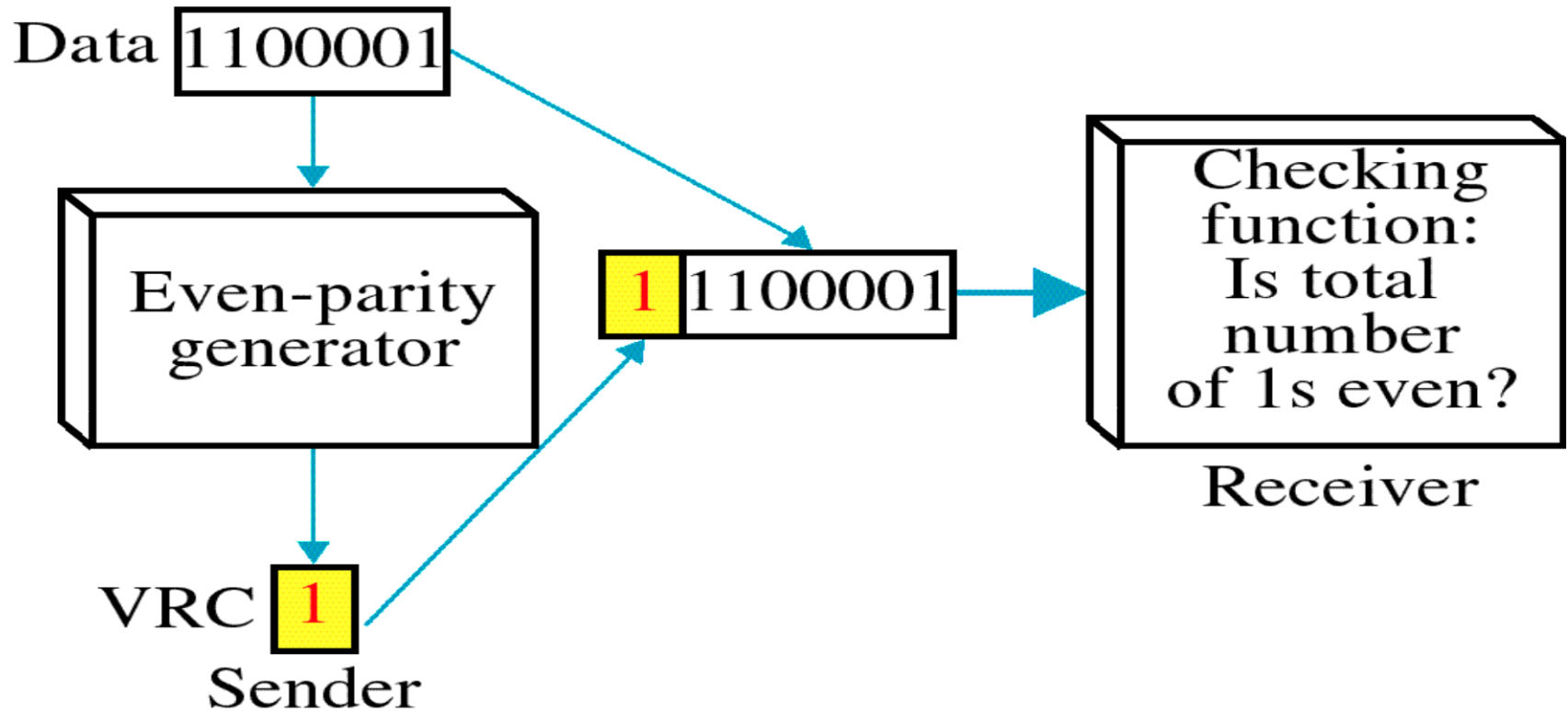


Detection methods

- Four types of redundancy checks are used in data communications

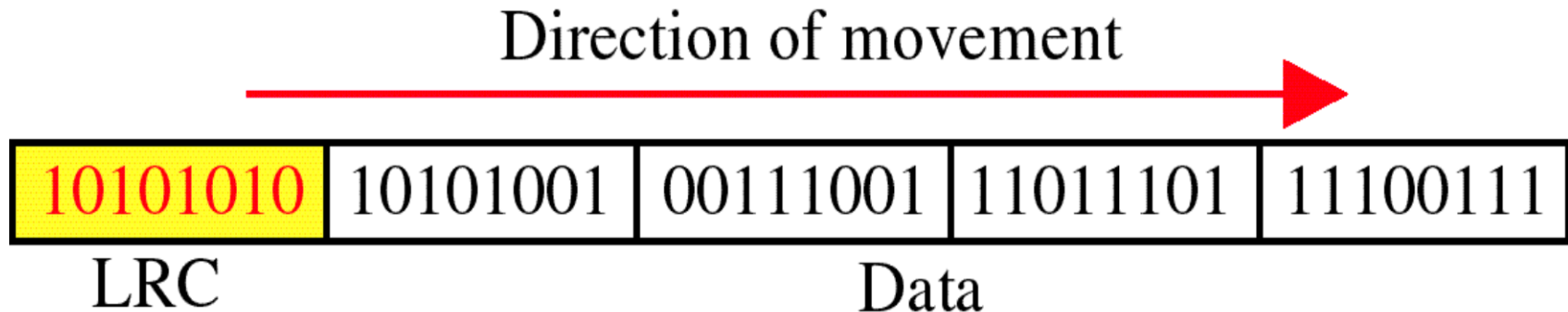


Vertical Redundancy Check (VRC)



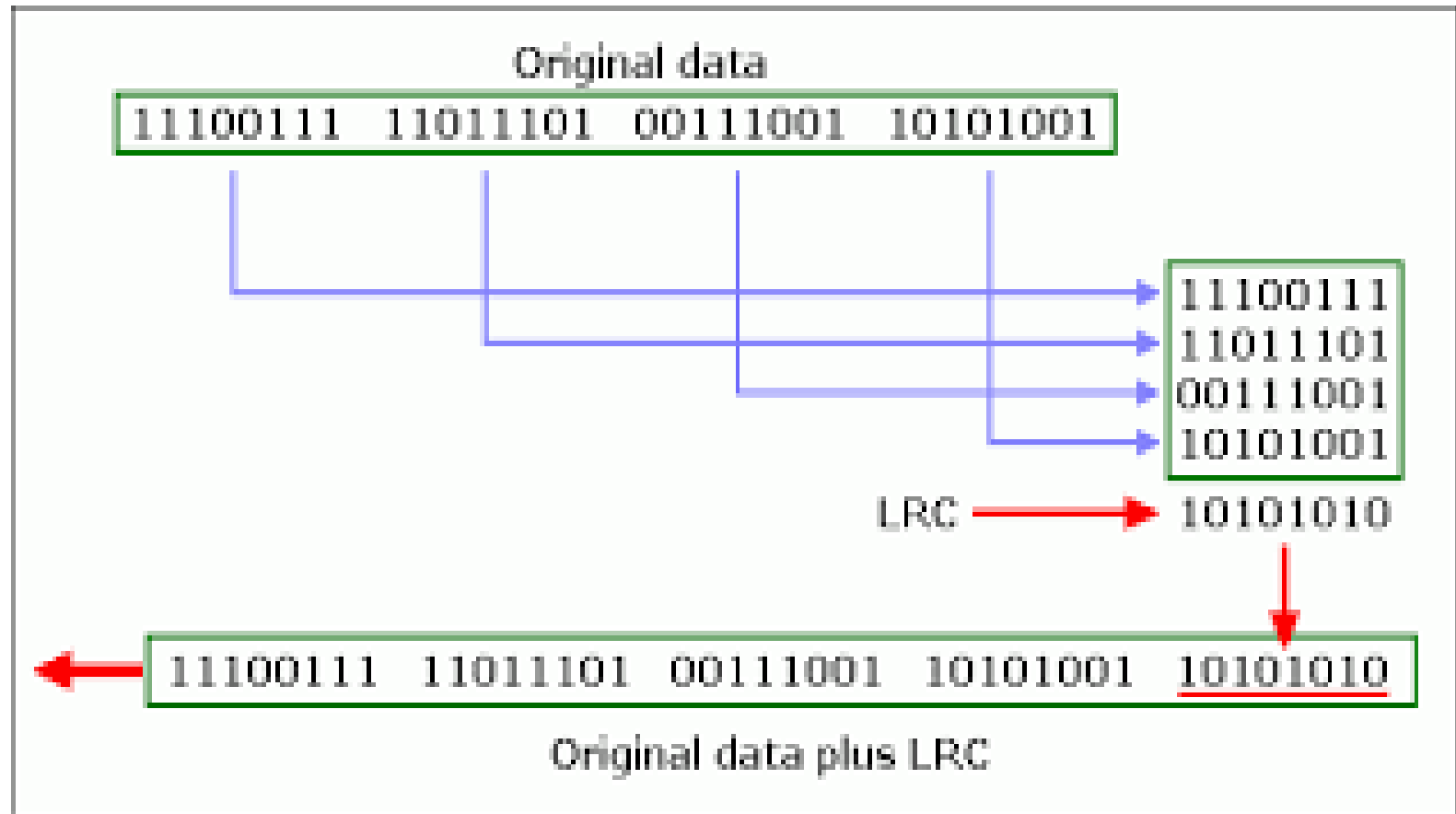
- ➡ It can detect single bit error
- ➡ It can detect burst errors only if the total number of errors is odd.

Longitudinal Redundancy Check (LRC)

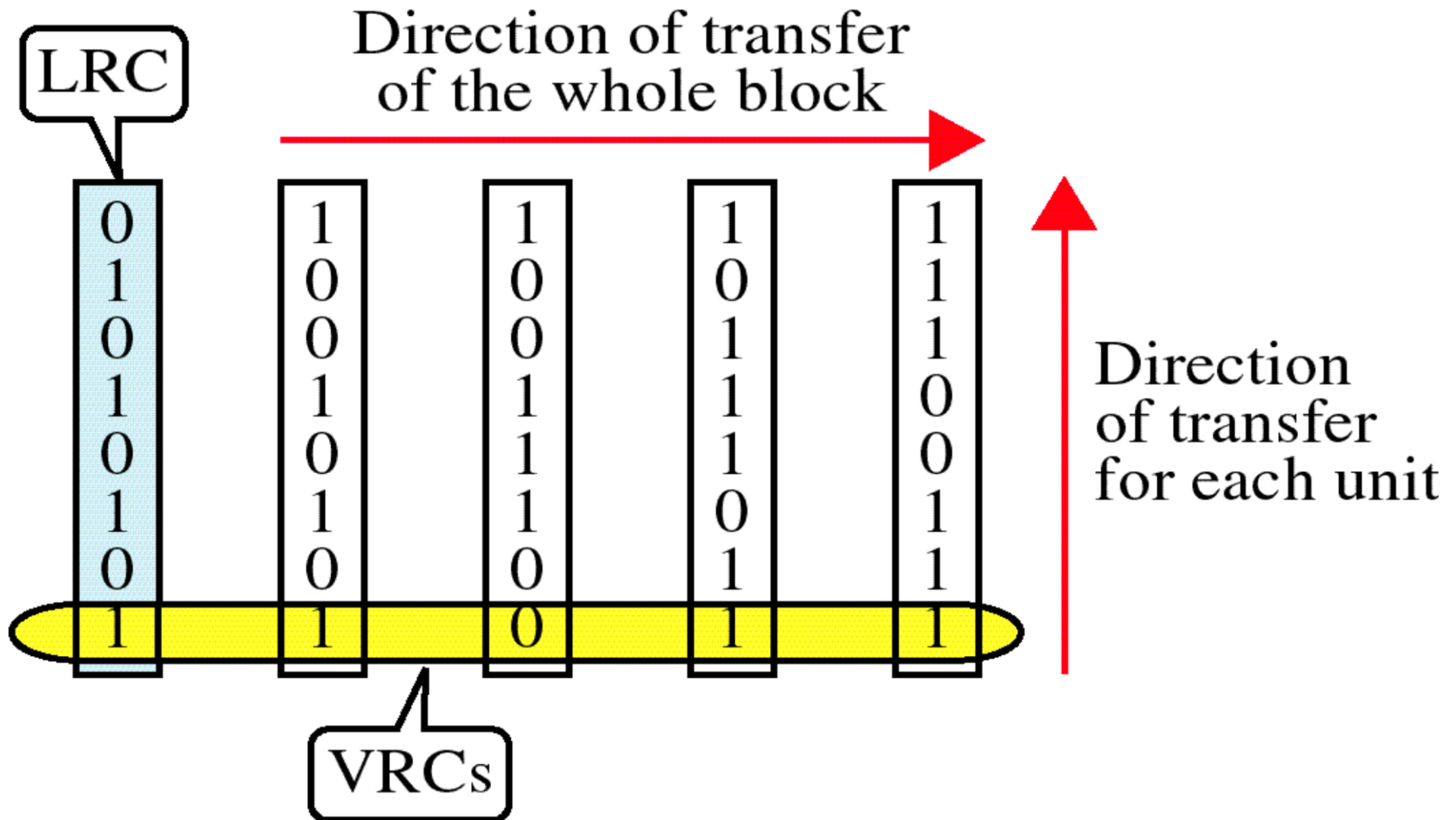


- If two bits in one data units are damaged and two bits in exactly the same positions in another data unit are also damaged, the LRC checker will not detect an error.
- Eg. Two data units are 11110000 and 11000011. If the first and last bits in each of them is changed. The data units are **01110001** and **01000010** and error cant be detected.

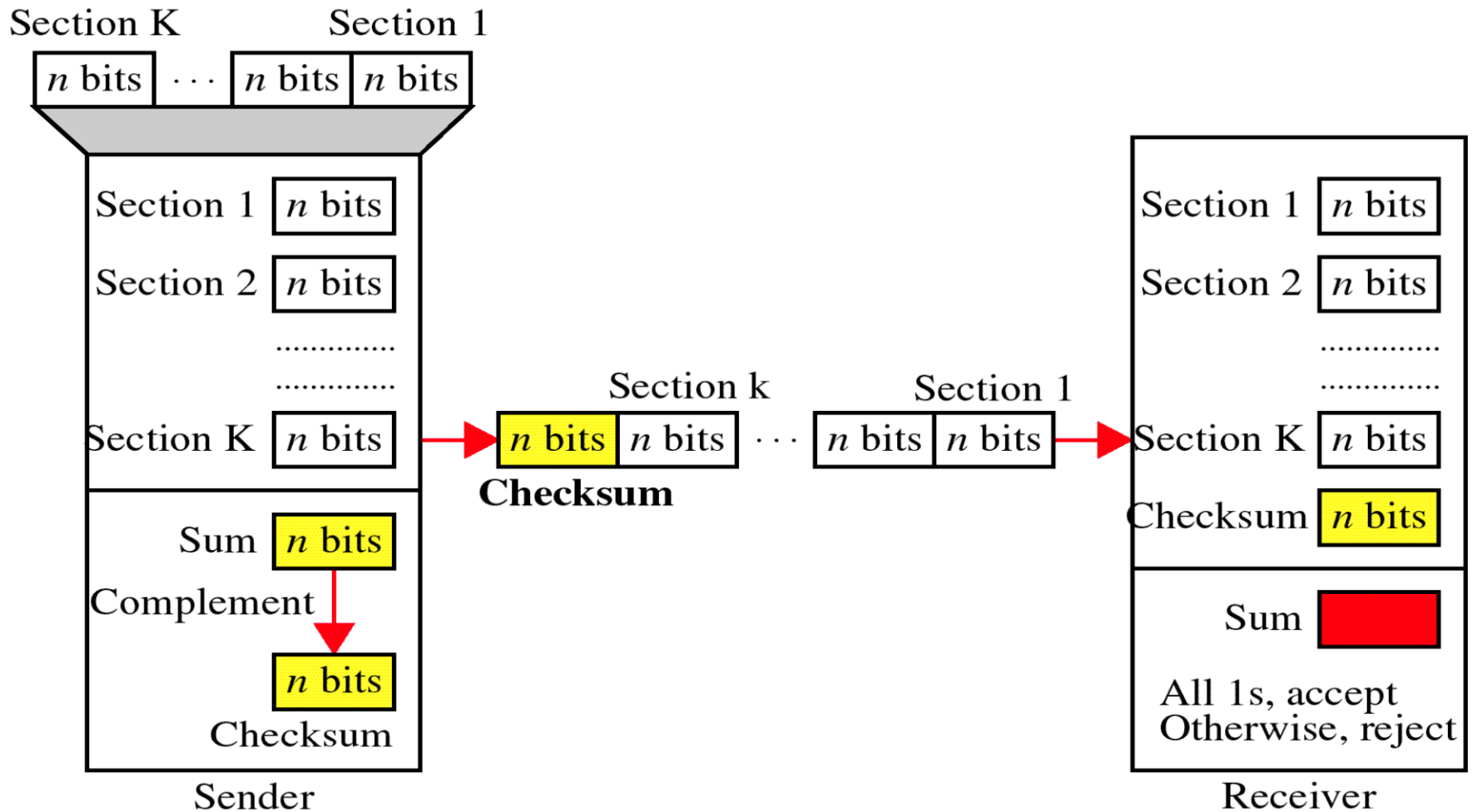
LRC



VRC and LRC



Checksum



At the sender



- The unit is divided into k sections, each of n bits.
- All sections are added together using one's complement to get the sum.
- The sum is complemented and becomes the checksum.
- The checksum is sent with the data

At the receiver

- The unit is divided into k sections, each of n bits.
- All sections are added together using one's complement to get the sum.
- The sum is complemented.
- If the result is zero, the data are accepted: otherwise, they are rejected.

Example Part 1

- Suppose the following block of 16 bits is to be sent using a checksum of 8 bits.
- 10101001 00111001
- The numbers are added using one's complement
- | | |
|-----|----------|
| | 10101001 |
| | 00111001 |
| | ----- |
| Sum | 11100010 |
- Checksum **00011101**
- The pattern sent is 10101001 00111001 **00011101**

Example part 2

- Now suppose the receiver receives the pattern sent in Example 1 and there is no error.
- 10101001 00111001 00011101
- When the receiver adds the three sections, it will get all 1s, which, after complementing, is all 0s and shows that there is no error.
- 10101001
- 00111001
- 00011101
- Sum 11111111
- Complement **00000000** means that the pattern is OK.

Example 3

Now suppose there is a burst error of length five that affects four bits.

10101111 11111001 00011101

When the receiver adds the three sections together, it gets

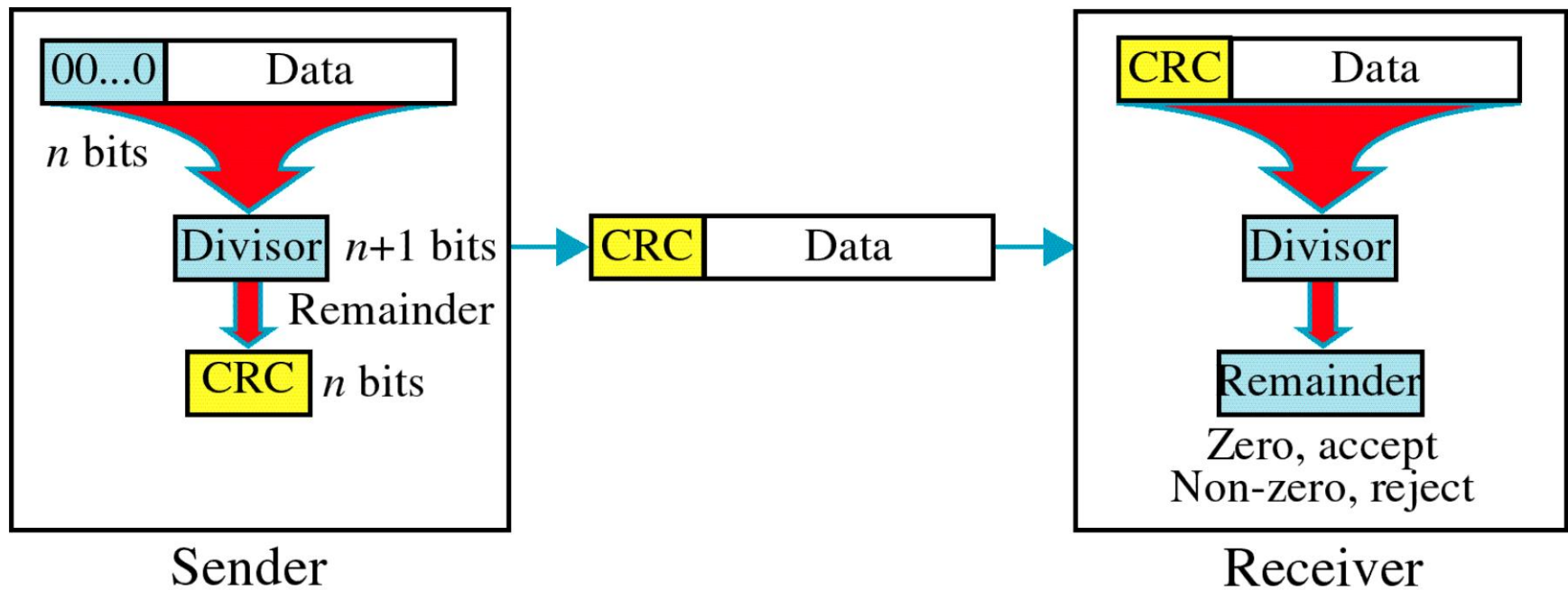
			10101111
			11111001
			00011101

Result	1		11000101
Carry			1

Sum			11000110
Complement			00111001

means that the pattern is corrupted.

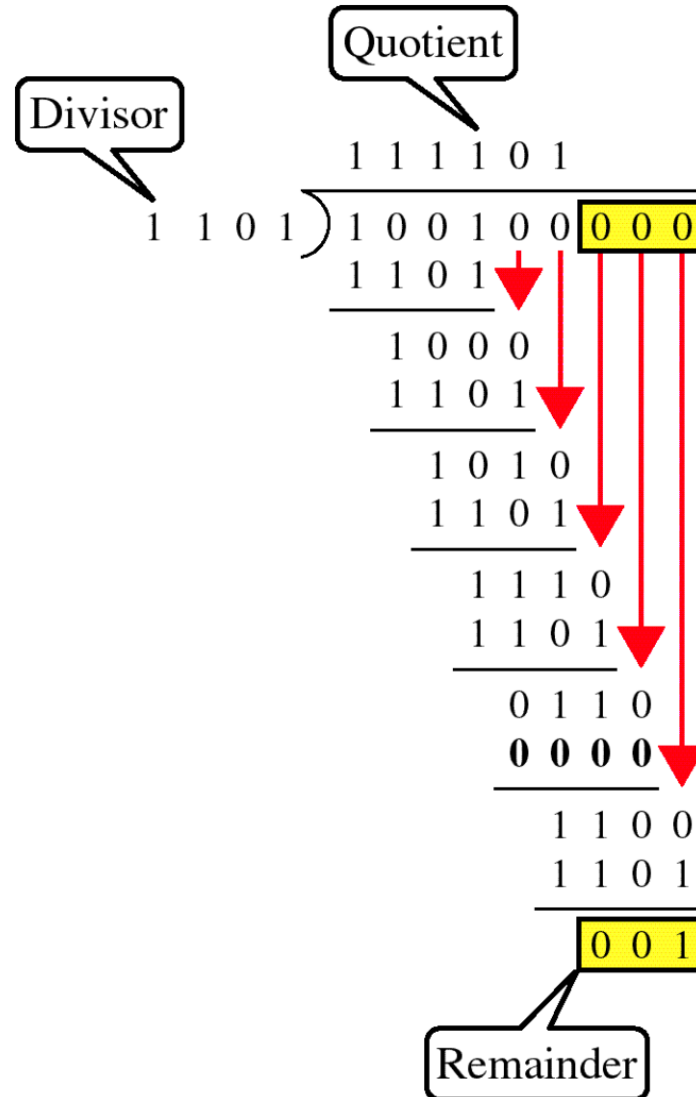
Cyclic Redundancy Check (CRC)



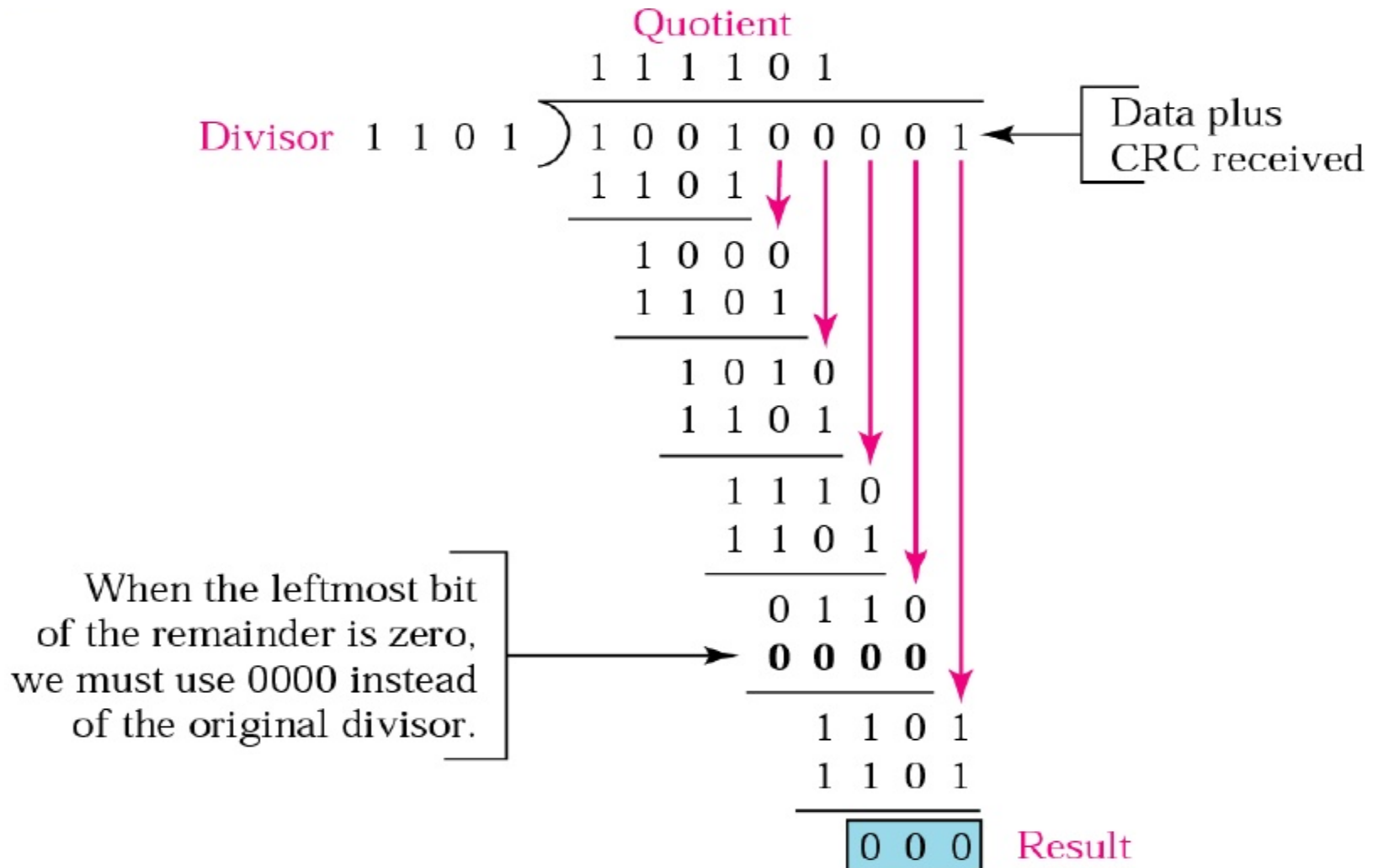
Cyclic Redundancy Check

- Given a k -bit frame or message, the transmitter generates an n -bit sequence, known as a frame check sequence (FCS), so that the resulting frame, consisting of $(k+n)$ bits, is exactly divisible by some predetermined number.
- The receiver then divides the incoming frame by the same number and, if there is no remainder, assumes that there was no error.

Binary Division



Binary Division



Error Correction

➤ *It can be handled in two ways:*

- Receiver can have the sender retransmit the entire data unit.
- The receiver can use an error-correcting code, which automatically corrects certain errors.

➤ *Single-bit error correction*

- To correct an error, the receiver reverses the value of the altered bit. To do so, it must know which bit is in error.

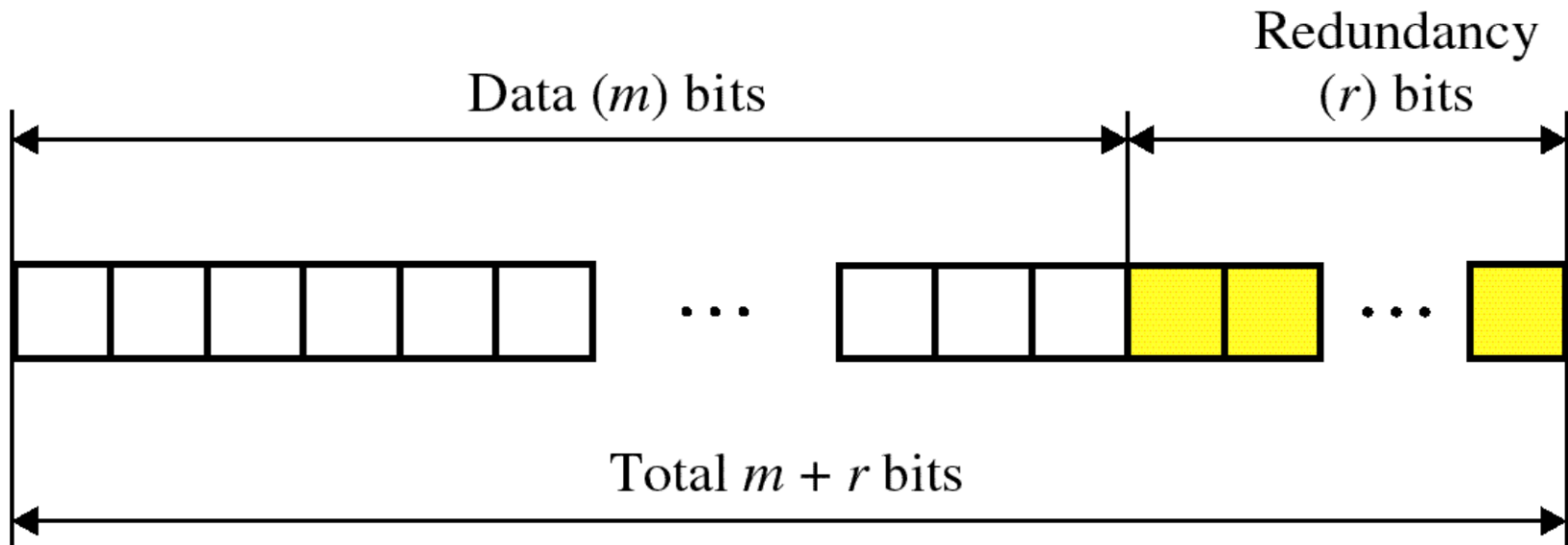
Number of redundancy bits needed

➤ Let data bits = m and redundancy bits = r

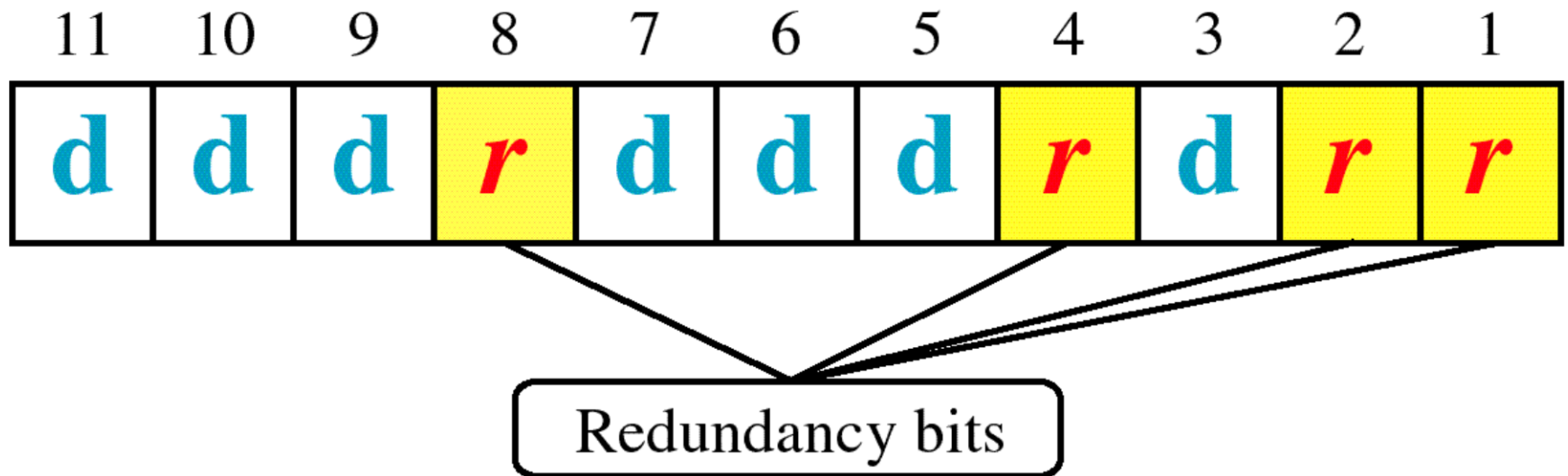
\therefore Total message sent = $m+r$

The value of r must satisfy the following relation:

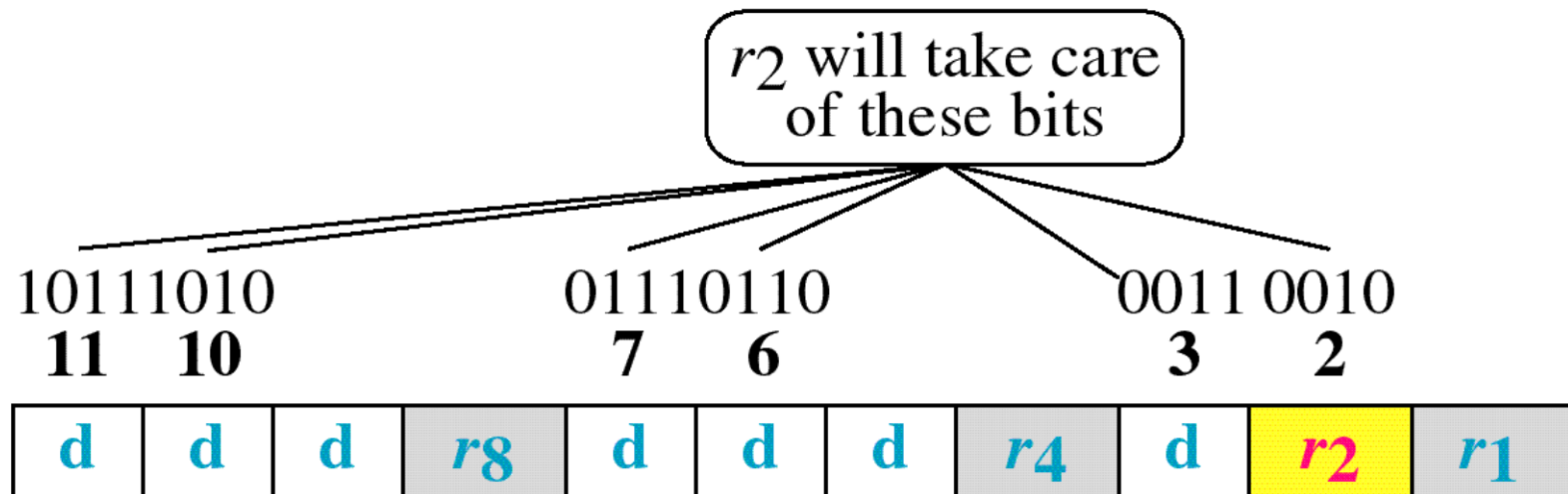
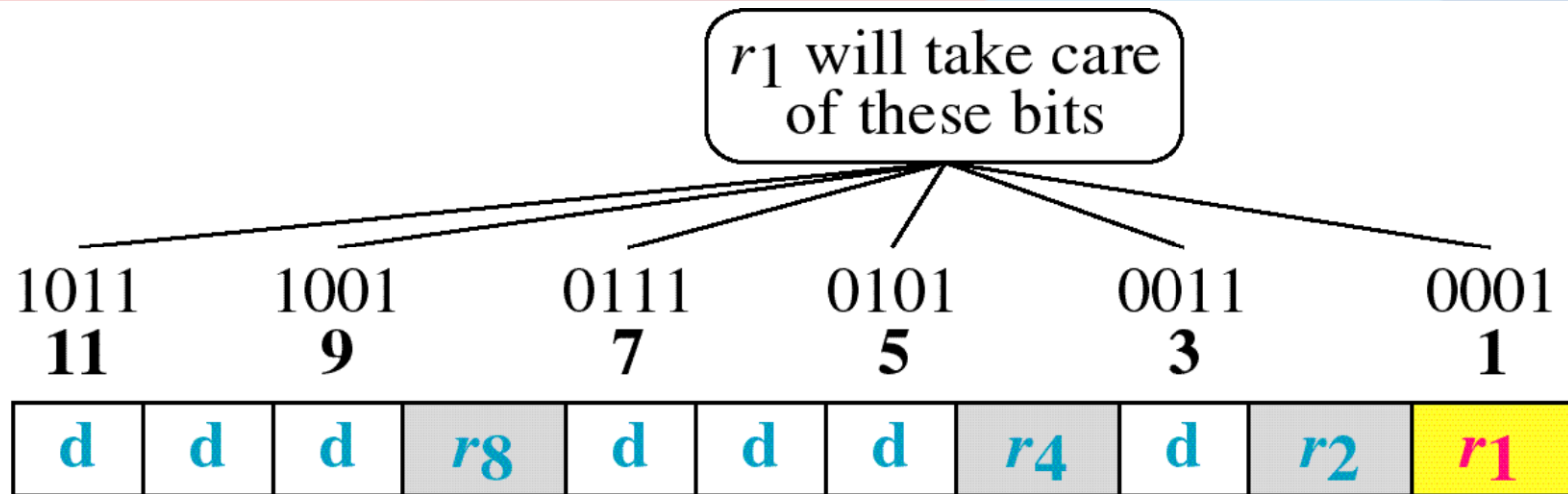
$$2^r \geq m+r+1$$



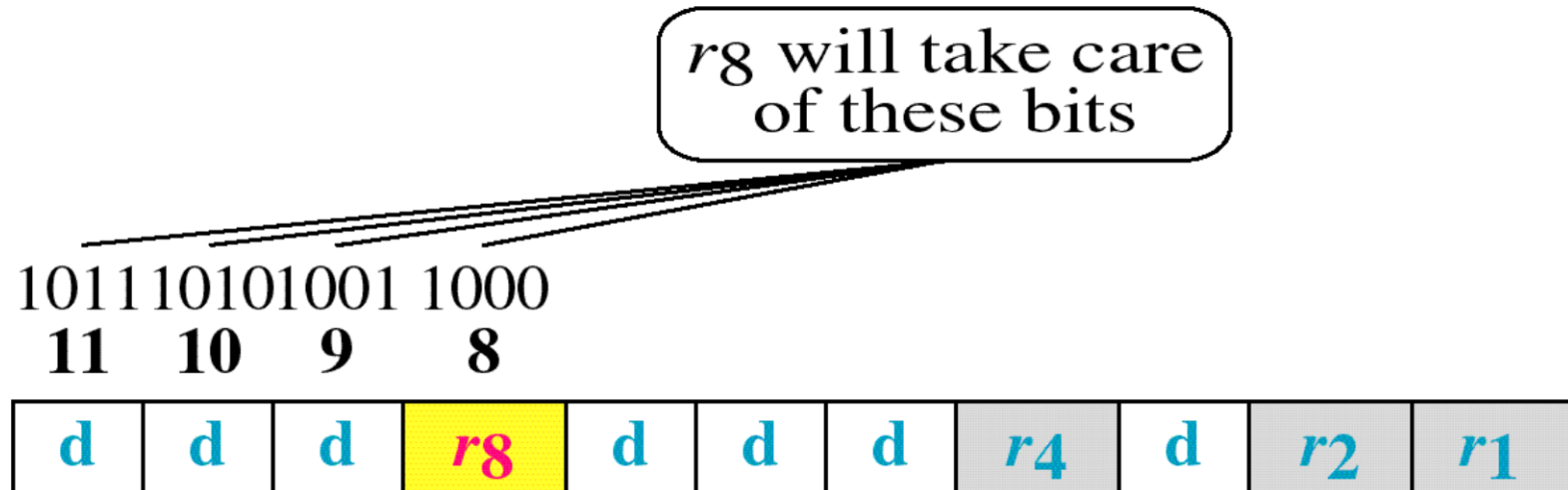
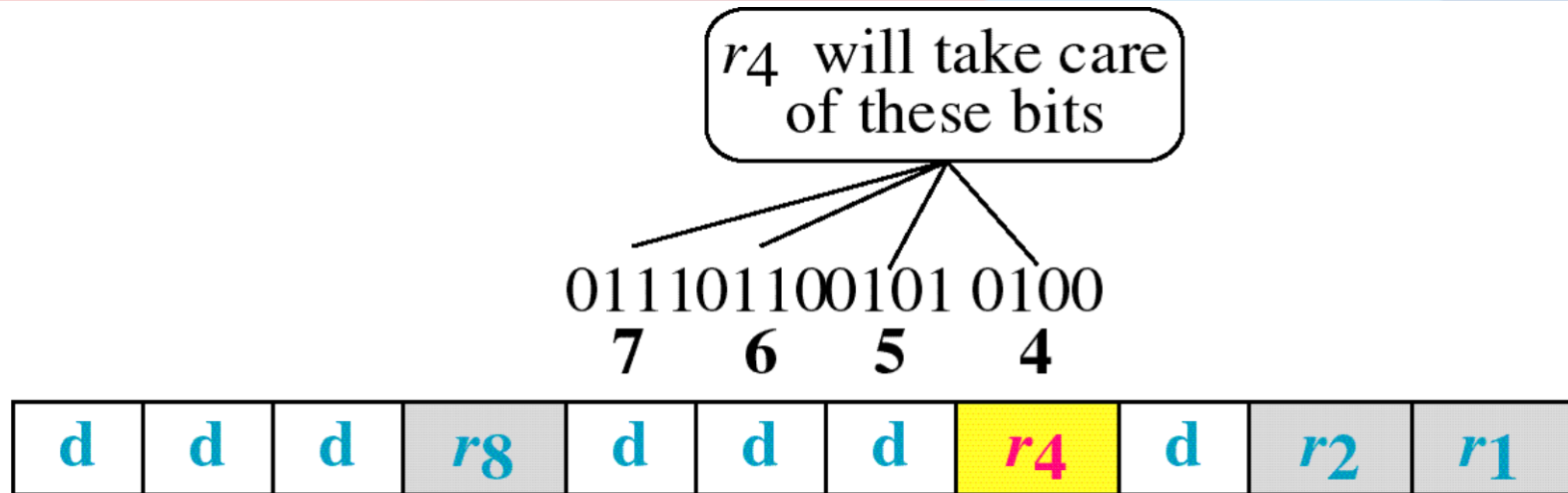
Hamming Code



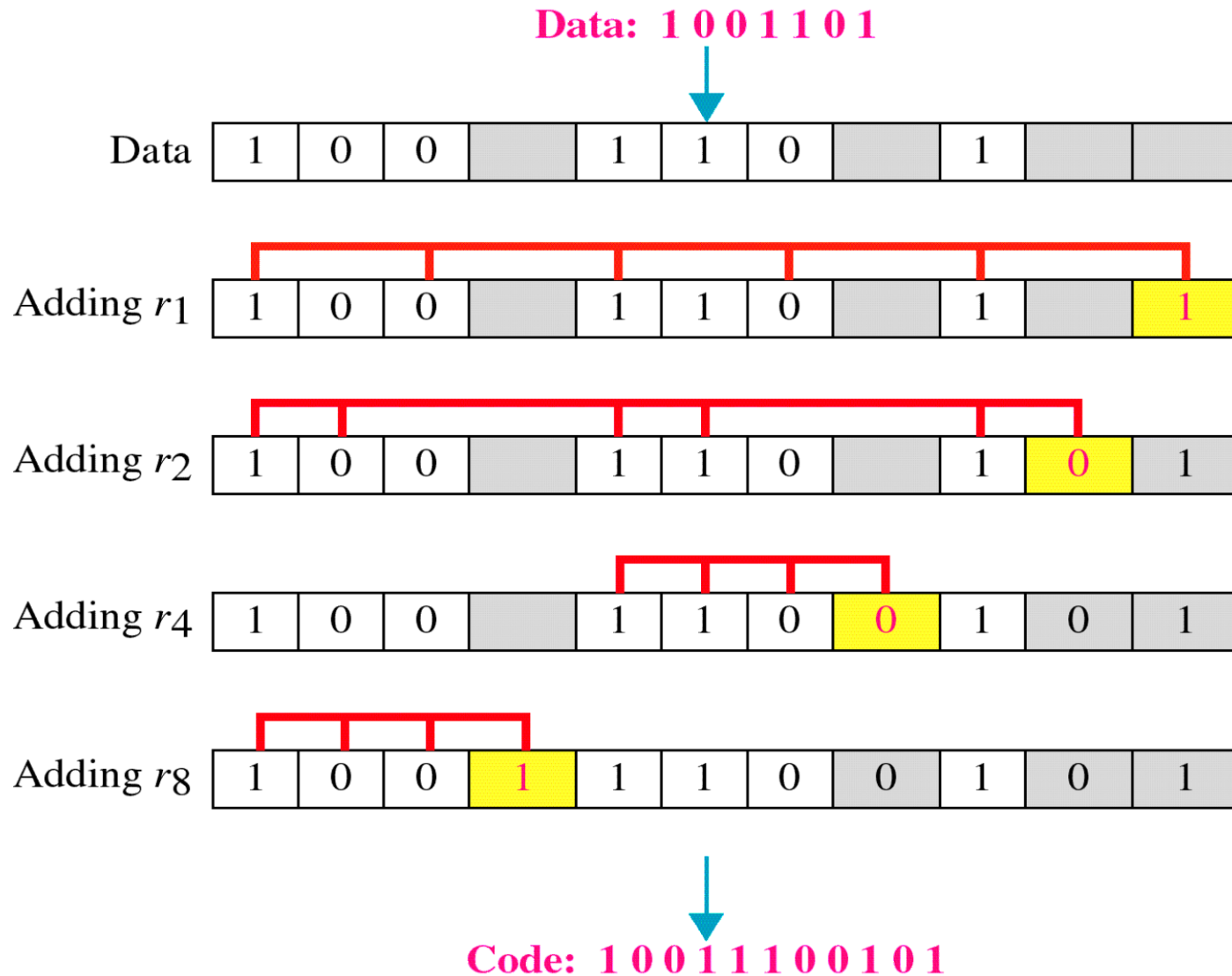
Hamming Code



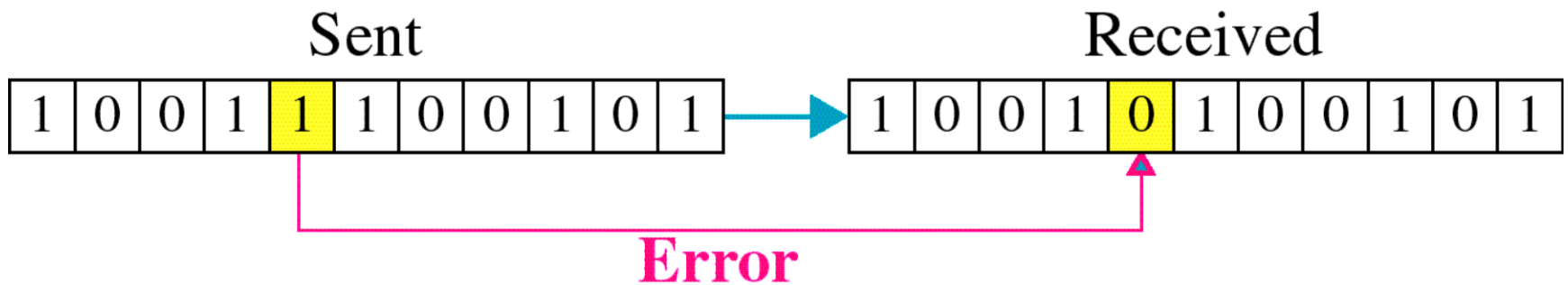
Hamming Code



Example of Hamming Code



Single-bit error



Error Detection

