

Task 2.2.a

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In [1]: 1 # For the given problem, dependent variable is "Price of the flat (z)" and
        2 # i.e "Size of the flat in square ft(x)" & "number of bedrooms in the flat(y)"
        3 # let  $z = ax+by+c$  is a hyperplane which is nearest to the points given in the dataset
        4 # Now, using least square method for linear regression,  $x=(a,b,c)^T = (A^T A)^{-1} A^T z$ 
        5 # This concept is described in part 2.1
        6 # The code is written below
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```
In [2]: 1 #Importing libraries
        2 import numpy as np
```

```
In [3]: 1 dataset = [[1600,3,8.2],
        2             [1260,2,6.6],
        3             [1800,4,10.3],
        4             [600,1,1.7],
        5             [850,2,3.6],
        6             [920,2,4.4],
        7             [1090,2,5.4],
        8             [890,2,4.8],
        9             [1340,3,10.5],
        10            [1650,2,7.4]]
        11 # For each sublist of list dataset, 1st entry shows x value, 2nd entry shows y value, 3rd entry shows z value
```

```
In [4]: 1 # writing it in  $z = ax+by+c$  form and then convert it into matrix form
        2 # I am writing it in matrix equation form directly
        3
        4 A=[]
        5 for i in range(10):
        6     temp=[]
        7     temp.append(dataset[i][0])
        8     temp.append(dataset[i][1])
        9     temp.append(1) # for coefficient of c i.e. 1
        10    A.append(temp)
        11
        12 B=[]
        13 for i in range(10):
        14     B.append(dataset[i][2])
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In [5]: 1 # Printing matrix A and vector B
        2 print(A)
        3 print(B)

[[1600, 3, 1], [1260, 2, 1], [1800, 4, 1], [600, 1, 1], [850, 2, 1], [920, 2, 1], [1090, 2, 1], [890, 2, 1], [1340, 3, 1], [1650, 2, 1]]
[8.2, 6.6, 10.3, 1.7, 3.6, 4.4, 5.4, 4.8, 10.5, 7.4]
```

```
In [6]: 1 #writing function for transpose of a matrix
        2 def transpose(A,m,n):
        3     trans=[]
        4     for j in range(n):
        5         temp=[]
        6         for i in range(m):
        7             temp.append(A[i][j])
        8         trans.append(temp)
        9     return trans
```

```
In [7]: 1 trans_A= transpose(A,10,3)
        2 print(transpose(A,10,3)) # printing transpose of matrix A

[[1600, 1260, 1800, 600, 850, 920, 1090, 890, 1340, 1650], [3, 2, 4, 1, 2, 2, 2, 2, 3, 2], [1, 1, 1, 1, 1, 1, 1, 1, 1, 1]]
```

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In [8]: 1 mul = np.dot(trans_A, A) # multiplying  $A^T$  and A
        2 inv = np.linalg.inv(mul) # inverse of  $A^T A$ 
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3 prod= np.dot(inv,trans_A) # multiplying (A^T*A)^-1 and A^T
4 res = np.dot(prod R) # finding (A^T*A)^-1 * A^T* R
In [9]: 1 # So, our result matrix is
        2 print(res) # It shows the values of a,b,c
[ 0.00362953  1.67818099 -1.9252501 ]

```

Conclusion : Best fit hyperplane for the given data is $z = 0.0036x + 1.6781y - 1.9252$

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To estimate the upper and lower limit of bank loan based on the requirement, I will use the above

best fit hyperplane

Here, according to requirement $950 \leq x \leq 1050$ and $y=2,3$

For, $x= 950, y=2 \rightarrow z = 4.851$

For, $x= 950, y=3 \rightarrow z = 6.5291$

For, $x= 1050, y=2 \rightarrow z = 5.211$

For, $x= 1050, y=3 \rightarrow z = 6.8891$

It means, for 950 square ft. flat with 2 bedrooms, flat cost will be minimum ie 4.851 millions and

for 1050 square ft. flat with 3 bedrooms, flat cost will be maximum ie 6.8891 millions

Note: These are just estimates