

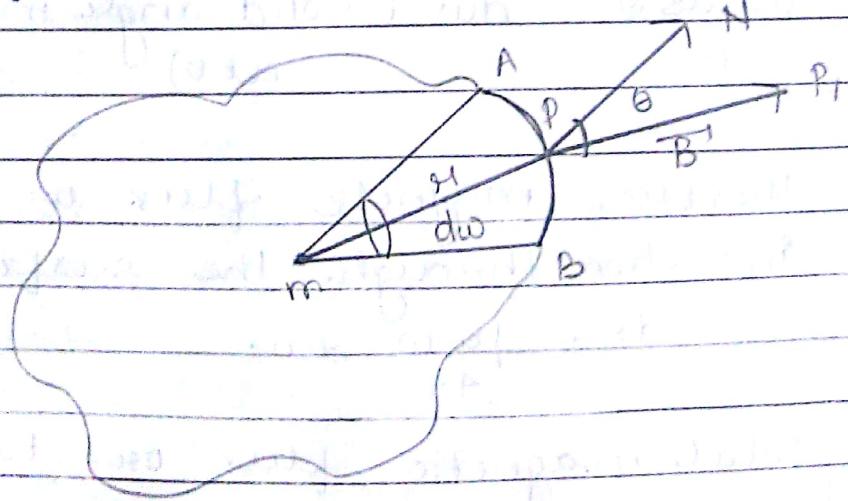
→ Gausses law in Magnetism:— Total normal magnetic

induction of magnetic flux through a surface represent the no. of lines of force crossing the surface in a direction normal to the surface. It is defined as the dot product of magnetic field vector (B^1) and area vector (A^1). Area vector represent the area of a surface in a dirⁿ normal to the surface. Magnetic flux is denoted by ϕ and it is a scalar quantity. Unit of magnetic flux in SI system is Weber (Wb) i.e.,

$$\phi = B^1 \cdot A^1$$

→ Gauss thm in Magnetism

Statement : Gausses thm states that total normal magnetic induction or magnetic flux over a closed surface is equal to μ_0 times in algebraic sum of the pole strength inside the closed surface.



consider a closed surface S inside which a pole of strength 'm' is placed. AB is small surface of surface area ds on the closed surface S. P is a point on AB. Pole is placed at O. Let $OP = r$. PN is normal on AB. Magnitude of magnetic field (B) at P due to pole strength 'm' at O is given by

$$B = \frac{\mu_0 m}{4\pi r^2} \text{ (along PP)}$$

θ = Angle between magnetic field \vec{B} and normal PN.

Resolve component of B along PN = $B \cos \theta$

induction through the surface AB of area ds = $B \cos \theta \cdot ds$

$$= \frac{\mu_0 m}{4\pi r^2} \cos \theta \cdot ds$$

$$= \frac{\mu_0 m}{4\pi r^2} \frac{ds \cos \theta}{r^2}$$

$$\frac{ds \cos \theta}{r^2} = dw \quad (\text{solid angle made by surface AB at } O)$$

therefore magnetic flux or normal magnetic induction through the surface AB of area

$$ds = \frac{\mu_0 m}{4\pi} dw$$

total magnetic flux or total normal magnetic induction through the closed

Teacher's Signature.....

Date		
Page No.		

surface. $S = \frac{\mu_0 m}{4\pi} \oint d\omega$

$\therefore \oint d\omega = 4\pi$ = Total solid angle made by closed surface S at O.

\therefore Total magnetic flux through the closed surface $= \frac{\mu_0 m}{4\pi} \times 4\pi$
 $= \cancel{\mu_0 m}$ proved

If the pole strength m is outside the closed surface. Then total magnetic flux through the closed surface is 0.

→ For objective ques:-

\because isolated poles is not possible and magnetic lines of force from the closed loop therefore there are as many as magnetic field lines outside the closed surface as their inside the closed surface.

\therefore Total magnetic flux over the closed surface is 0.

i.e., $\oint \vec{B} \cdot d\vec{s} = 0$

This integral is called surface integral of magnetic field. A result something different from the gauss law of electrostatics.

Wave particle duality of radiations.

- The phenomenon of interference, the interaction and polarisation of light, can only be explained by considering the light travel in the form of wave. i.e., it is an electromagnetic radiation but after the invention of photoelectric effect and compton effect it has been established that electromagnetic radiation exhibits corpuscular nature or particle nature. i.e., E.M.W we have as particles also it means that sometimes it behaves as wave and sometimes it behaves as particle. it is called wave particle duality or dual nature of electromagnetic radiation.

Photo electric effect is experimental evidence of corpuscular nature of electromagnetic radiation. A/c to photo-electric effect when electromagnetic radiation of particular wavelength and frequency incident on a particular metal surface then electrons are emitted from the metal surface.

The emitted electrons are called photoelectrons. The minimum frequency at which electrons are emitted from the metal surface is called threshold frequency (ν_0) and energy corresponding

to threshold frequency is called work function (ϕ_0).

If ν_0 = threshold frequency
then threshold energy or work function (ϕ_0)
 $= h\nu_0$

Work function is the characteristic of metal surface.

The nature of photoelectric effect couldn't be explained by classical theory. It was explained by Einstein in 1905 on basis of quantum theory given by Max Planck.

According to Max theory electromagnetic electro-magnetic radiation doesn't act like a wave only, but consist of quanta of photons of energy ($h\nu$) where h is Planck's constant.

Photons behave as particle having rest mass 0 and it moves with velocity equal to velocity of light (c). Photons has energy equal to $h\nu$. The concept of Max Planck proves the wave particle duality. i.e., electromagnetic radiation behave as wave as well as particles in the form of photons of quanta of energy ($h\nu$).

Let ν = frequency of incident wave

ν_0 = threshold frequency

Energy of incident wave = $h\nu$

Threshold energy = $h\nu_0$

$$\nu > \nu_0$$

m = mass of ejected electrons

v = velocity of ejected electrons.

K.E of ejected electrons = $\frac{1}{2}mv^2$.

from the law of conservation of energy

$$hv = hv_0 + \frac{1}{2}mv^2$$

$$\text{or } \frac{1}{2}mv^2 = h(v - v_0) \quad \text{①}$$

This eqn ① is called einstein photo-electric eqn.

from eqn ① it is clear that

- 1) Energy of ejected electron depends upon the frequency of the incident wave.
- 2) The no. of electrons emitted from the metal surface depends upon the intensity of incident wave.
- 3) The energy of ejected electron doesn't depend upon the intensity of incident wave and the no. of electrons emitted from metal surface doesn't depend upon the frequency of incident wave.

21/08/18

Date

Page No.

→ Wave Particle duality of Matter :-

We know that electromagnetic radiation behaves as wave as well as particle i.e., it posses dual nature.

In 1924 De-Broglie put forward a bold hypothesis that matter should also posses dual nature i.e., it behave as particle as well as wave.

→ The following observation led him that matter should also posses dual nature.

- 1) The whole energy in this universe is due to radiation and matter.
- 2) Nature love symmetry.
- 3) When radiation possess dual nature then matter should also possess dual nature.

a/c to de-Broglie every moving material particle associated with a wave of wavelength.

$$\lambda = \frac{h}{p} \quad \text{--- (1)}$$

where h is planks constant. and p is momentum of particle. these wavelength is called de-Broglie wavelength and the wave is called de-Broglie wave or matter wave.

Date _____
Page No. _____

If 'm' is the mass of the particle and
'v' is the velocity of the particle,
then $p = mv$

$$\lambda = \frac{h}{mv} \quad \text{--- (2)}$$

eqn ① relates momentum which is the characteristics of particle with wavelength which is the characteristics of wave.

- 1) Lighter the particle greater is the de-broglie wavelength.
- 2) Higher is the velocity of the particle smaller is the de-broglie wavelength.
- 3) De-broglie wavelength is independent of nature and charge of the particle.
- 4) De-broglie wave is different from that of electromagnetic wave. Electromagnetic wave are produced by accelerated charged particle.

Eqn ② is called De-broglie eqn.

• De-Broglie wavelength of electrons :-

Let m = mass of the electron

e = charge of the electron

V = applied potential difference to accelerate the electron

E = energy acquired by the electron

$$E = ev$$

v = velocity of the electron

$$E = \frac{1}{2} mv^2$$

$$v^2 = \frac{2E}{m} \Rightarrow v = \sqrt{\frac{2E}{m}}$$

We know that,

$$\lambda = \frac{h}{mv}$$

$$\text{or } \lambda = \frac{h}{m \sqrt{\frac{2E}{m}}}$$

$$\text{or } \lambda = \frac{h}{\sqrt{2meV}}$$

$$\text{finally } \lambda = \frac{h}{\sqrt{2meV}} \quad \text{--- (1)}$$

We know that

$$m = 9.1 \times 10^{-31} \text{ Kg}$$

$$h = 6.62 \times 10^{-34} \text{ Js}$$

$$e = 1.6 \times 10^{-19} \text{ coulomb}$$

Teacher's Signature.....

$$\lambda = \frac{6.62 \times 10^{-34}}{\sqrt{2 \times 9.1 \times 10^{-31} \times 1.6 \times 10^{-17}}} \times \frac{1}{\sqrt{V}}$$

$$= \frac{12.27 \times 10^{-10}}{\sqrt{V}} \text{ meter}$$

$$\lambda = \frac{12.27}{\sqrt{V}} \text{ Å}$$

If the electrons are accelerated by a potential difference 100 volt.

$$\lambda = 1.227 \text{ Å} \quad (\text{which is same as the wavelength of } x\text{-rays})$$

But both are quite different from each other in nature.

28-08-18

* **Uncertainty Principle.**

→ Heisenberg's uncertainty principle.

Uncertainty Principle is the direct consequence of the dual nature of matter. According to classical mechanics, a moving particle has a definite momentum and occupies definite positions in space, and it is possible to determine both its position and momentum (velocity). The above view for simultaneous determination of position and velocity is applicable for object of

Teacher's Signature.....

appreciable size but does not hold for the particles of atomic dimensions.

In quantum mechanism a particle is described by a wave packet, which represents all about particle and moves with the group velocity. The particle may be found anywhere within the wave packet. This means that position of the particle is uncertain within the limit of the wave packet. The another fact of wave packet is that it has a velocity spread and hence there is uncertainty about the velocity or momentum of the particle. From the above logic it is clear that it is impossible to know where within the wave packet the particle is and what its exact velocity or momentum. In conclusion we can say that it is impossible to determine simultaneously both the position and momentum or velocity of particle.

Heisenberg's uncertainty principle states that product of uncertainty in determining the position and momentum of the particle is approximately equal to a number of the order of \hbar .

\hbar , where $\hbar = \frac{h}{2\pi}$ ①

i.e., $\Delta p \cdot \Delta q \approx \hbar$

Δp = Uncertainty in determining the momentum.

Teacher's Signature.....

Δq = uncertainty in determining the position of the particle.

Thus the smaller the value of Δq , larger the value of Δp i.e., more certain the position. i.e., larger the value of Δp . i.e., less certain about the position of momentum or vice versa.

This relation shows that both the position and momentum of the particle accurately.

This relation hold could for all canonically conjugate physical quantities like position and momentum, energy and time, angular momentum and angle etc. whose product has unit of joule second.

Thus if ΔE uncertainty in determining the energy.

Δt uncertainty in determining the time

ΔJ uncertainty in determining the angular momentum.

$\Delta \theta$ uncertainty in determining the angle.

Then we must have,

$$\Delta E \cdot \Delta t \asymp h$$

$$\Delta J \cdot \Delta \theta \asymp h$$

The uncertainty principle can also be stated as follows:-

Teacher's Signature.....

The product of the uncertainties in determining the position and momentum of the particle can never be smaller than the number of the order of $\frac{\hbar}{2}$.

Hence eqⁿ (1) can also be written as

$$\Delta p \cdot \Delta q \geq \frac{\hbar}{2}$$

similarly $\Delta E \cdot \Delta t \geq \frac{\hbar}{2}$. and $\Delta J \cdot \Delta \theta \geq \frac{\hbar}{2}$

4/09/18

Elementary idea of dia-para and ferro magnetic substances and their Comparative Study :-

i) Dia-magnetic material :- Dia-magnetic substances are those which are repelled by magnet and when placed in non-uniform magnetic field move from stronger to weaker part of field.

Eg. :- Bi, Au, Cu, H₂, Sb, H₂O, P. etc.

ii). Para-magnetic material :- para-magnetic substances are those which are attracted by magnet & when placed in a non-uniform magnetic field move from weaker to stronger part of field.

Eg. :- Mn, Pt, Na, O₂ etc.

3). Ferro-magnetic Substances : Ferro-magnetic substances are those which are attracted by magnets and can be also magnetised.
Eg: Co, Fe, Ni etc.

* Ferro-magnetic material show all the properties of para-magnetic material to much greater degree.

Comparative Study b/w dia-para and Ferro-magnetic materials :-

i) Dia-magnetic materials:-

a). There is no permanent atomic magnetic dipole moment, these materials are repelled by magnetic field.

b). Induced dipole moment always oppose the applied field \Rightarrow Susceptibility.

c). $\chi_{ii} (\chi < 0)$ is practically independent of temp (T) and magnetic field.

d). Magnetization (I) varies linearly with external magnetic field.

2). Para-magnetic \rightarrow

a). These material causes permanent atomic dipole.

b). In the absence of external field the dipoles are randomly oriented and there is no net magnetization. The presence of external field causes alignment of dipole and hence magnetization.

c). (χ) is positive fraction. (χ) varies inversely with Temp (T). but independent (H) magnetizing force.

d). Magnetization varies with external field.

3). Ferro-magnetic \rightarrow

a). It contains permanent atomic dipoles which interact strongly with each other and make cause spontaneous magnetization with in a single part even in the absence of external field. They are strongly attracted by magnetic field.

b). A strong external field can cause large magnetization.

$\sigma \propto H^{2/3}$ and depends on temp (T) and according to Curie's law $\sigma \propto T^{-1}$.
 Hence σ is function of (H) and T .
 σ is Curie temp.

d) For each ferro-magnetic material there is a particular temp called Curie temp, where it's spin favours magnetization for $T < 0$, if $T > 0$ ferromagnetic material becomes paramagnetic.

* Some definitions

i) Intensity of magnetization (I): The ratio of pole strength and cross-sectional area of magnet is called Intensity of magnetization.

$$I = \frac{m}{a} = \frac{\phi l m}{\phi l a}$$

{ ϕl = magnetic length.

$$I = \frac{m}{V} \text{ (magnetic moment)}$$

V (volume)

Hence magnetic moment per unit volume of the magnet is also called Intensity of magnetization.

⇒ Permeability (μ) is

The ratio b/w magnetic induction to the magnetizing force (H). is called permeability.

$$\mu = \frac{B}{H}$$

$$\left\{ \begin{array}{l} \mu = \mu_r \mu_0 \\ \text{for air} \\ \mu_r = 1 \end{array} \right.$$

$$B = \mu H$$

$$B = \mu_r \mu_0 H$$

$$\mu_{air} = \mu_0$$

unit of (μ) permeability in S.I system :
Henry / m

3). Susceptibility (χ) : The ratio b/w intensity of magnetization (I) to the magnetizing force (H). is called susceptibility. The susceptibility of substances show the ability of a substance has to how easily and how much more magnetization it can hold.

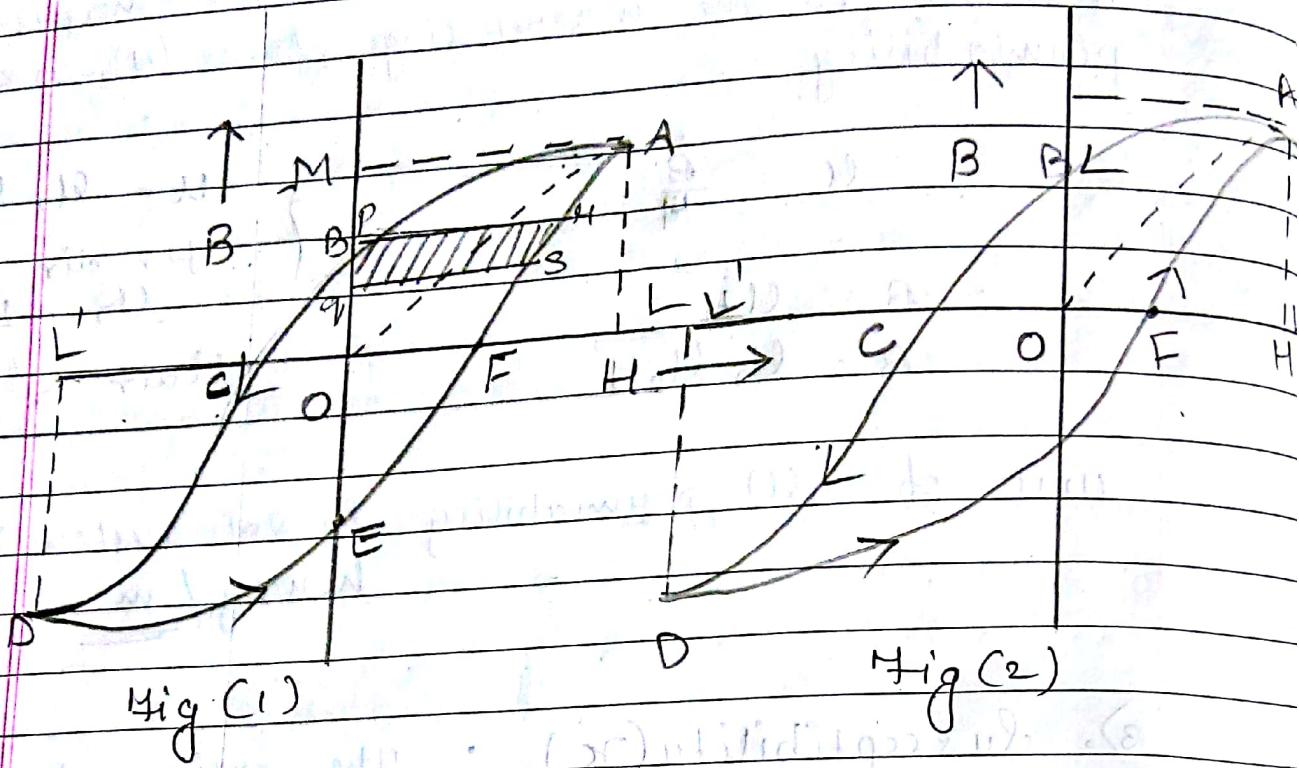
$$\chi_{para} = \frac{I}{H}$$

- * Soft iron is more susceptible than steel.
- * It has no unit. Since it is the ratio of two similar quantities.

END

11/09/18

Hysteresis :-



A Specimen of iron (ferromagnetic material) be magnetised by passing an electric current through it.

If the value of current increase the magnitude of the magnetising 'H' increased

and the magnetic induction B_B also increases. The graph between B and H is shown below fig (1). The analysis of graph indicate various informations between the B_H and H values and all the diagram (1).

Teacher's Signature.....

Hysteresis:- The lagging of magnitude of induction behind the magnetising force producing it when a specimen of iron is taken through a cycle of magnetisation is called Hysteresis.

Hysteresis loop :- The variation of B with H from 0 to a maxm value in one direction and then back through zero to a maxm value in the opposite direc. and finally back again through zero to the first maximum value is called Hysteresis loop.

loss of energy per cycle in (B-H)

consider a graph between B along y -axis and H along x -axis is similar to the nature of graph between I along y -axis and H along x -axis as shown in fig(-2). Let ABCDEF A is a complete cycle of magnetisation. Let PQ be the small step in the process of magnetisation in which B increased by a small amount dB .

\therefore So work done per unit volume = HdB .

Date			
Page No.			

$$HdB = \text{area PQRS} \quad \text{unit: } \text{Am}^{-1}$$

- (1) When the magnetising force H increases from O_1 to O_2 , B changes from OE to OM .
- ∴ Work done on the specimen per unit volume in increasing B from OE to OM
- $$= \mu_0 \int_{OE}^{OM} H dB = \text{area EFAMBOE}$$

- (2) When H increases from O_2 to zero, B decreases from OM to OB .
- ∴ Work done by the specimen per unit volume = $\int_{OM}^{OB} H dB = \text{area AMBA}$

Work done by the specimen = $\text{area AMBA} - \text{area EFAMBOE}$

∴ Required deflux B is given by H from given χ & θ . Position all of periphery with work done T measured