

Quantitative trading strategies:

Simplest form of trading:

→ Buy low sell high



Why it might not work always?

- 1) Stock may go down
- 2) Stock may not go up or not go down.

What are the prerequisites for it to work.

- You may win ——— ①
- You may loose ——— ②
- You may waste time ——— ③

① ———→ happens then what  
 ———→ How far it will go up  
 ———→ Is it right time to sell  
 ———→ What if market suddenly goes down

② You ~~may~~ loose

——→ Stop loss

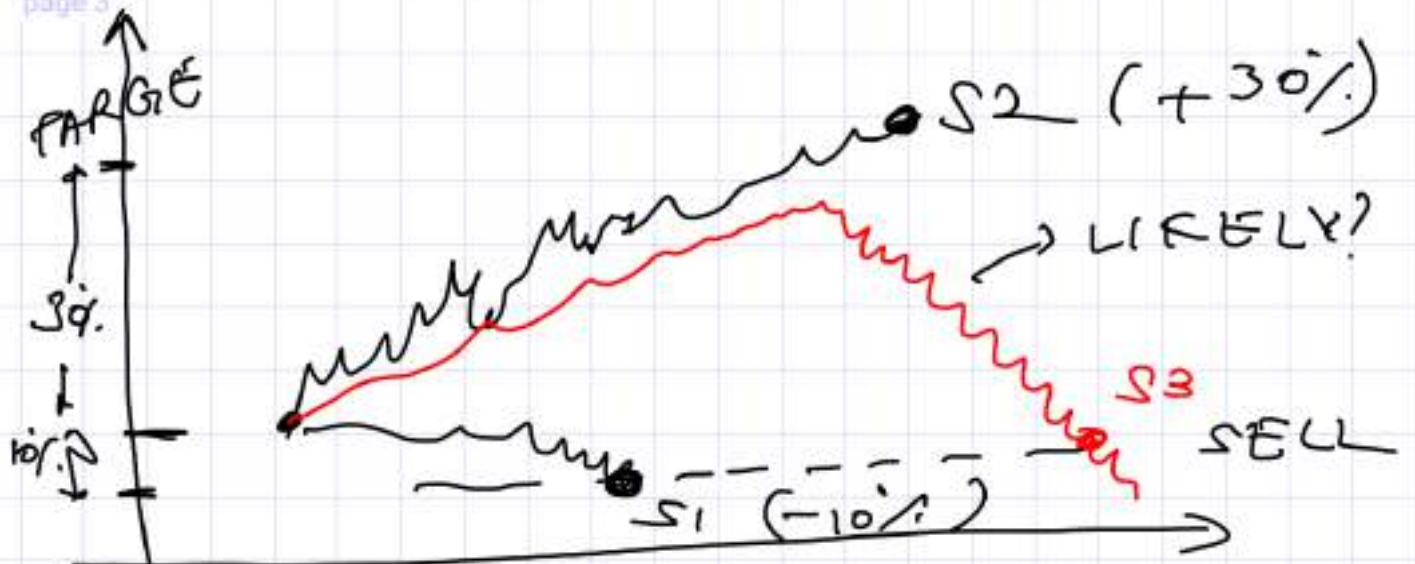
——→

③ Time stop loss

←————→

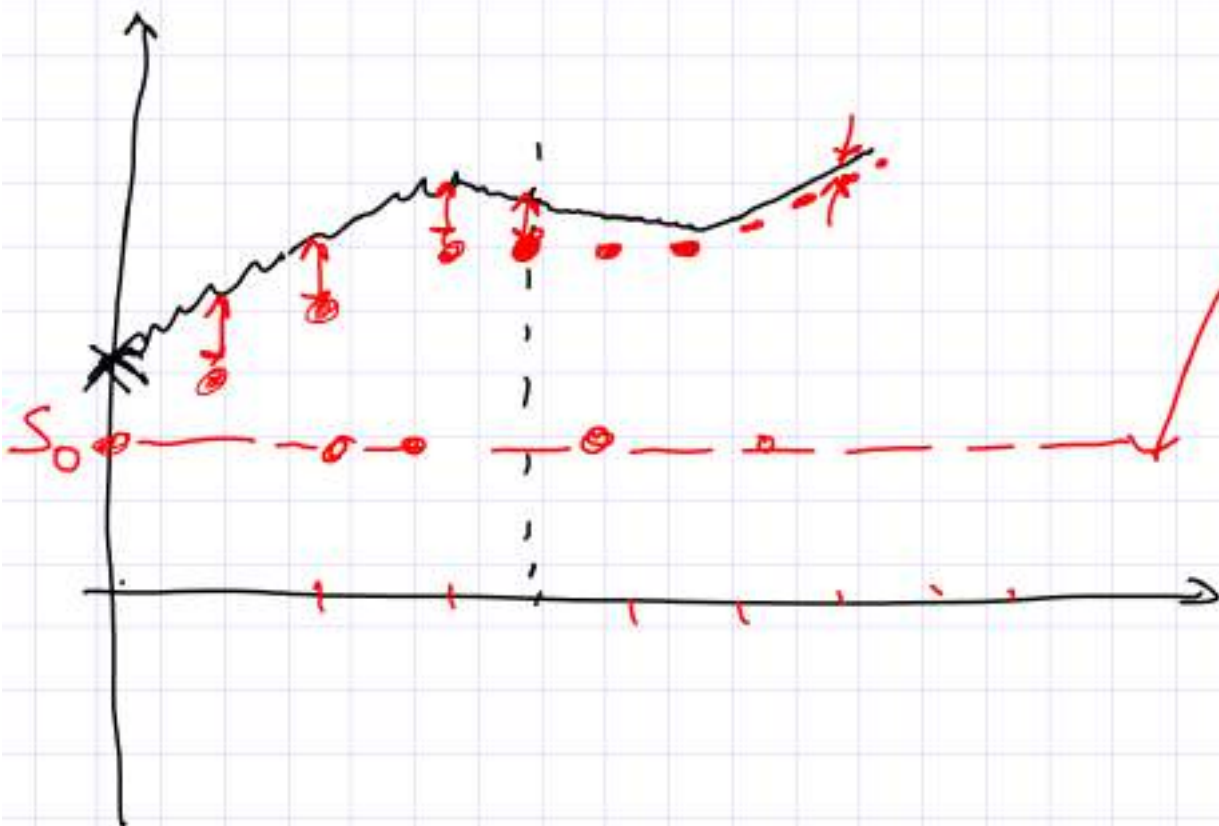
1) Stock will go up.

2) Stop loss.      3) Target



Trailing stop loss  $S_0$

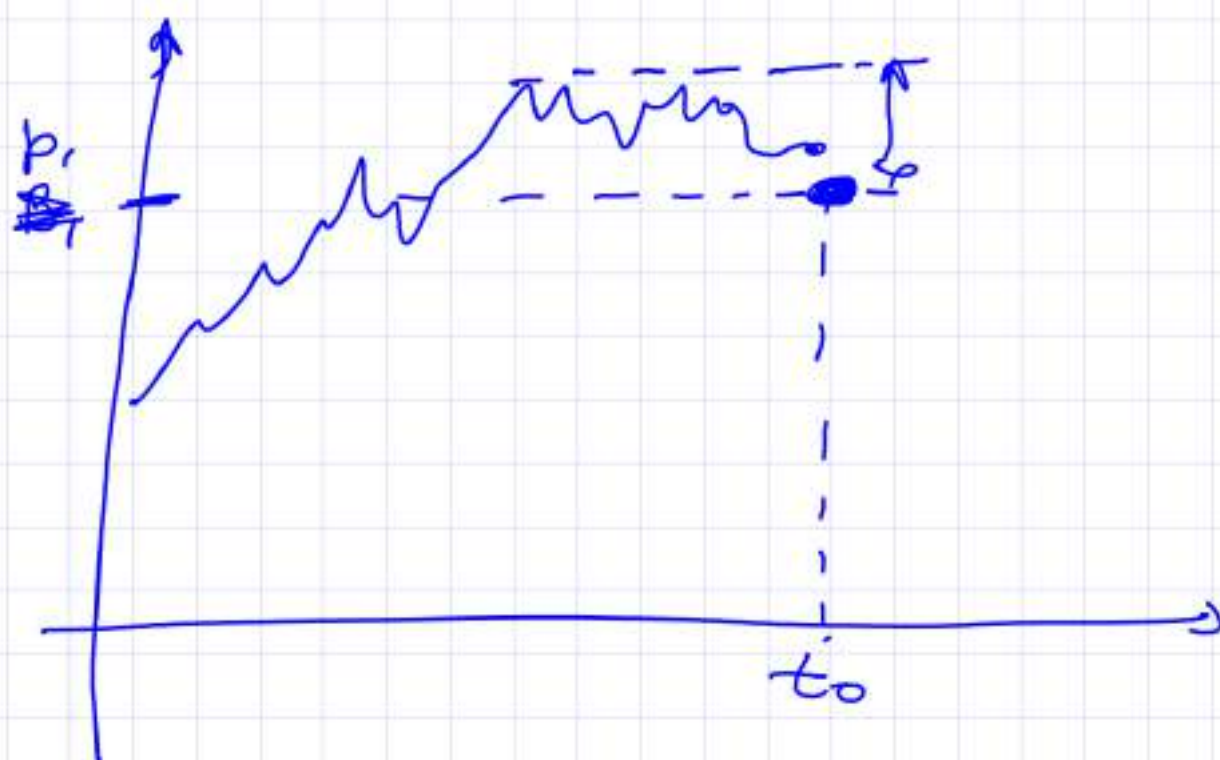
$S(B(t))$



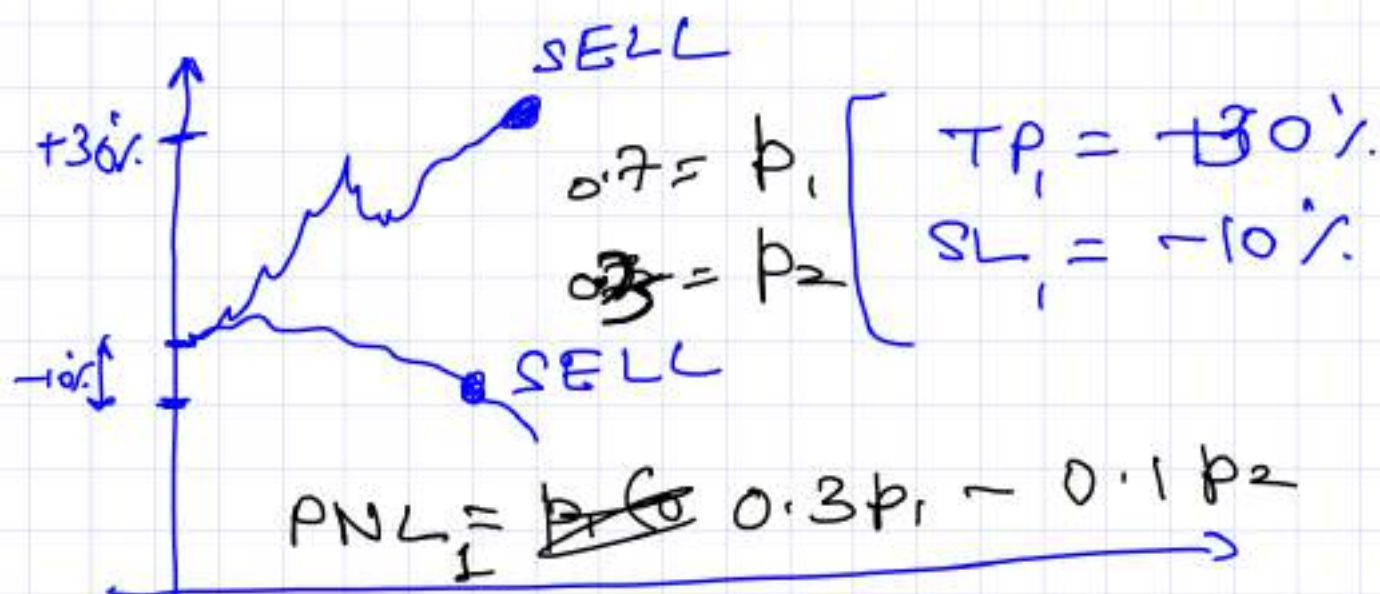




Trailing stop loss.



$$SL(t_0) = p_1$$

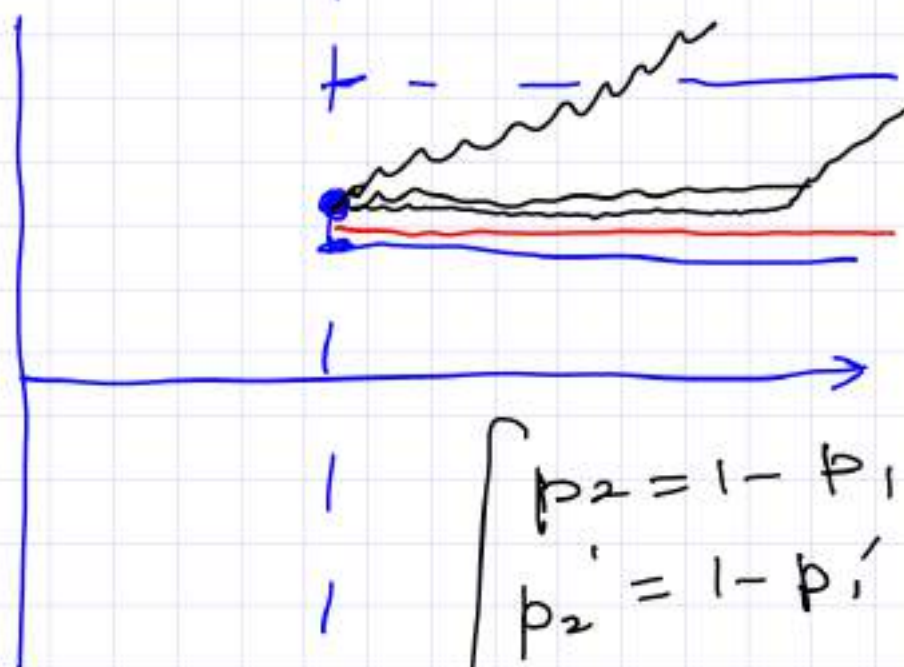


$p_1 \neq p_2$   
 $= p_1' + p_2' = 1$

$p_1'$   
 $p_2'$

$\left[ \begin{array}{l} TP_2 = 30\% \\ SL_2 = -5\% \end{array} \right.$

$PNL_2 = 0.3 p_1' - 0.05 p_2'$



Unless

$\cancel{p_2' > 2 p_1}$

$0.3 p_1 - 0.1 p_2 < 0.3 p_1' - 0.05 p_2'$

$$0.3 p_1 - 0.1(1-p_1) < 0.3 p'_1 - 0.05(1-p'_1)$$

$$0.4 p_1 - 0.1 < 0.25 p'_1 - 0.05$$

$$0.4 p_1 \leq 0.25 p'_1 + 0.05$$

$$0.4(1-p_2) < 0.25(1-p'_2) + 0.05$$

$$0.4 - 0.4 p_2 < 0.25 + 0.05 - 0.25 p'_2$$

$$0.1 - 0.4 p_2 < 0.3 - 0.25 p'_2$$

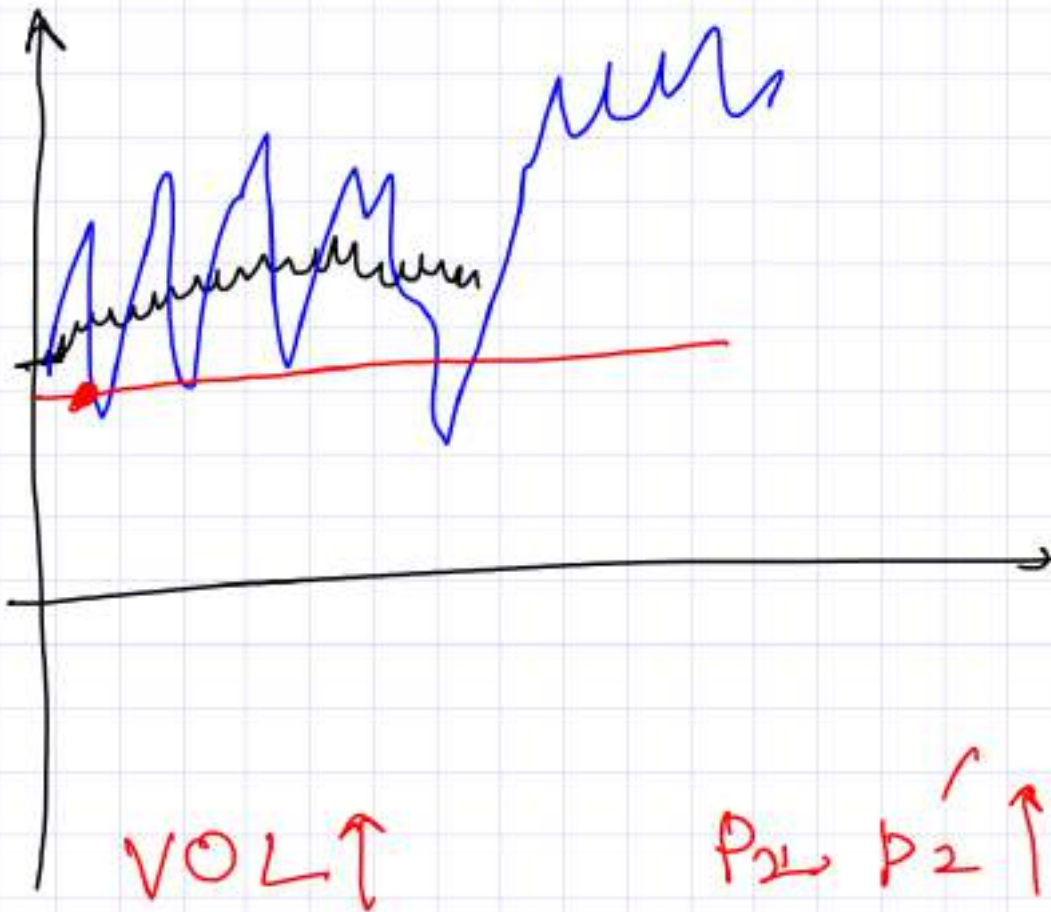
$$0.1 + 0.25 p'_2 < 0.4 p_2$$

$$0.25 p'_2 < 0.4 p_2 - 0.1$$

$$p'_2 < 4(0.4 p_2 - 0.1)$$

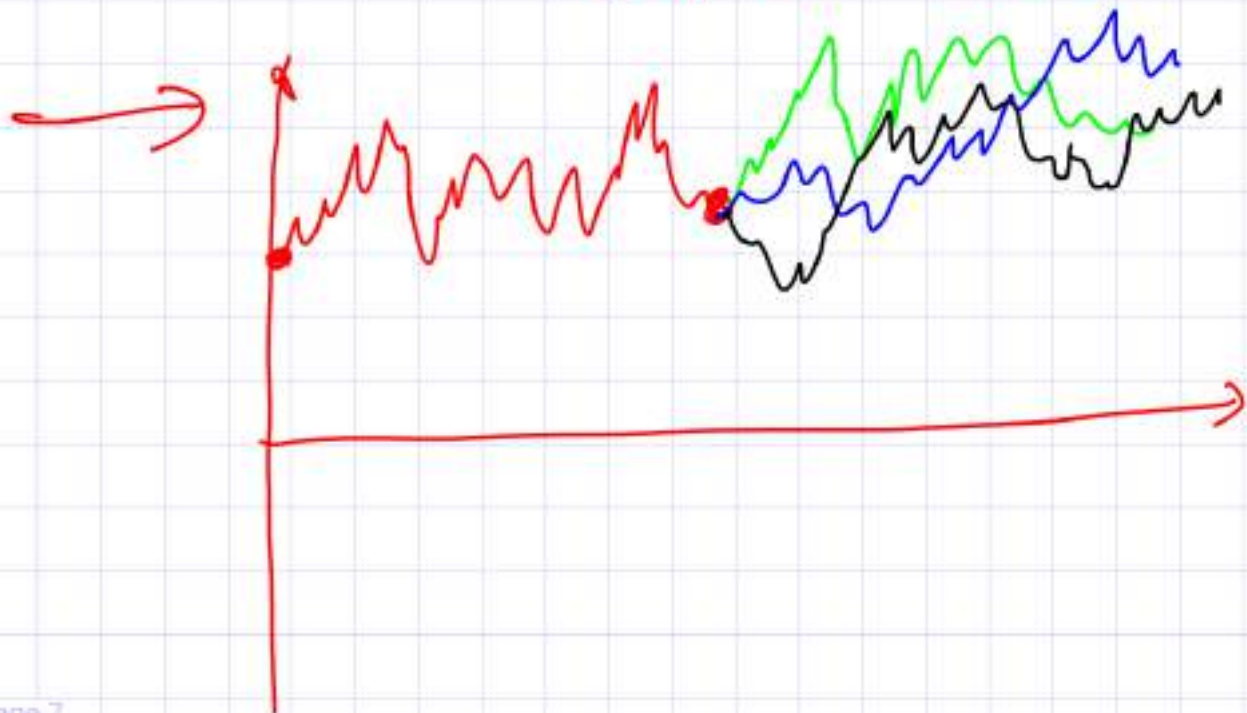
$$p'_2 < 1.6 p_2 - 0.4$$

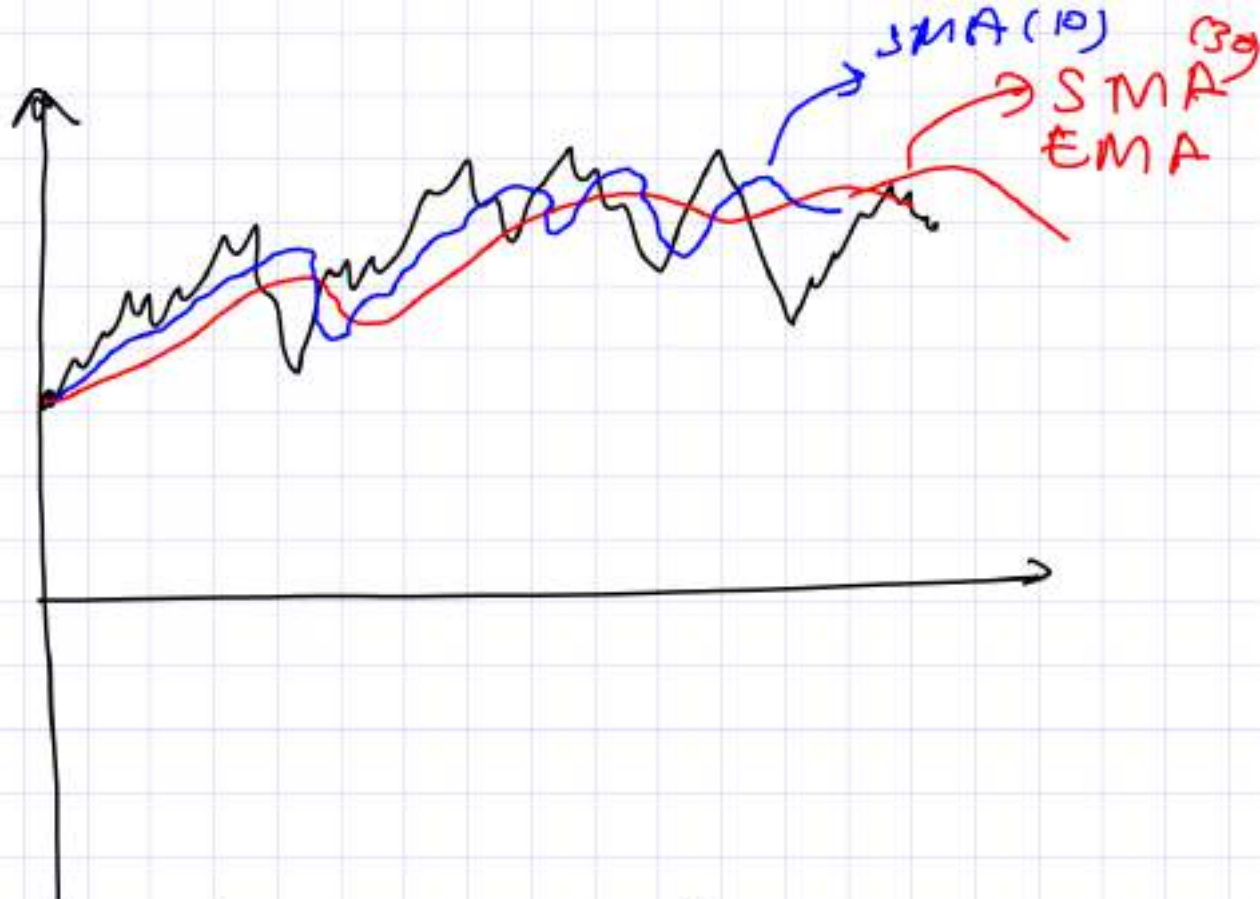




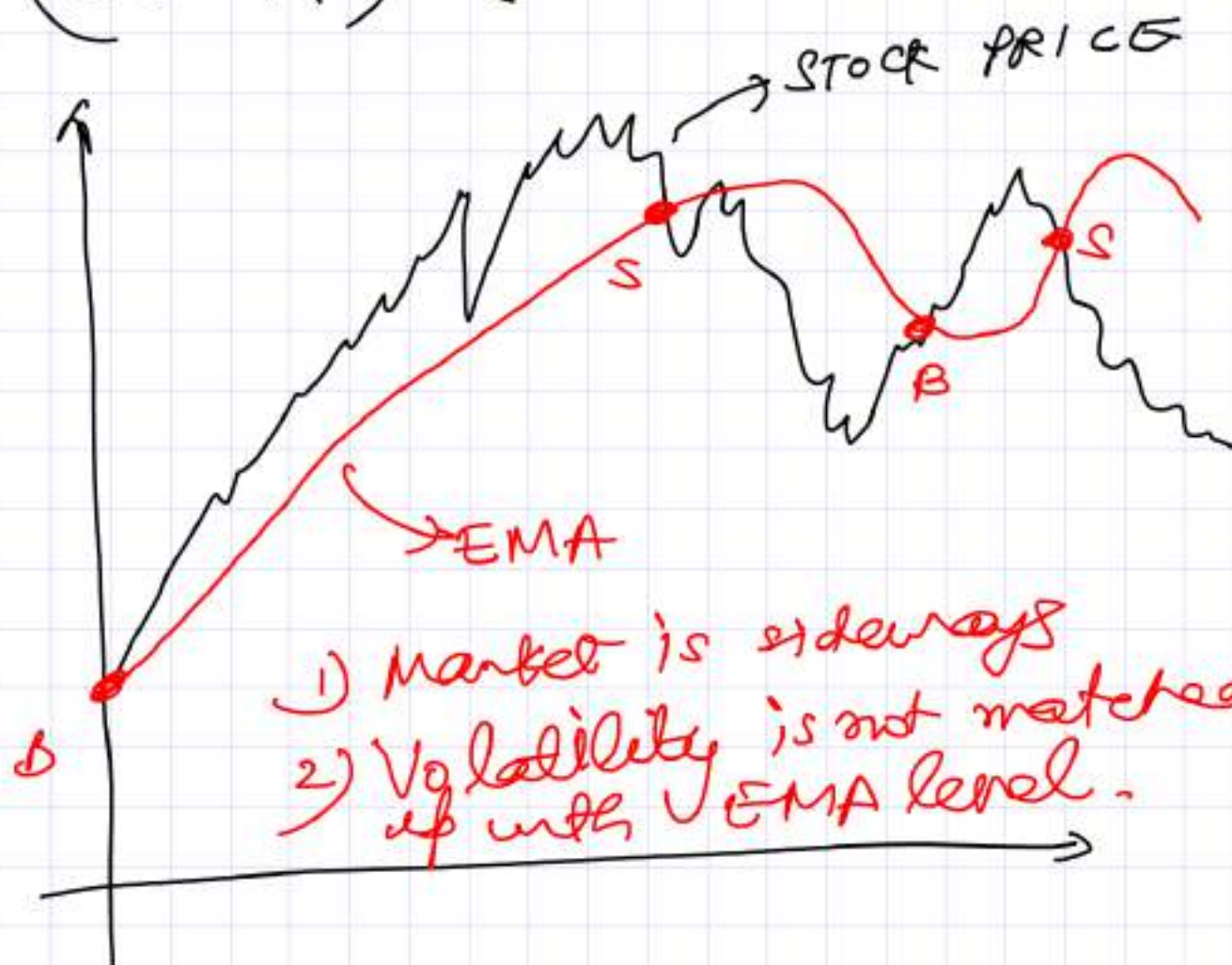
$$P_2' \gg P_2$$

Calculating  $P_1, P_2, P_1', P_2'$   
difficult



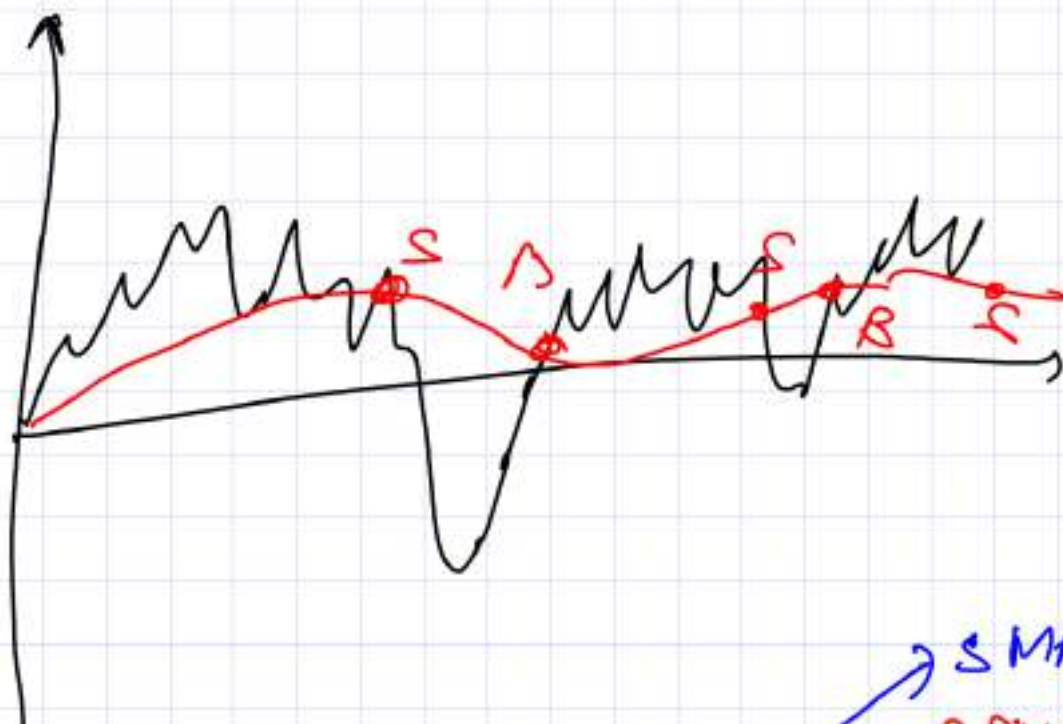


(EMA) (SMA)



RSI





There are Technical analysis books where we can find these strategies

# General book:

① Technical analysis of Financial markets.

— John Murphy

② Encyclopedia of chart patterns

— Bulkowski

[ Bollinger band  
RSI  
MACD

[ Chaikin money flow

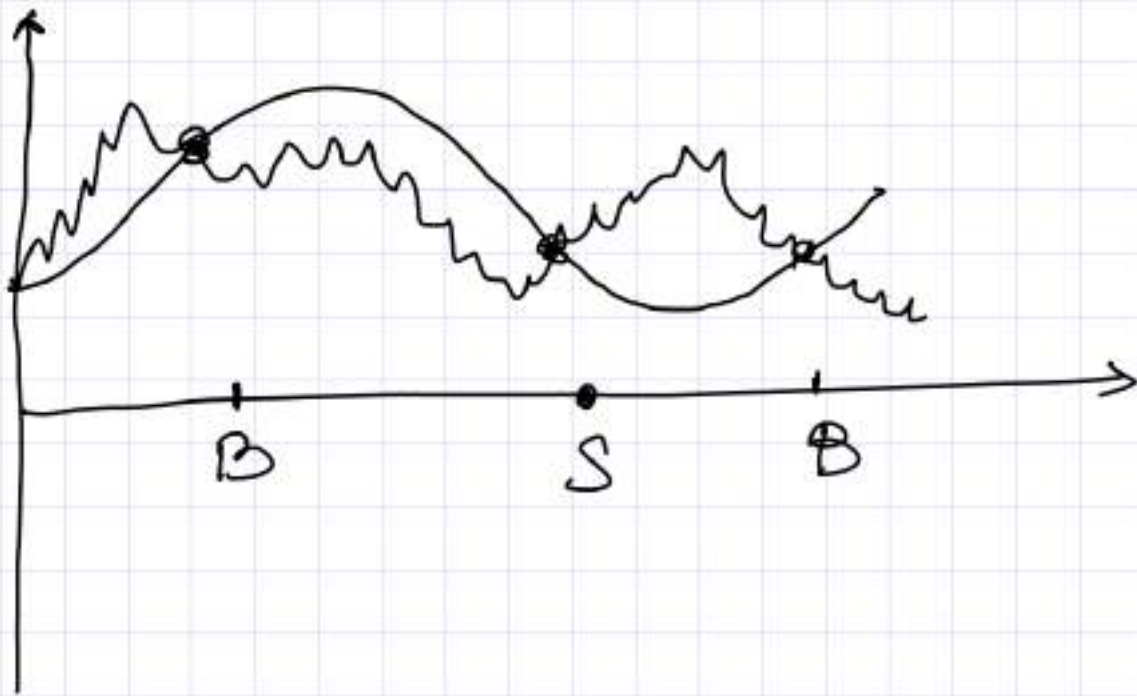
[ VWAP

[ Keltner Channel



[KST (Know Sure thing)]

Directional trading strategies:



[EMA (Exponential moving average)]

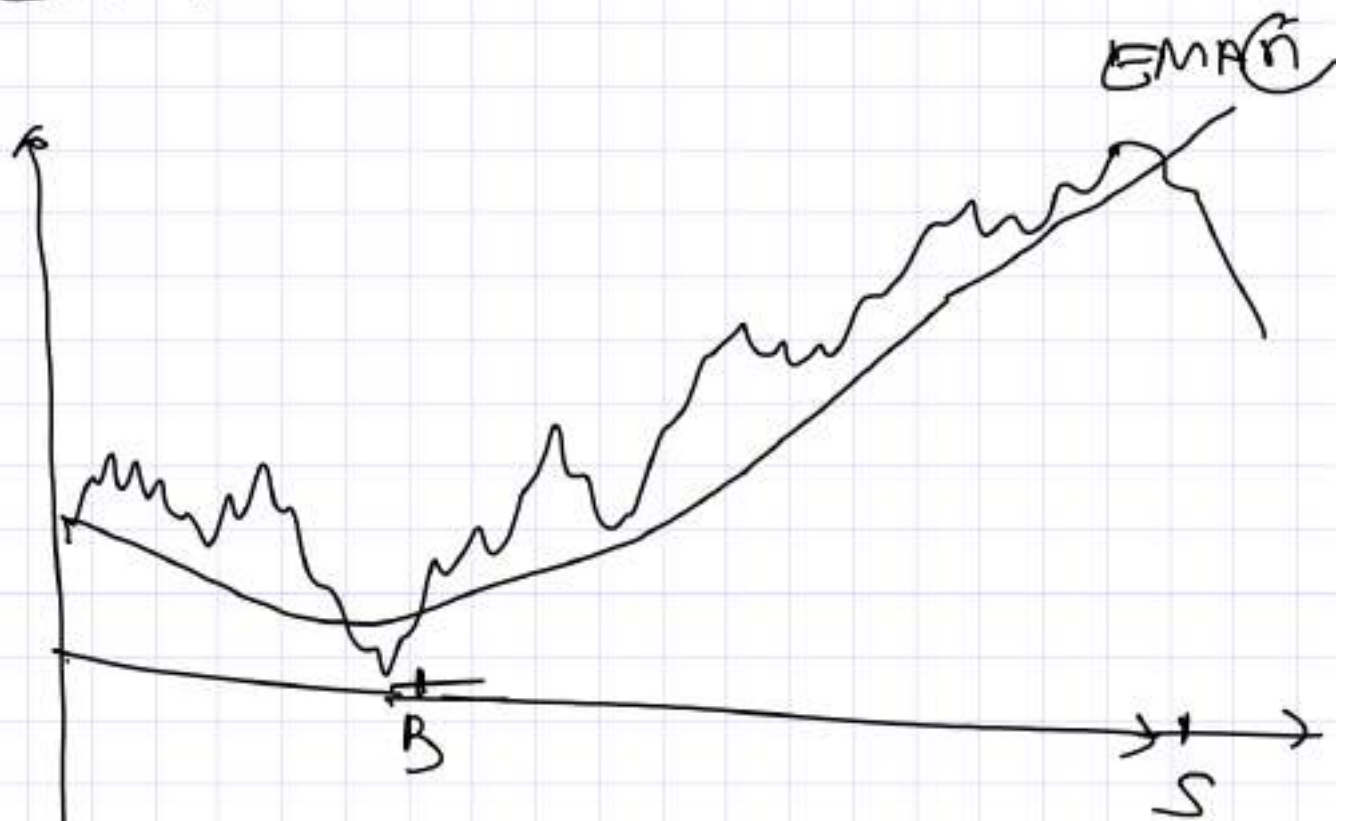
[SMA (Simple moving average)]

~~We can~~

[EMA gives more weightage to latest values.]



## EMA



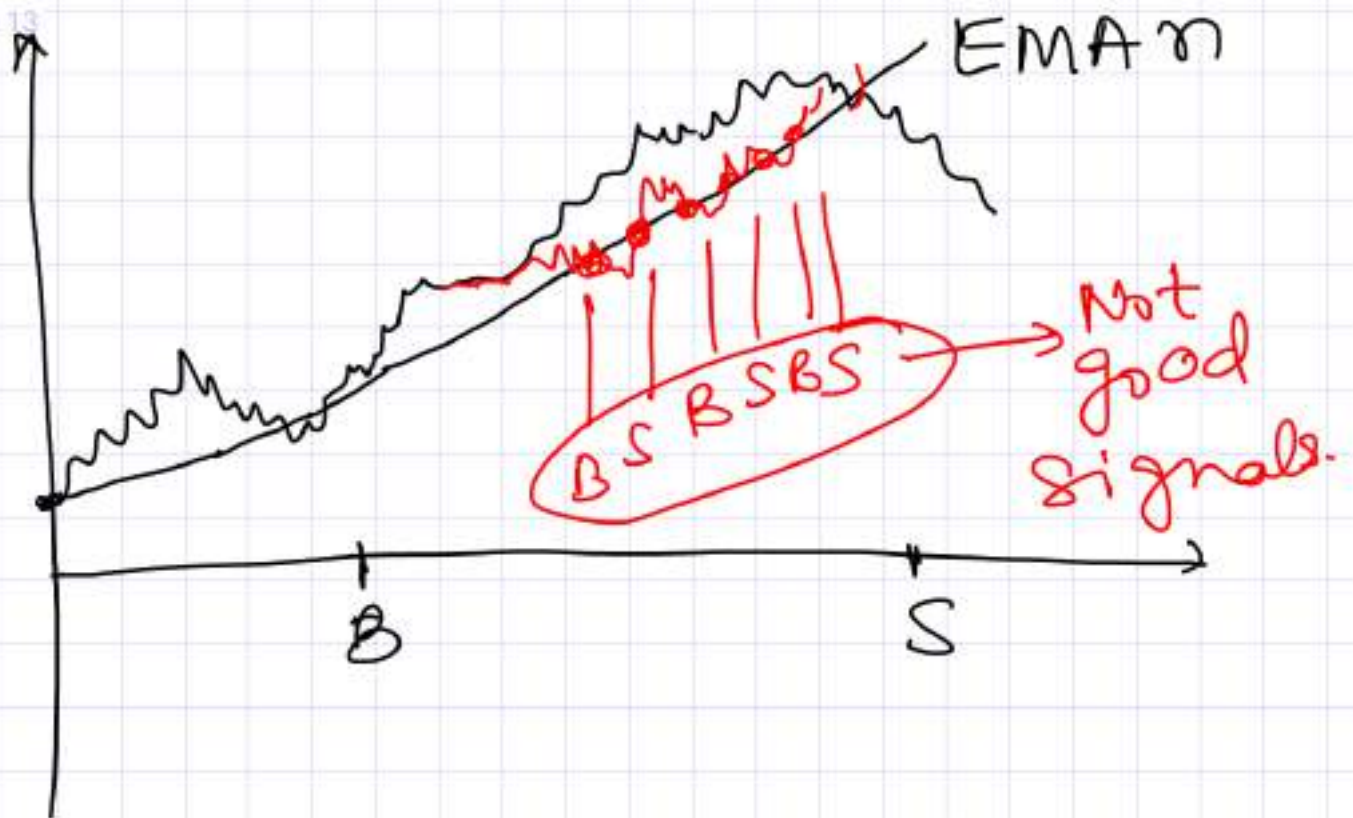
{ EMA 10  
 { EMA 20  
 { EMA 30

Less lag,  
 less smooth

More lag. with  
 stock price,  
 More smooth

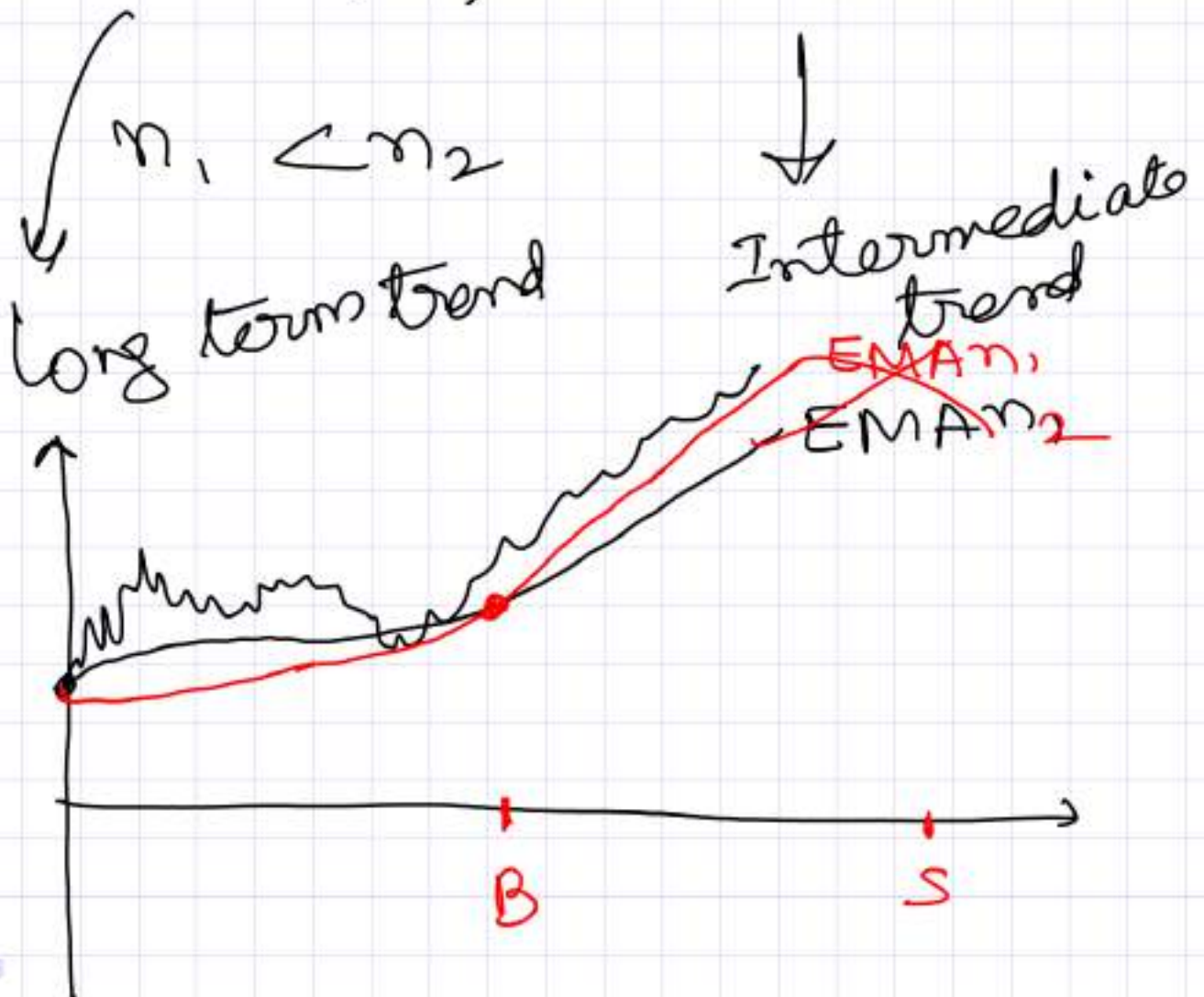
$n$  can be 10 or 20 or 30

[ We take higher values of  
 $n$  when we are tracking  
 a longer term trend.



Then we take two EMA'S

EMA  $n_1$  , EMA  $n_2$



$S \rightarrow \text{When}$

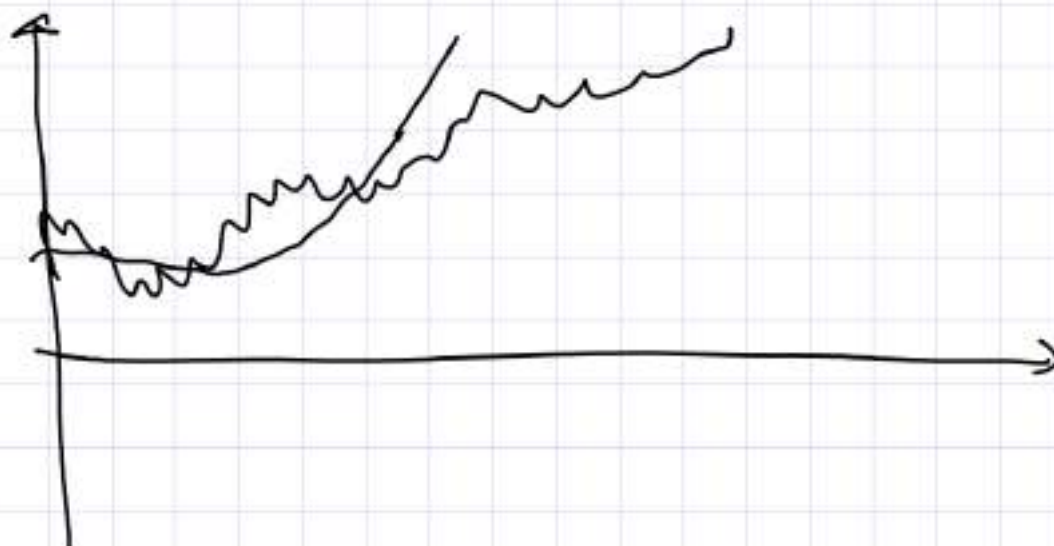
$\left[ \text{EMA } n_1 \text{ crosses EMA } n_2 \right]$   
from above.

$\left[ \text{Intermediate trend} \right]$   
has changed



$\left[ \text{SVM, Linear regression, etc.} \right]$

$\left\{ \text{Machine learning techniques} \right\}$



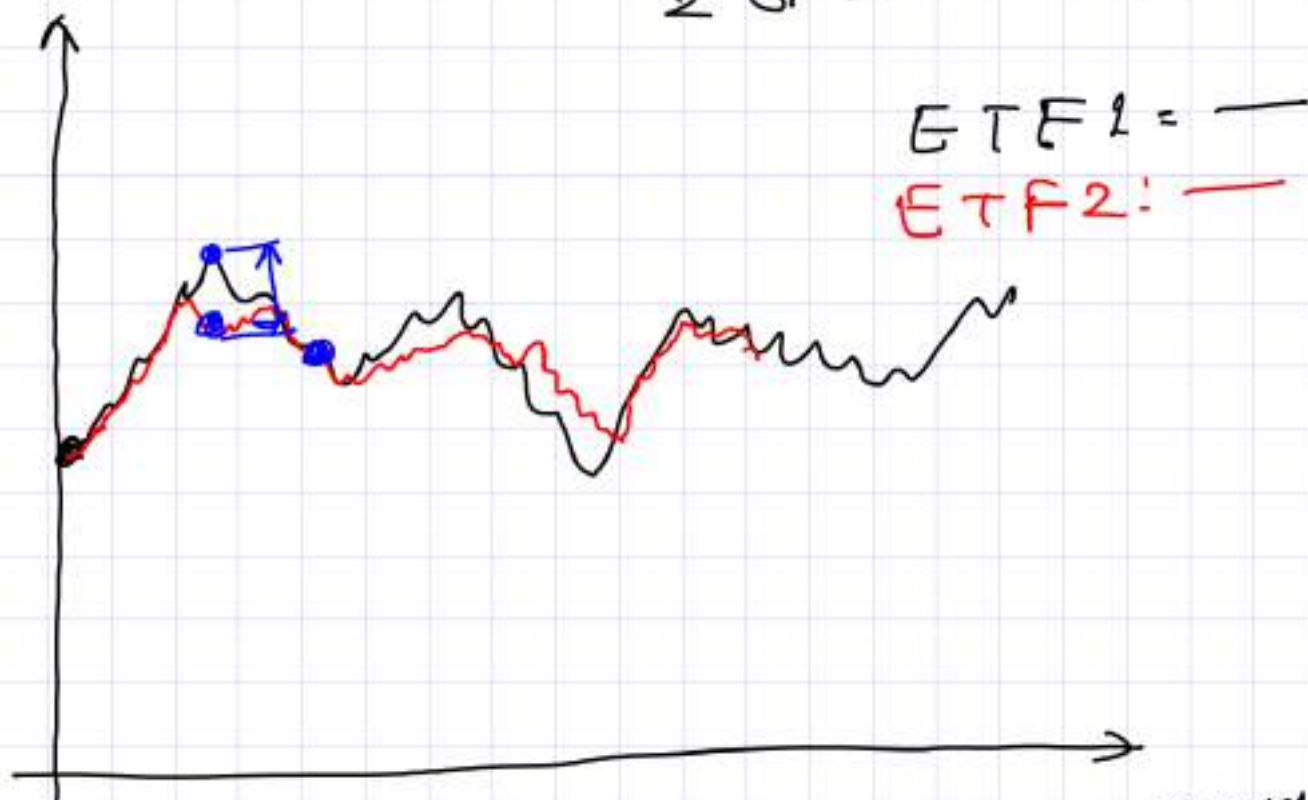


If future predicted value  
is high (low)  $\rightarrow$  we buy (sell)  
we retain our long (short)  
positions

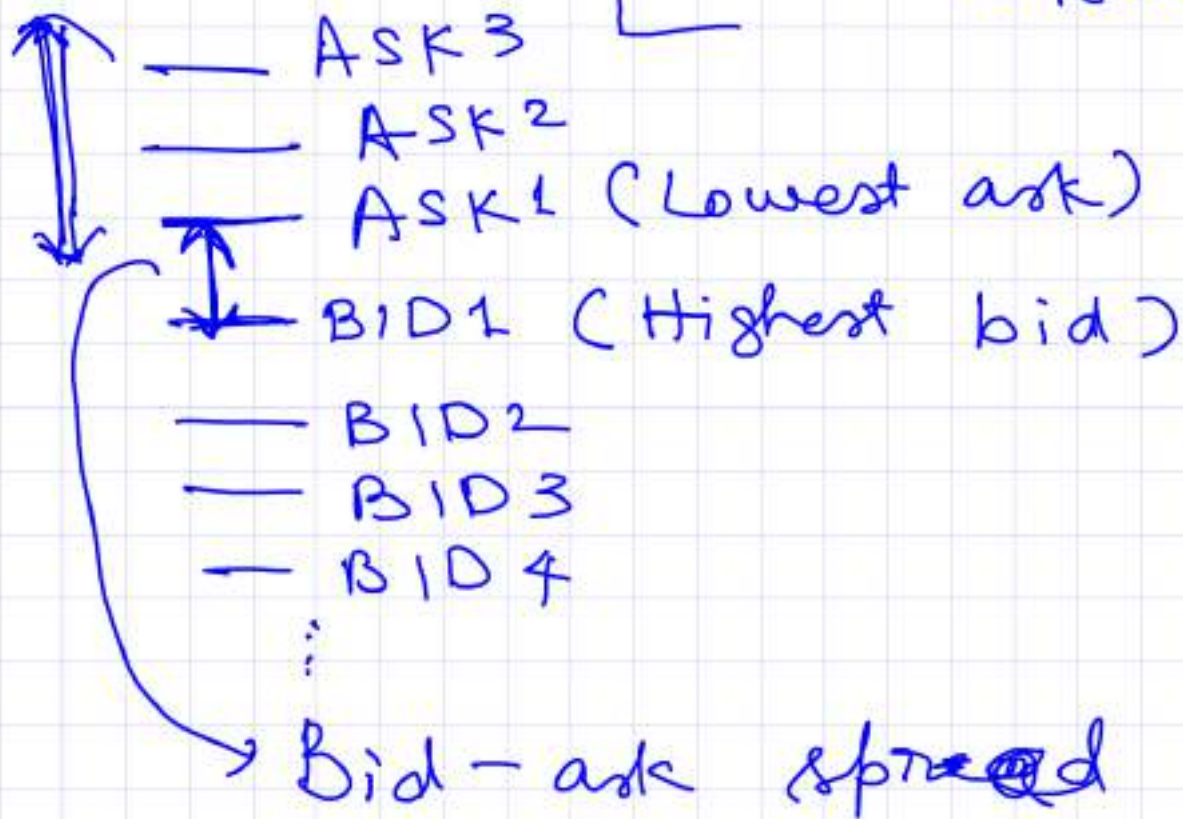
# Arbitrage strategies:

Arbitrage is short term movement of an instrument from its natural position.

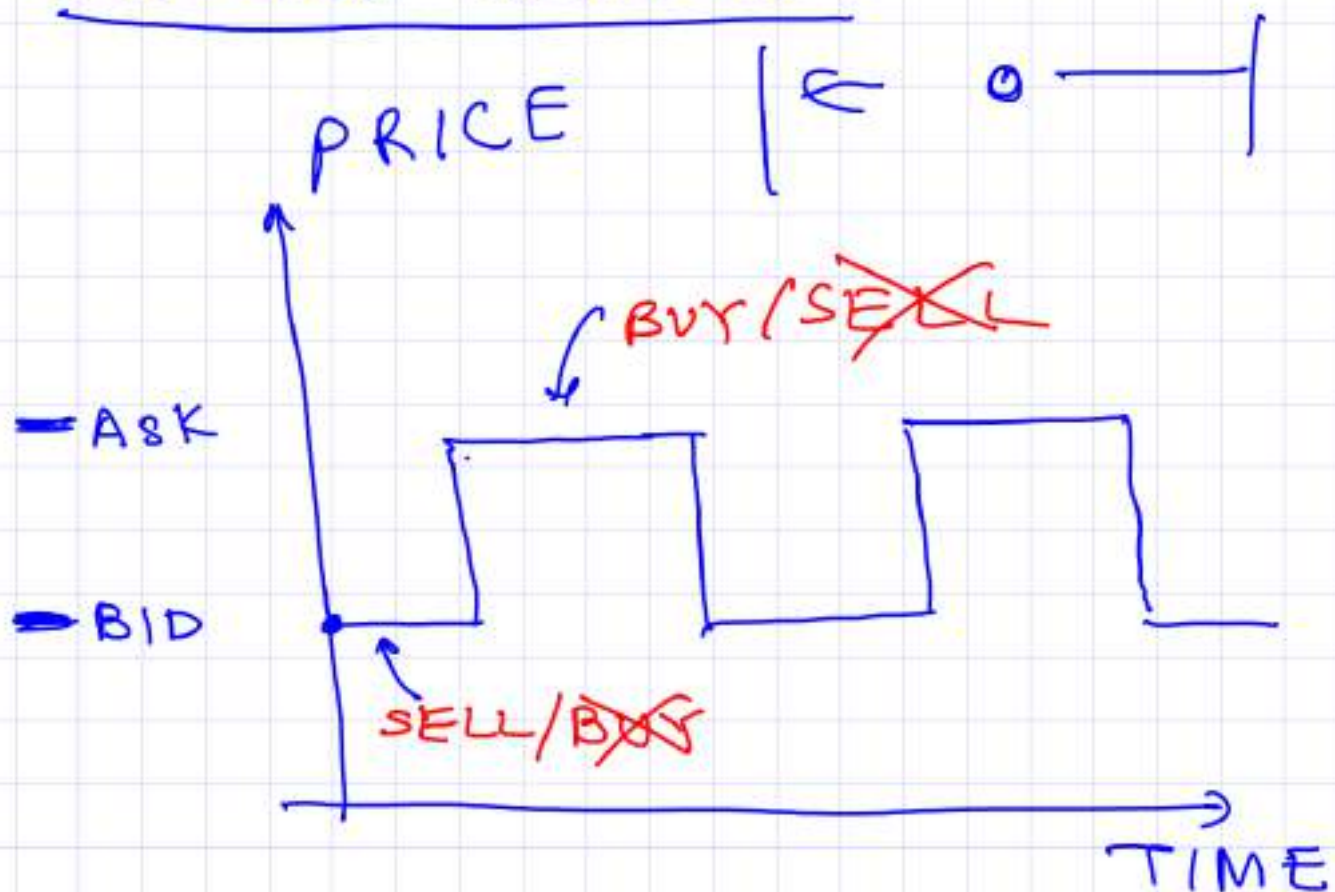
2 GOLD ETFS



Market book: { BID  $\rightarrow$  Price willing to buy  
ASK  $\rightarrow$  Price willing to sell



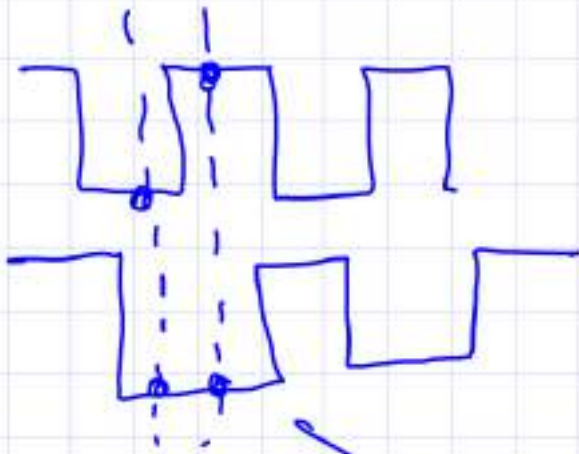
Bid-ask bounce:





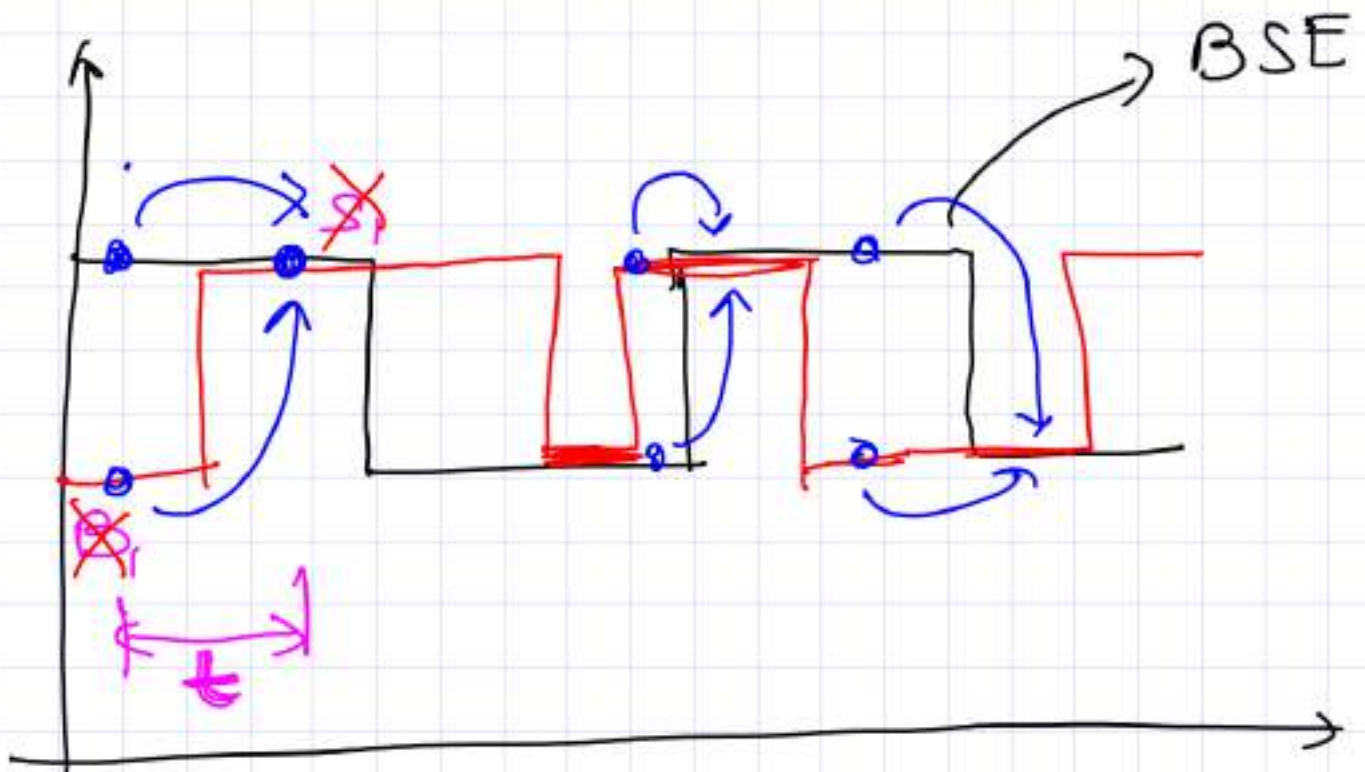
EXCH1

EXCH2



NOT

Arbitrage is possible?



## Index arbitrage:

- ① 2 different versions of 'index' (ETF) running on different exchanges. ~~are~~  
~~causing~~ And there is a price difference in them.
- ② The catch is in modern market  
→ ~~You can~~ The price difference is only for milliseconds.
- ③ Difficult for retail.

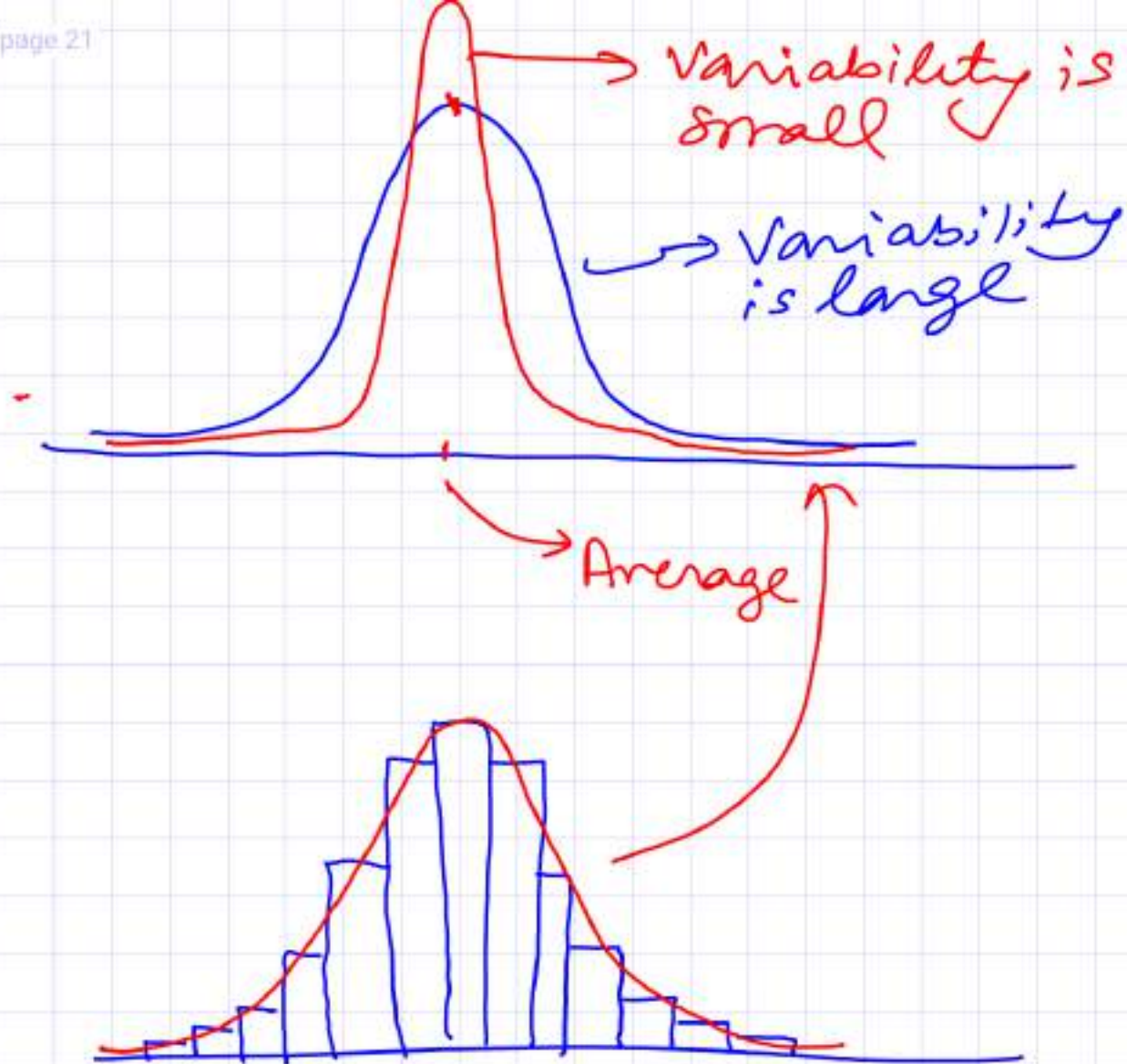


# Spread Arbitrage

- ① For many reasons it is possible ~~to~~ that there is some <sup>anomaly</sup> difference in the price of spot and future contract of the same underlying.
- ② Between two ~~futts~~ futures of different expiries.

(Arbitrage Funds)

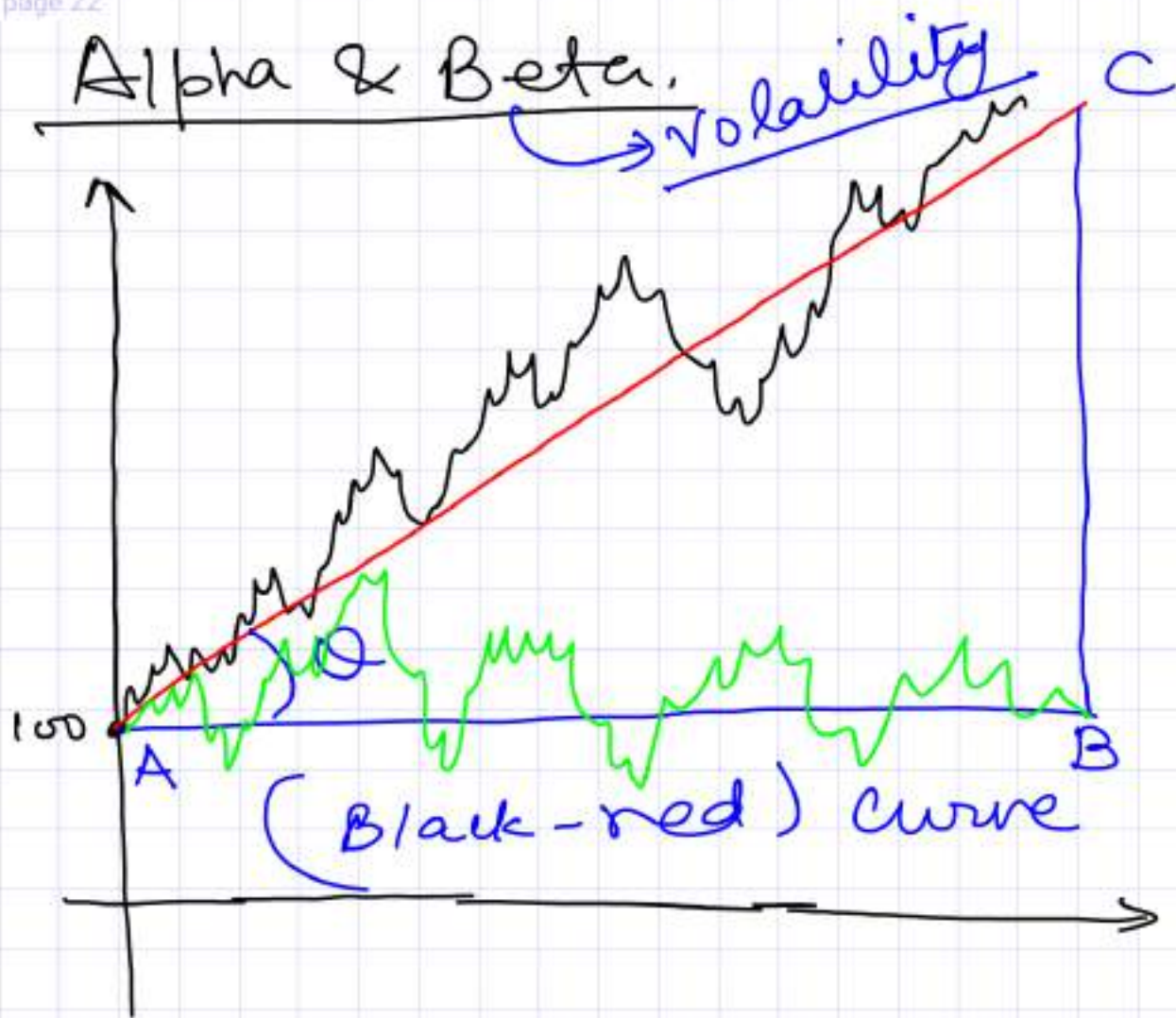




Volatility trading:

What is volatility?

VIX



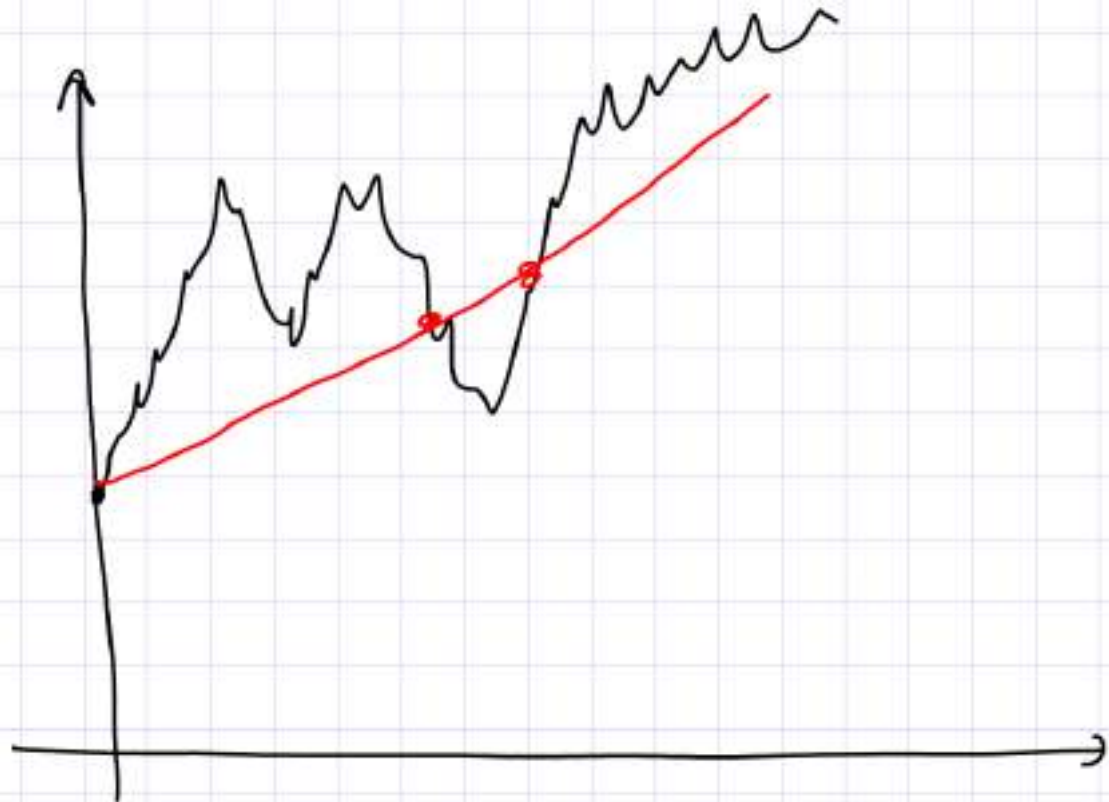
$$\left[ \alpha = \frac{BC}{AB} = \text{Slope of the line} \right. \\ \left. = \tan Q \right]$$

Day to day fluctuations

- ① Calculate day to day stock price movement
- ② Find the average value

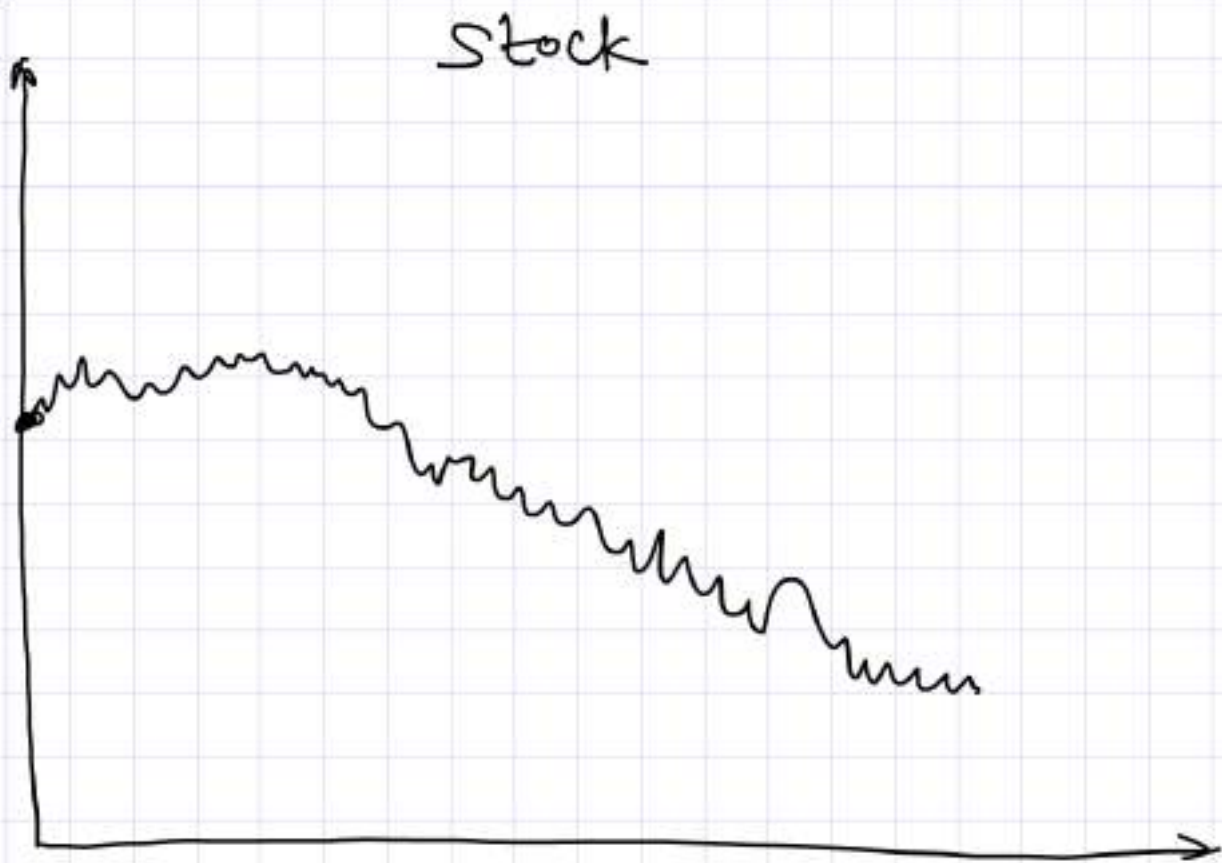






What are options:

John Hull  
Options Futures & Other  
derivatives



Loss:

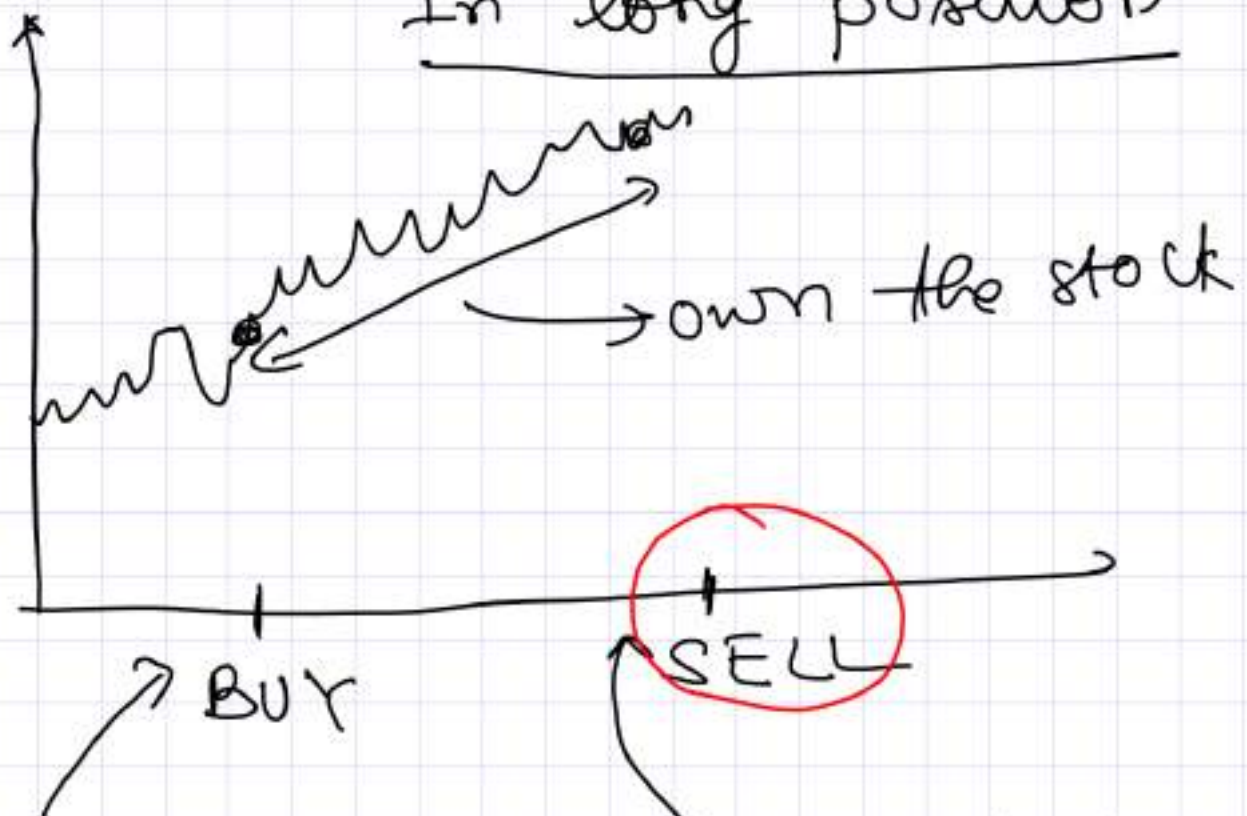
to avoid loss

One possible way is to sell the stock when it is going down.

If you ~~is~~ have a short position in stock, in order to avoid loss when it is going up,

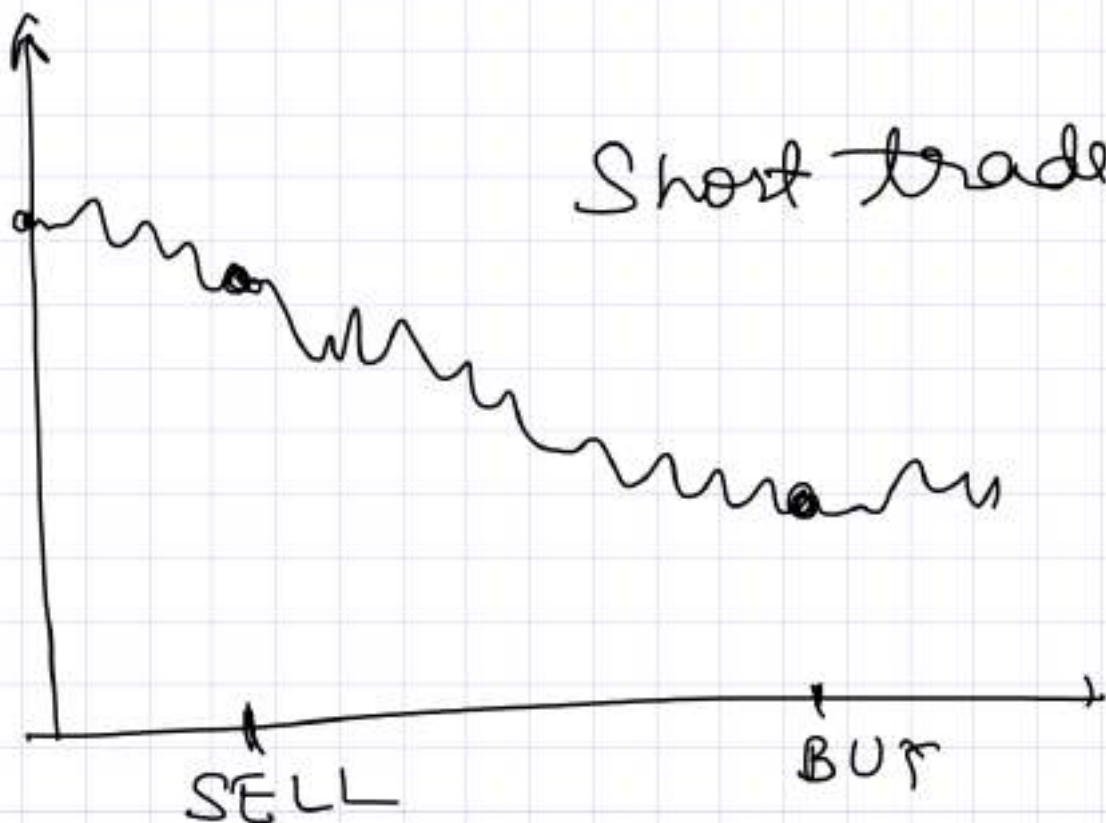
the way is to buy it back

In long position



First leg of the trade

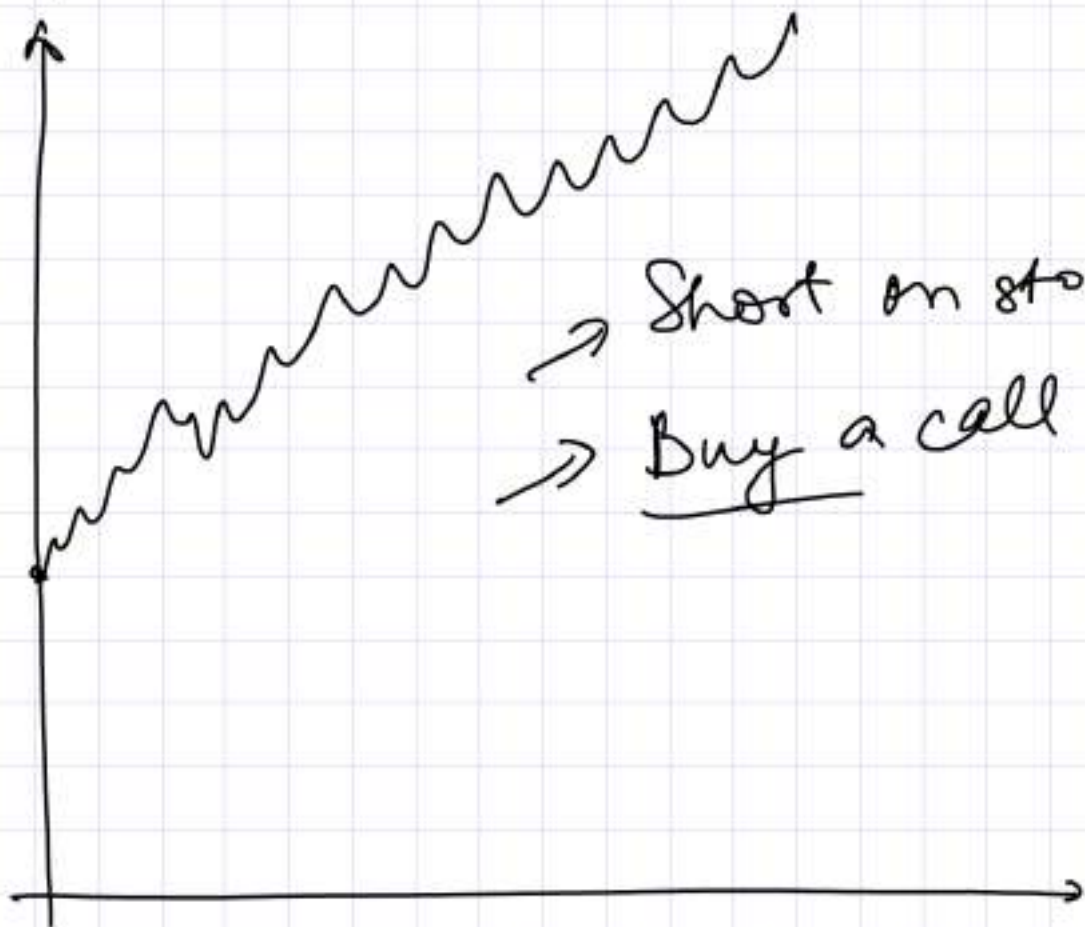
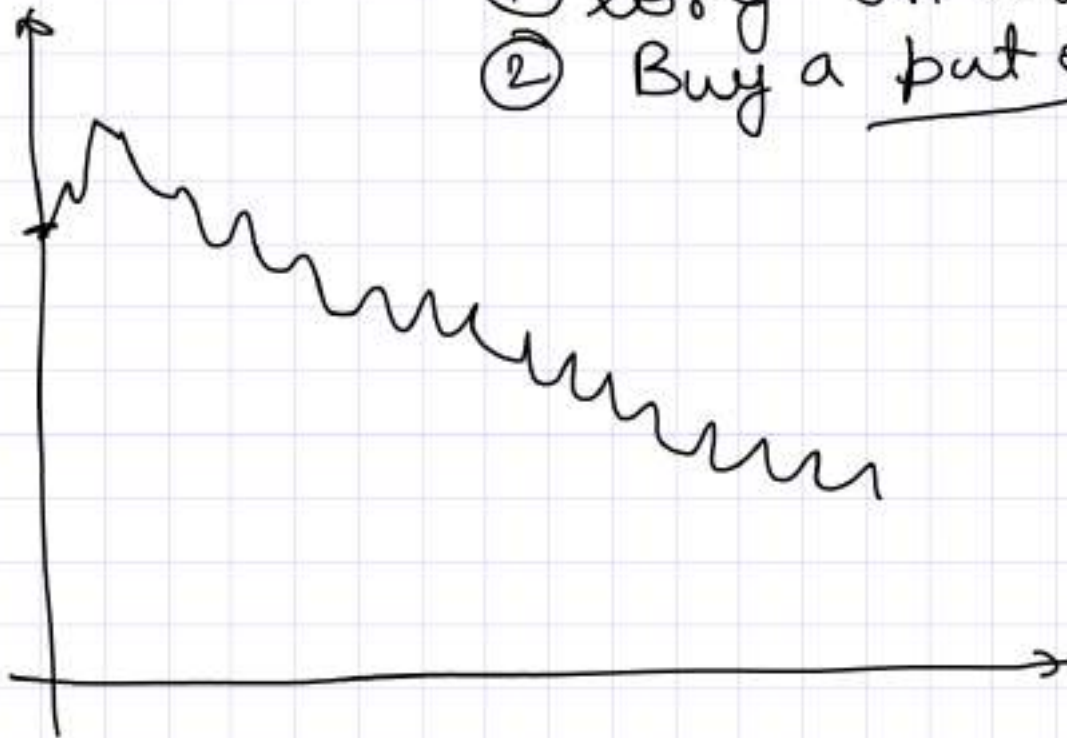
Second leg of the trade





Options are basically hedging mechanism.

- ① long on a stock
- ② Buy a put option



- Short on stock
- Buy a call option

$$S = 120$$

$$K = 100$$

## Call option :

- ① Strike price ( $K$ )
- ② Expiry time ( $T$ )

Call option gives you (a right but not obligation) to

→ Buy <sup>one unit of</sup> the underlying stock at price  $K$  at time  $T$ .

## Put option :

$$S = 70$$

$$K = 80$$

- ① Strike price ( $K$ )
- ② Expiry time ( $T$ )

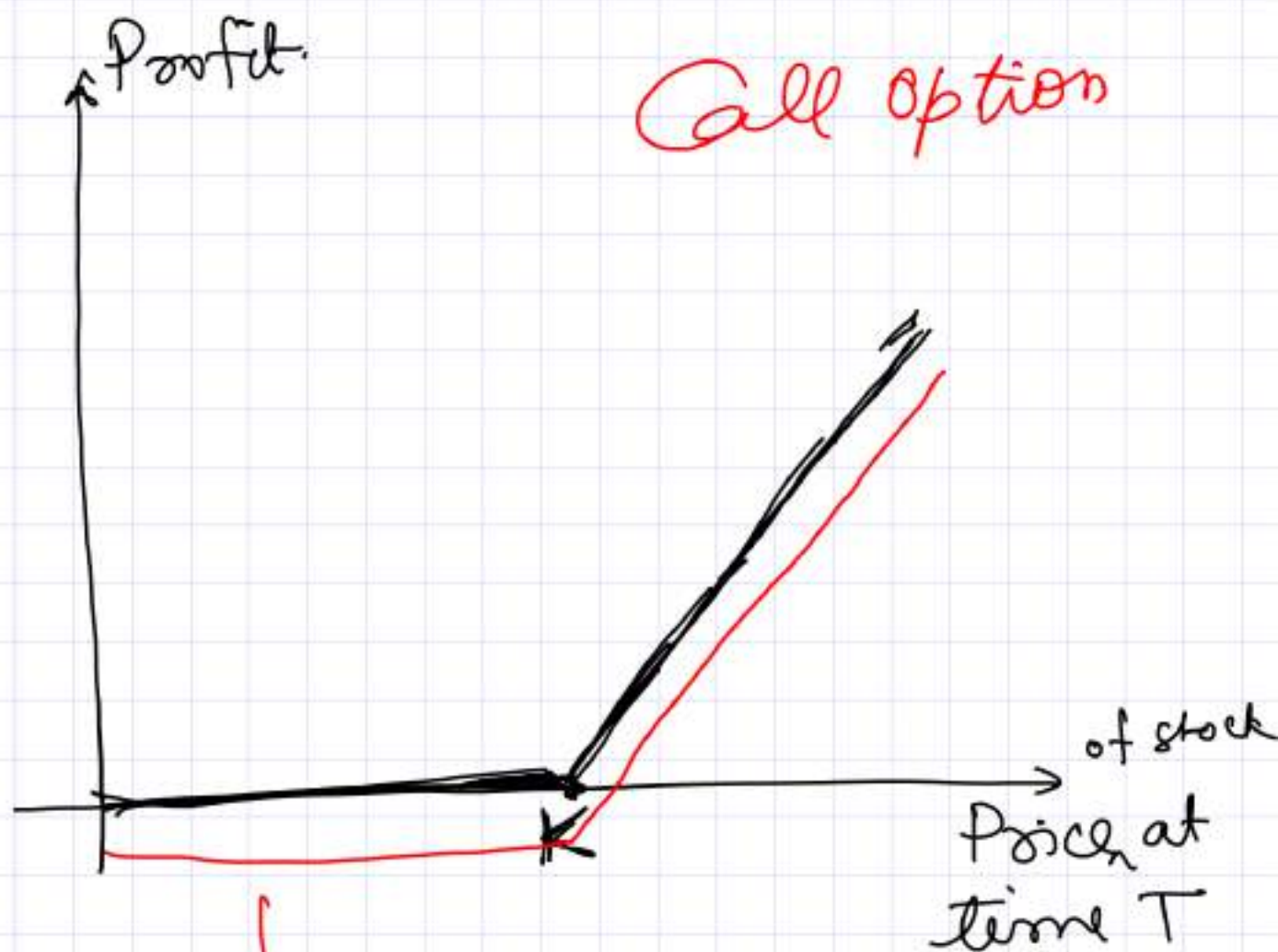
<sup>Put</sup>  
~~Call~~ option gives you (a right but not obligation) to

→ <sup>Sell</sup>  
~~Buy~~ the underlying stock at price  $K$  at time  $T$ .

For the call option:

Strike price  $(K) = 100$

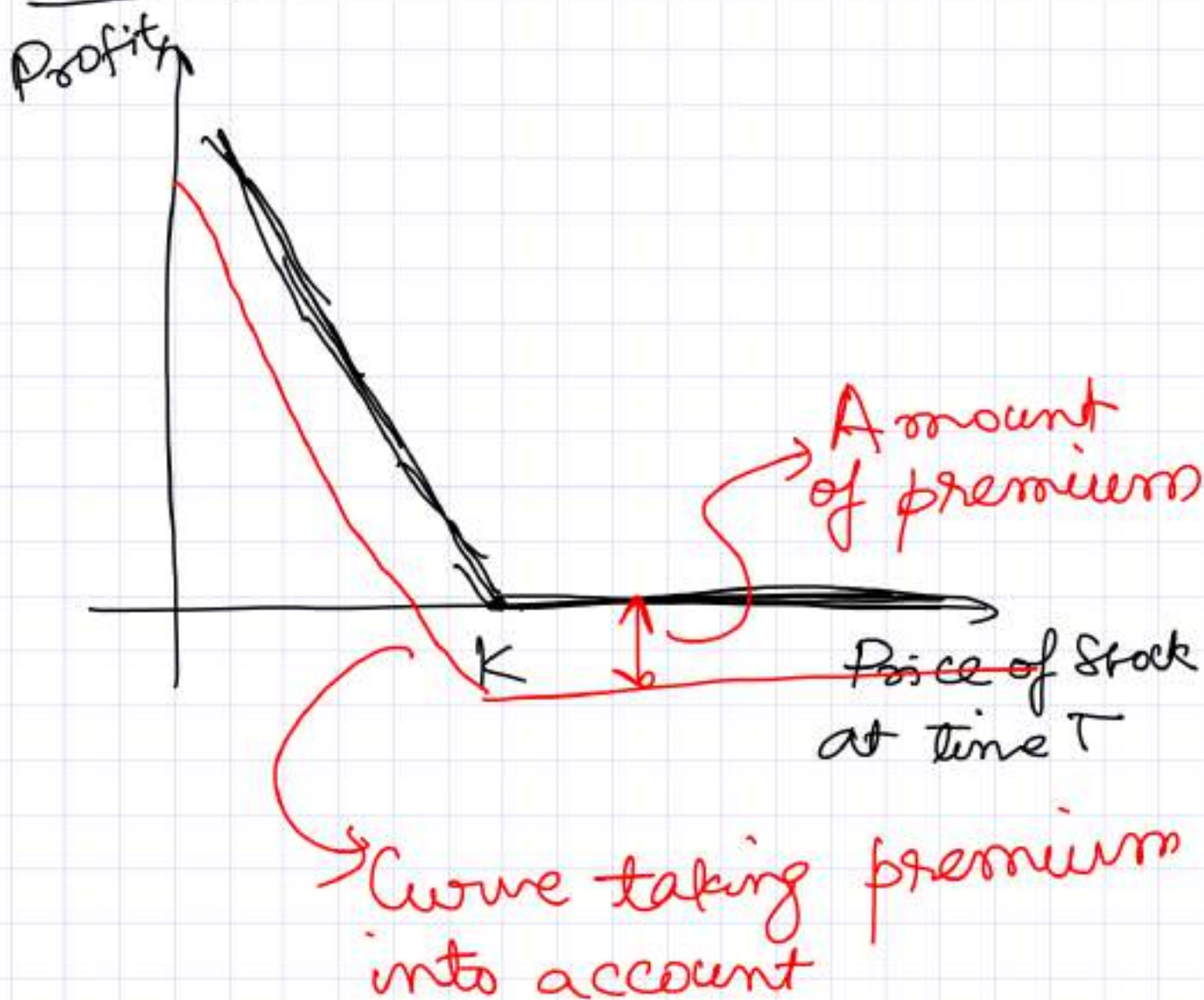
Price of stock at time  $T$  ( $S$ )  
 $S = 120$



Curve taking into  
account the premium



# Put option :



Both long & short options can be of two types.

- American option
- European option

Q: What are the factors that affect option prices?  $\rightarrow$  Option Premium  $\rightarrow 0$

A: There are 6 factors.

- ① The current stock price ( $S_0$ )
- ② The strike price ( $K$ ) ( $K \uparrow$ ,
- ③ The time to expiration ( $T$ )
- ④ The volatility of the stock price ( $\sigma$ )
- ⑤ The risk free interest rate ( $r_f$ )
- ⑥ The dividends that are expected to be paid.

Calc of option premium =  $C$

$C_1 \rightarrow S_0, K_1$

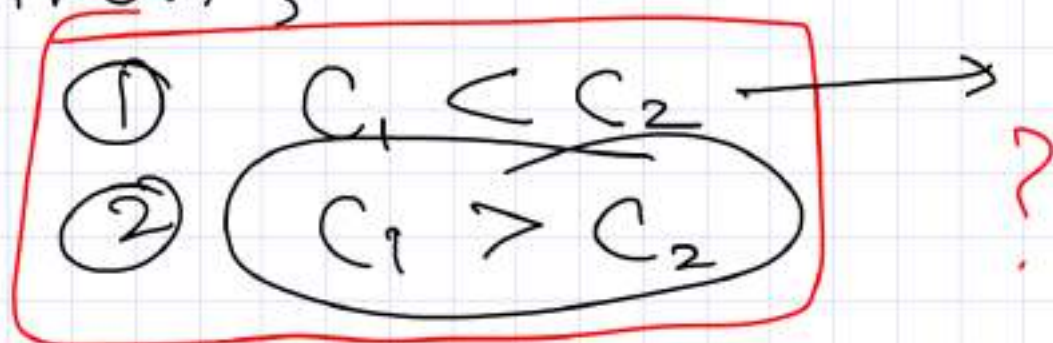
$C_2 \rightarrow S_0, K_2$

$\rightarrow$  current stock price



$K_1 < K_2 \longrightarrow$  Given

Then,



Which of ① or ② is true.

For a call option (C)

① $S_0$	$\longrightarrow$	$S_0 \downarrow$	, $C \downarrow$
② $K$	$\longrightarrow$	$K \uparrow$	, $C \uparrow$
③ $T$	$\longrightarrow$	$T \uparrow$	, $C \uparrow$
④ $\sigma$	$\longrightarrow$	$\sigma \uparrow$	, $C \uparrow$
⑤ $r$	$\longrightarrow$	$r \uparrow$	, $C \uparrow$
⑥ $d$	$\longrightarrow$	$d \uparrow$	, $C \downarrow$

For the put option the premium



# Black Scholes formula:

$$c = S_0 N(d_1) - K e^{-rT} N(d_2)$$

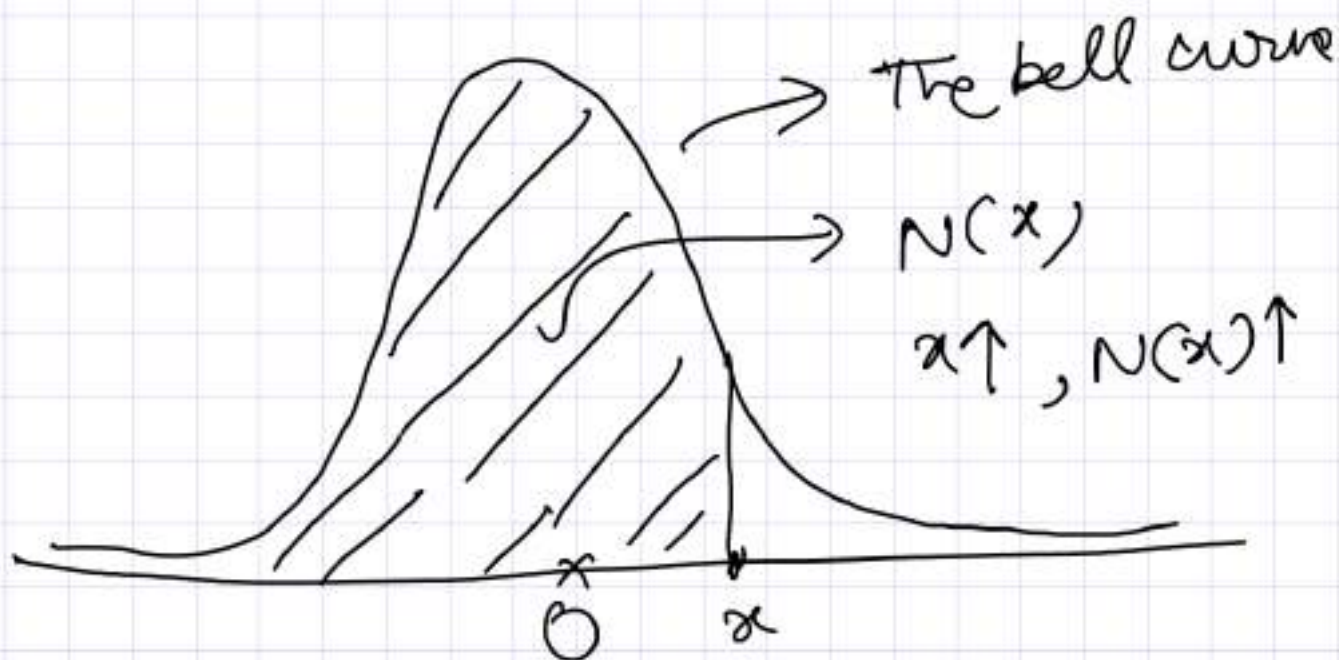
$$p = K e^{-rT} N(-d_2) - S_0 N(-d_1)$$

where,

$$d_1 = \frac{\ln(S_0/K) + (r + \sigma^2/2)T}{\sigma\sqrt{T}}$$

$$d_2 = \frac{\ln(S_0/K) + (r - \sigma^2/2)T}{\sigma\sqrt{T}}$$

$$= d_1 - \sigma\sqrt{T}$$



## Option Greeks:

- ① Delta
- ② Gamma
- ③ Vega
- ④ Theta
- ⑤ Rho

## Option greek Delta:

One of the factors that affect option price is current stock price.

For call option  $S_0 \uparrow, C \uparrow$   
 $S_0 \downarrow, C \downarrow$

For put option  $S_0 \uparrow, P \downarrow$   
 $S_0 \downarrow, P \uparrow$

The delta tells you by what fraction the option premium is affected if we change the stock price.

$\Delta \rightarrow$  Option Premium

$\Delta = C$  for call  
 $\Delta = P$  for put

$$\frac{\Delta \Delta}{\Delta S_0} = \frac{\partial \Delta}{\partial S_0}$$

Delta is between  $-1$  &  $+1$   
 For call option  $\rightarrow$  between  $0$  &  $1$   
 For put option  $\rightarrow [-1, 0]$





$$\Delta = \frac{\text{Change in Price}}{\text{Change in Underlying Price}}$$

$$\Delta = \frac{-0.1}{1} = -0.1$$

Diagram showing the calculation of Delta for a put option. The Delta is calculated as  $\Delta = \frac{-0.1}{1} = -0.1$ . The result  $-0.1$  is labeled "Out of the money" and the result  $1$  is labeled "In the money".

Out of the money

In the money

$$\left[ \begin{array}{l} S_0 = 100 \\ K = 50 \end{array} \right] \text{ Out of the money put option}$$

$$S_0 = 100$$

$$K = 250$$

In the money  
Put of 100

$$S_0 \rightarrow 101$$

Then

$$100$$

$$\cancel{101} \quad 99$$

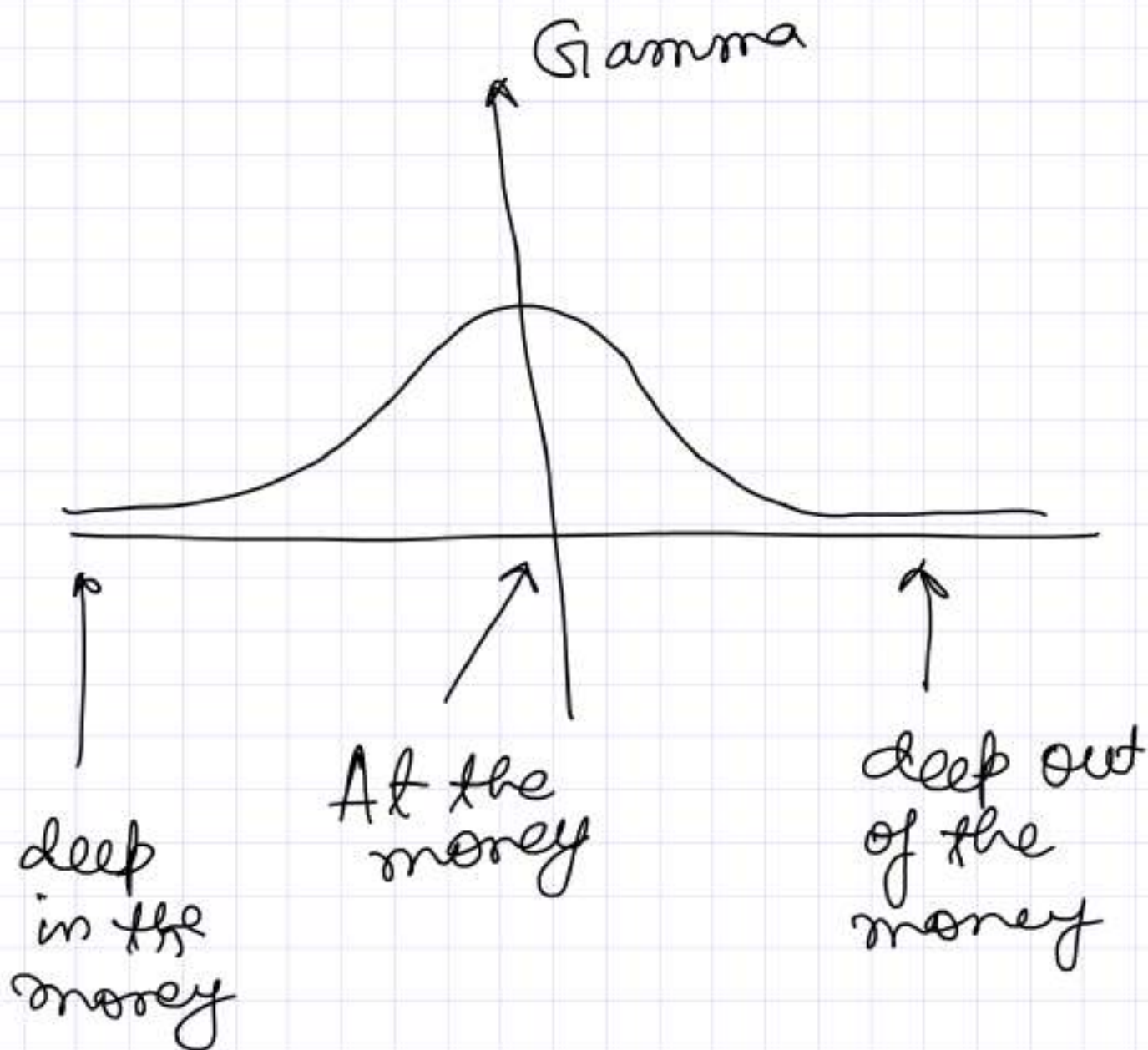
{Change in Payoff}

$$\Delta S_0$$

$$= \frac{-1}{+1} = \textcircled{-1}$$

# Gamma :

↪ Change in delta relative to price of the underlying.

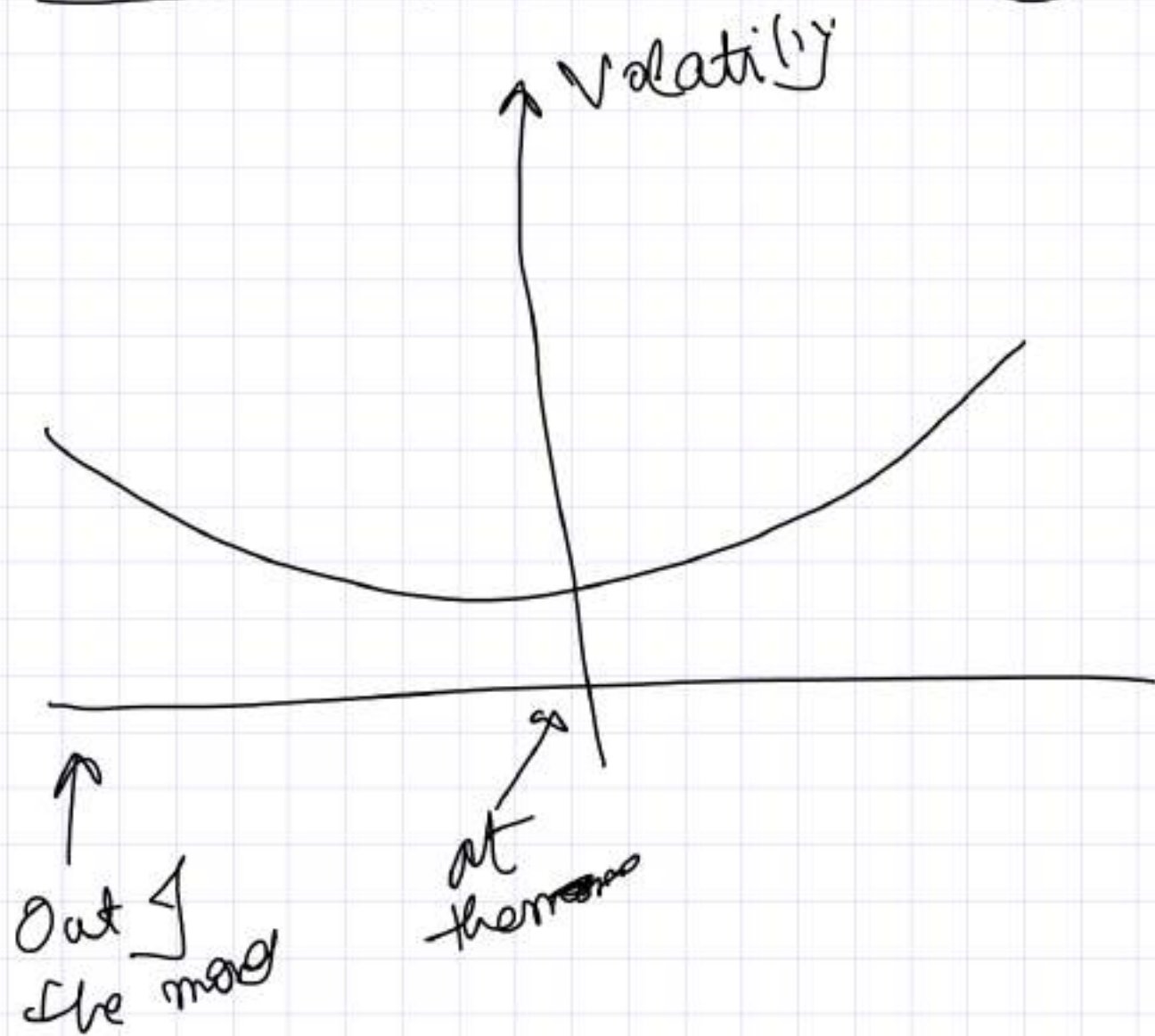




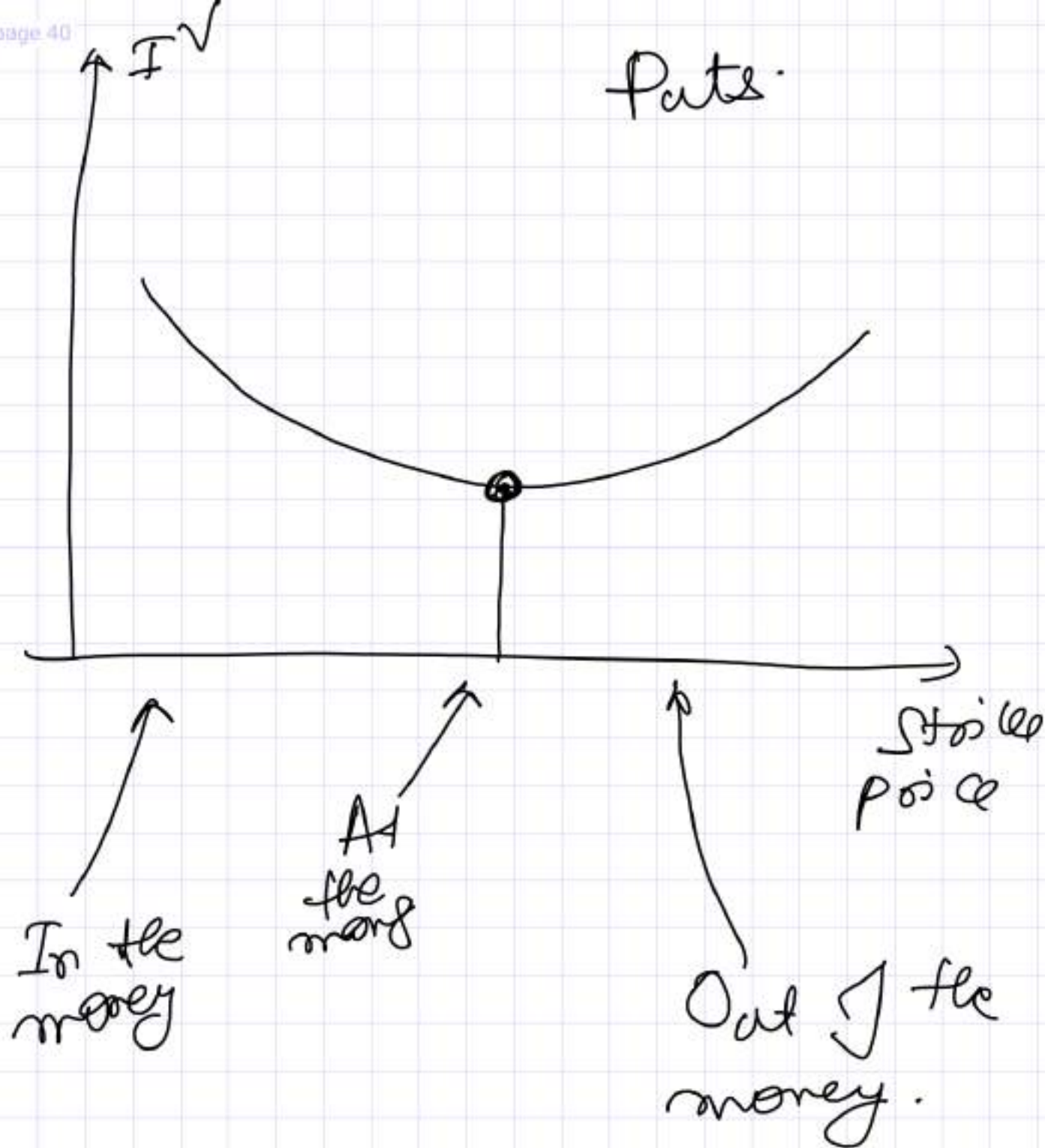
# Implied Volatility (IV):

The volatility at which the option price was calculated.

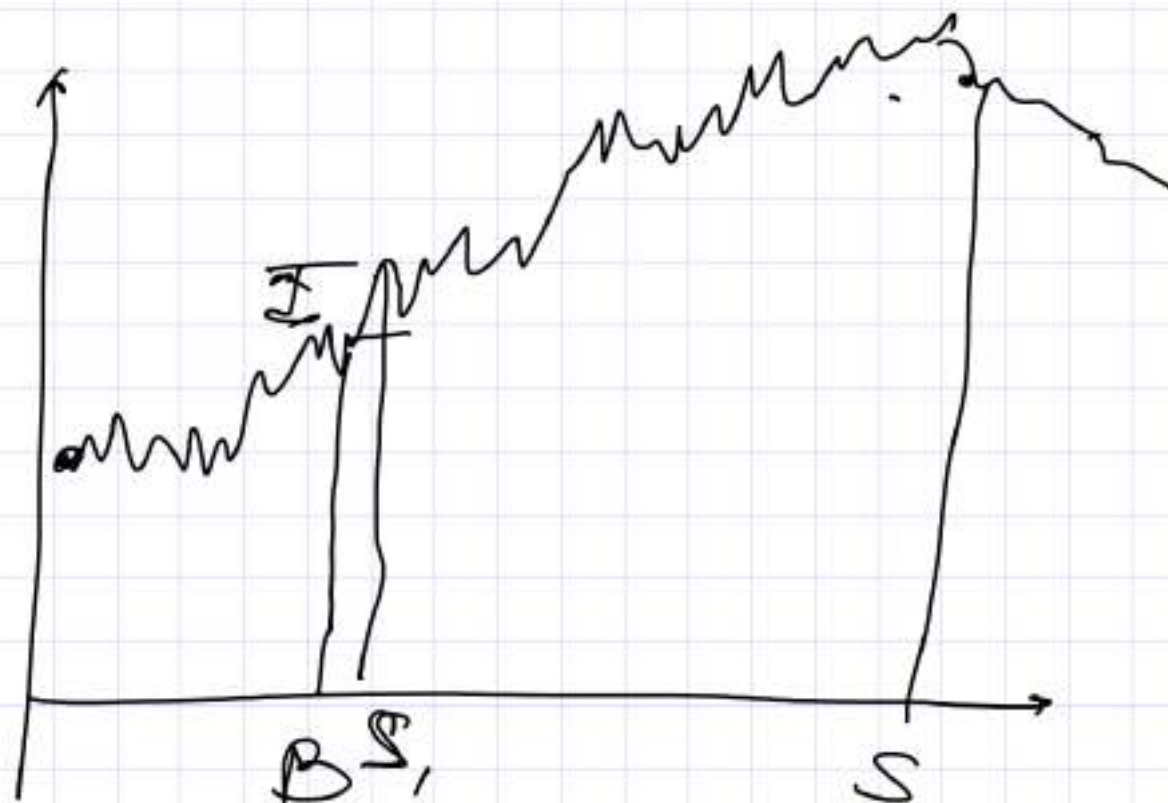
## Volatility Smile: ☺



Puts.



Scalping: It is a trading strategy where we close the position immediately when we are in profit.



Now we'll study.

Gamma Scalping:



There are many option trading strategies.

→ Butter fly } → You can  
→ Straddle. } get the  
resources.

## Straddle option trading strategy:

It involves the following

- ① Buying or selling of call/put option (at the money)
- ② The options should have the same underlying asset.
- ③ They should have the same strike price ( $K$ )

- ④ They must have the same expiring date,  $(T)$

## Gamma Scalping:

- ① Trader purchases straddle at some initial price.
- ② Initially deltas cancel each other

$$\Delta_C - \Delta_P = 0$$

- ② Then market moves in some direction, and deltas change.

$$\Delta'_C - \Delta'_P \neq 0$$



Then we implement this strategy.

$$\textcircled{3} \quad S \downarrow \quad \Delta_C - \Delta_P < 0$$

Then The investor buys one stock.

Delta of the stock = 1

$$\Delta_C - \Delta_P + \alpha S = 0$$

We have rebalance the delta of the portfolio to zero again.

We'll keep buying or selling the stock to rebalance the delta of the



# portfolio.

⇒ With ~~the~~ time your portfolio value ~~with~~ will increase

IF there are moves in the market.

HOWEVER IF :

Market mostly does not move. Investor loses money.

# Spread Arbitrage:

Here we take advantage of the spot & future contract of the same asset with different strike price.

$$\left[ \begin{array}{l} \text{Spot Price} \\ \text{Future Price} \end{array} \right] \rightarrow \left[ \begin{array}{l} (F = S + \alpha) \\ \text{where } \alpha \begin{cases} (+) \text{ve or} \\ (-) \text{ve} \end{cases} \end{array} \right]$$

long in the future.

$\rightarrow$  You have <sup>obligation</sup> to buy one unit of stock at time 'T'.

There is no strike price.



① Arbitrage money is made when there is a stock & future prices are not related to each other, the way they should have been after taking into account all the necessary factors like

→ Interest rate

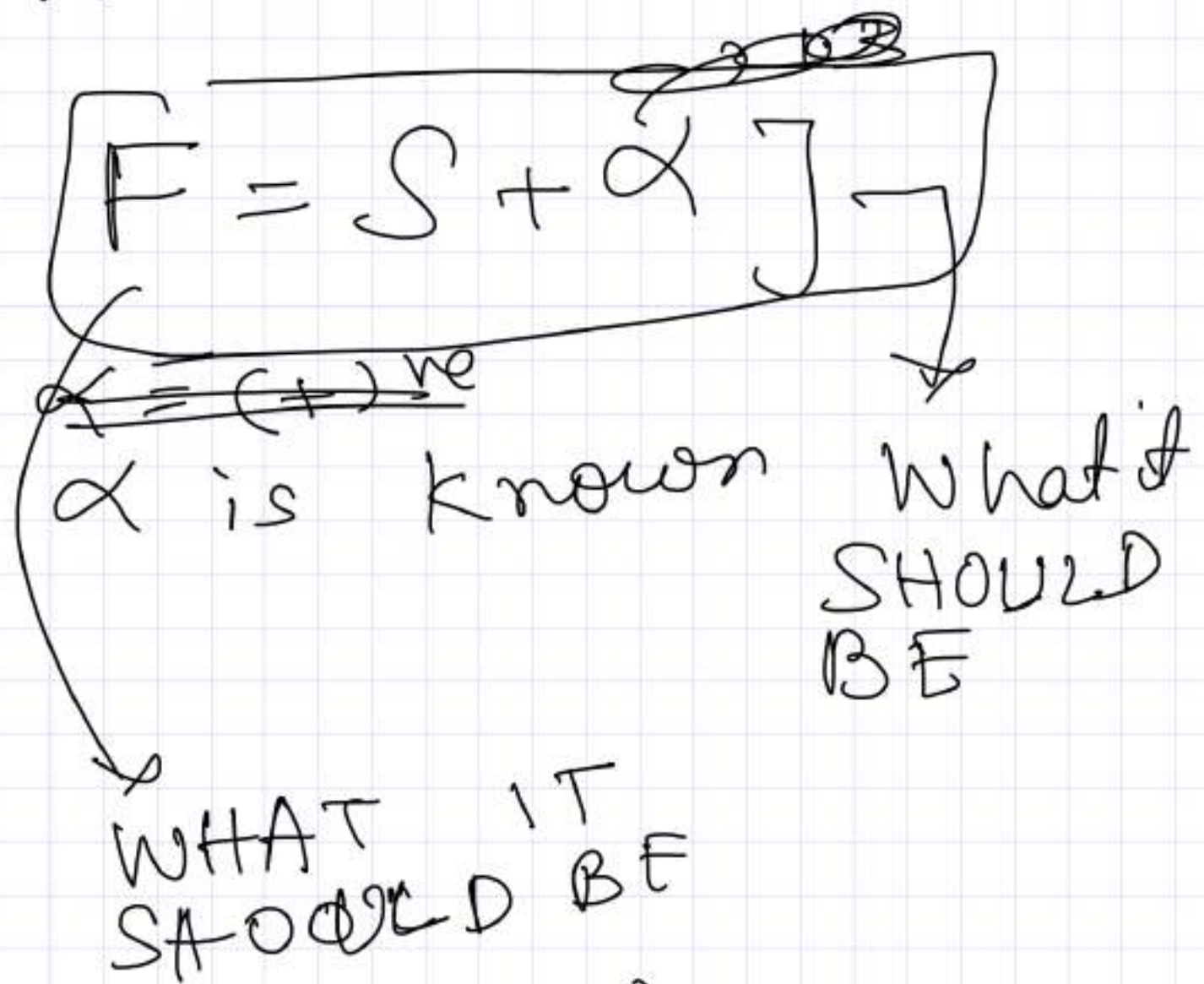
→ Delivery / Storage cost

→ Contango / Backwardness

→ ~~Expected~~ Expected demand etc. etc.



All these factors are Public Knowledge.



$F = S + \beta$

REALITY

$\alpha = 1, \beta = 2$

~~$F = S + 1$~~   $\rightarrow$  Should be

$F = S + 2 \rightarrow$  IS

# Short on Future

→ Sold a future contract

$$= S_0$$

↖ [Adjustments  
for time  
value] money

- ① Sell a future contract
- ② Buy the stock

$$F = S_0$$

$F > S_0$  } This will lead  
 $F < S_0$  } to arbitrage  
 opportunity.

- ( $F < S_0$ )
- ① Buy the future
  - ② Sell the stock

Future we have expiring

$F_1 \longrightarrow$  expiring  $T_1$

$F_2 \longrightarrow$  expiring  $T_2$

There is a relation in  $F_1$  &  $F_2$  price. In case  $t_2 = 0$ , etc.

$$F_1 = F_2$$

O.w.

$$F_1 = F_2 + \text{~~0~~}$$

$$\rightarrow F_1 > F_2$$

Calendar spread.



# Electronic market making:

Market makers place limit orders for both buy & sell. They make money based on the ~~difference between~~ Bid ask spread.

———— Ask ( $P_1$ )  
———— Bid ( $P_2$ )

$$P_1 > P_2$$

They sell at  $P_1$

They buy at  $P_2$

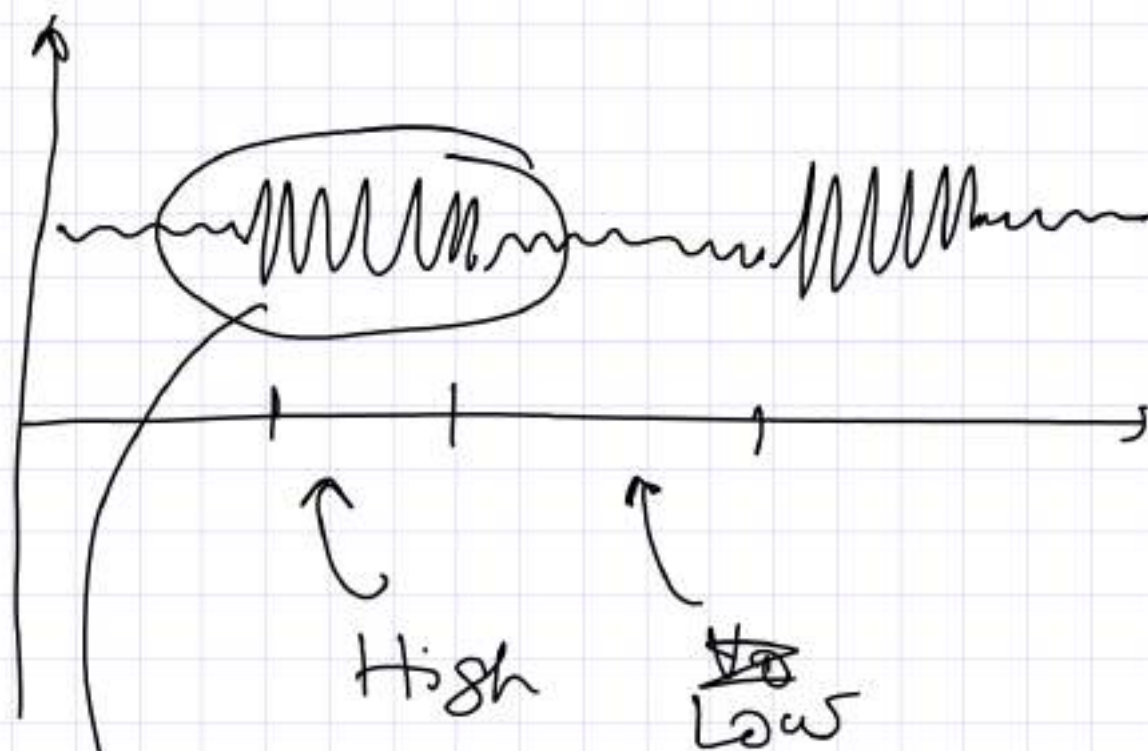
They make money  
 $(P_1 - P_2)$

Bid - Ask spread.

② Volatility ( $V$ )

$V \uparrow$ , Bid-ask spread  $\uparrow$

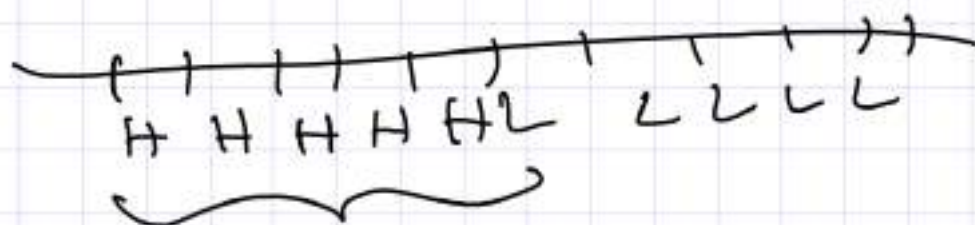
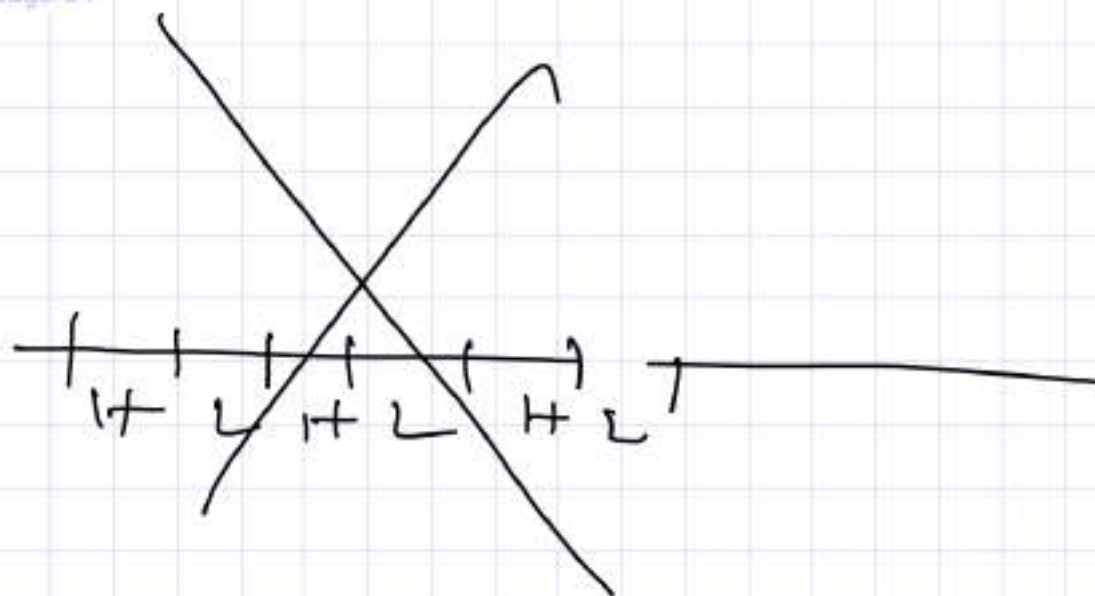
# Volatility clustering:



High ~~the~~ volatility  
movements are clustered  
and near each

Volatility clustering

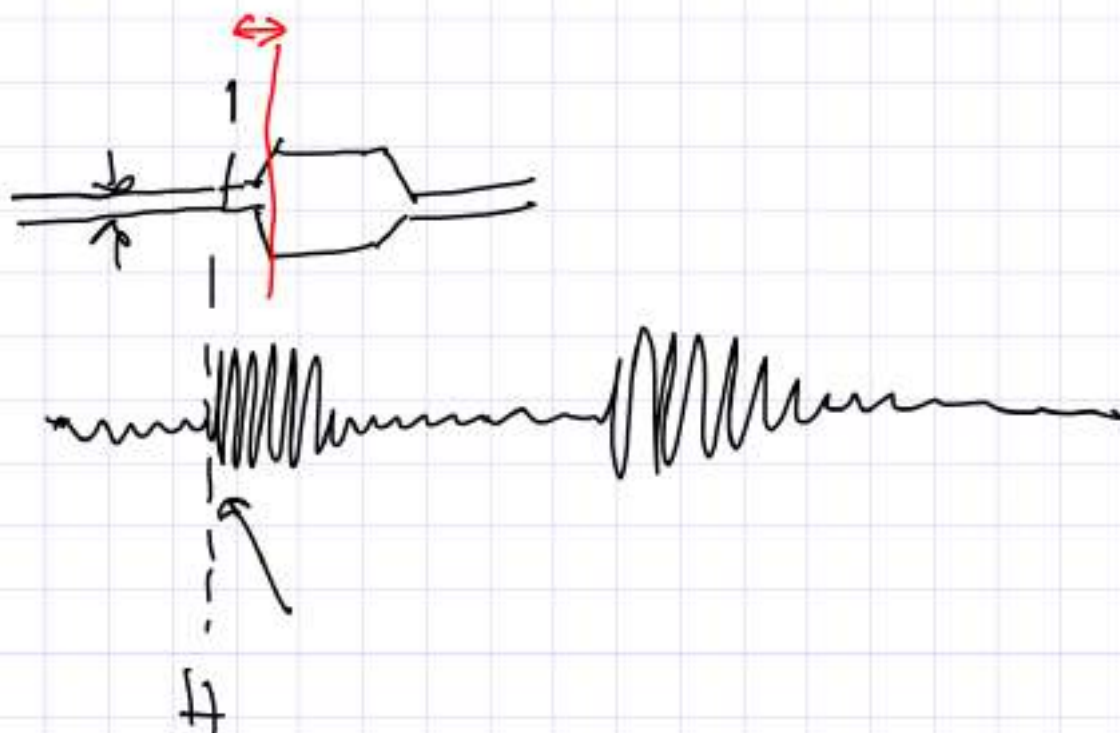




However we do not know when volatility <sup>will be</sup> ~~is~~ high.

If we know in advance we will be able to increase bid ask spread.

[Predict when the next high volatility zone will come]



These things can be modeled.

