



Advancing
Physics

76th Annual Meeting of the Division of Fluid Dynamics

Correlating hydrodynamic and acoustic fields in a turbulent combustor through community-based dimensionality reduction of vortical networks

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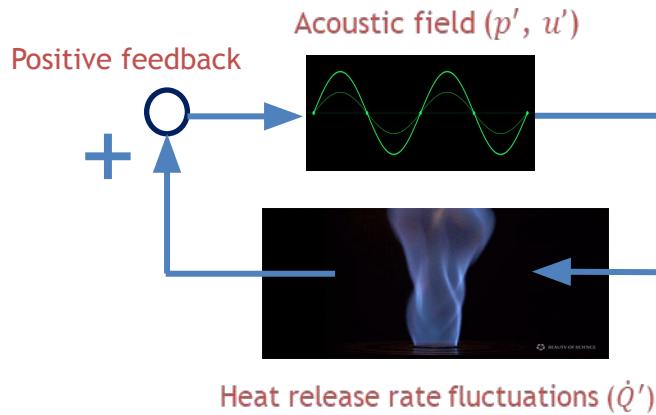
Acknowledgement:

Office of Naval Research Global

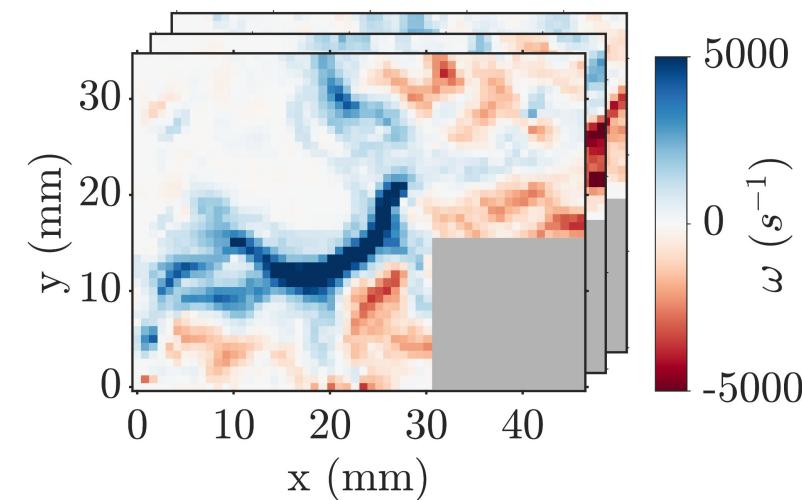
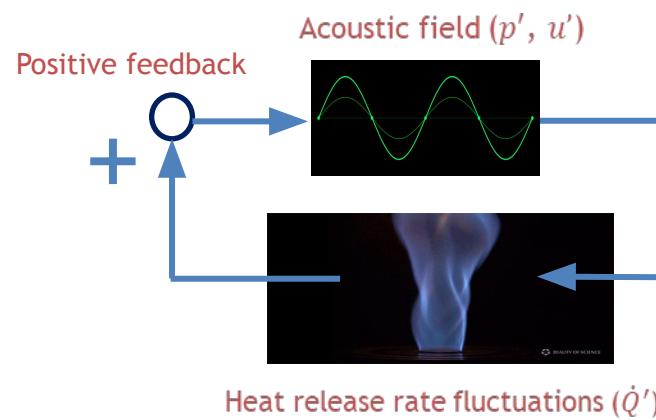
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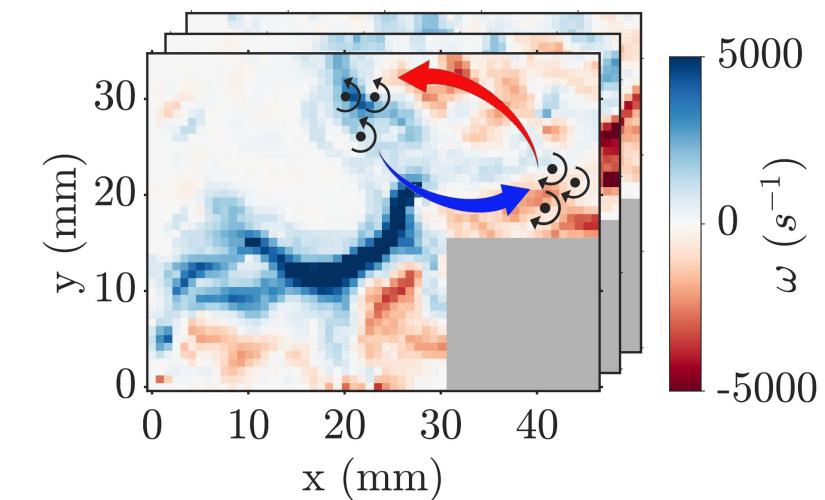
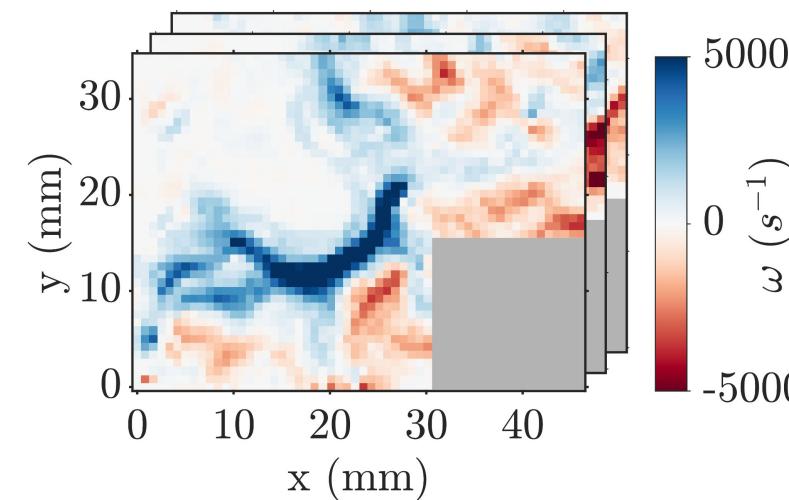
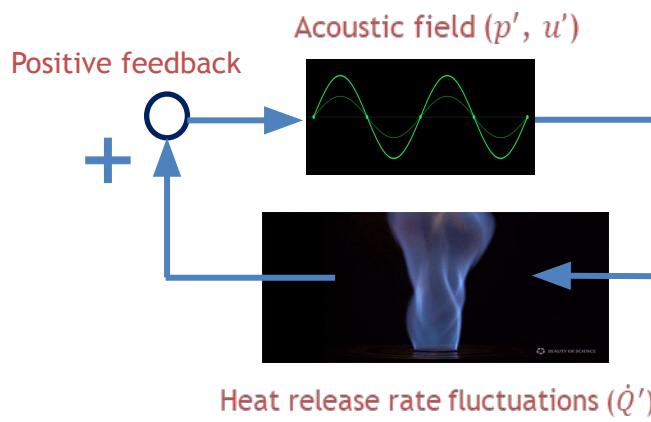
Positive feedback between acoustic pressure and heat release rate oscillations



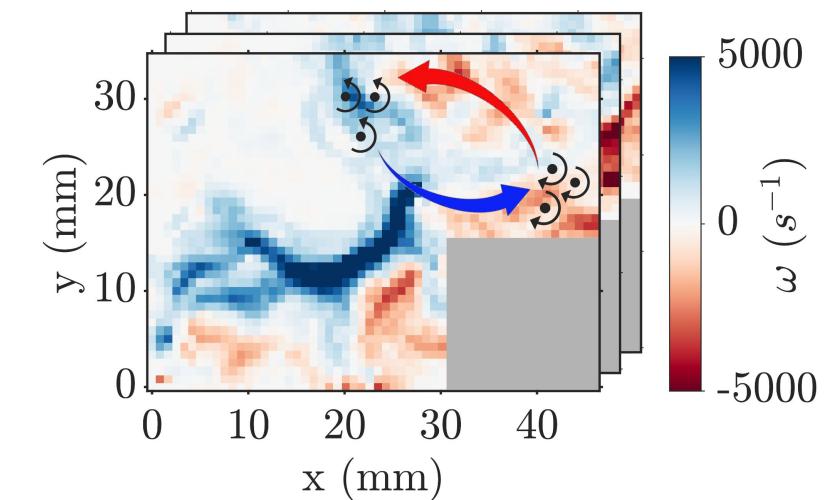
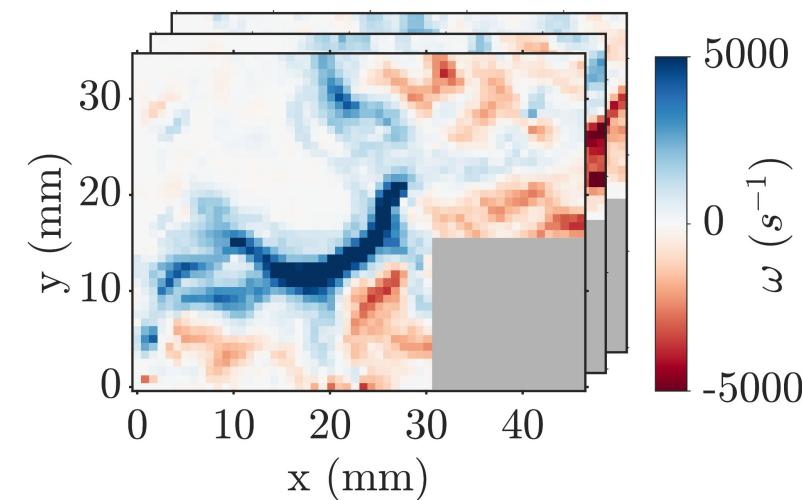
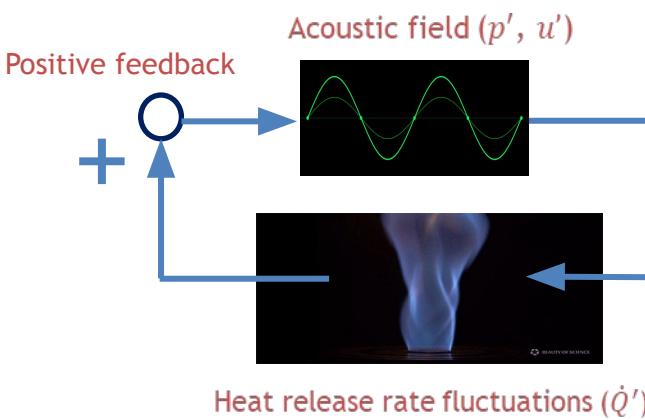
Vortical structures drive thermoacoustic instability in many combustors



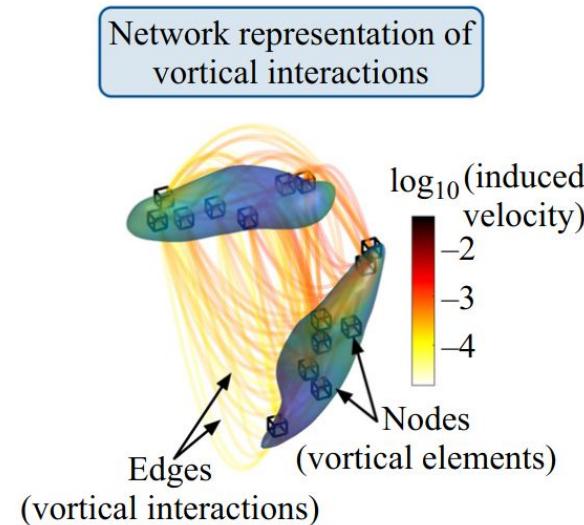
Understand the relation between vortical interactions and acoustic pressure oscillations



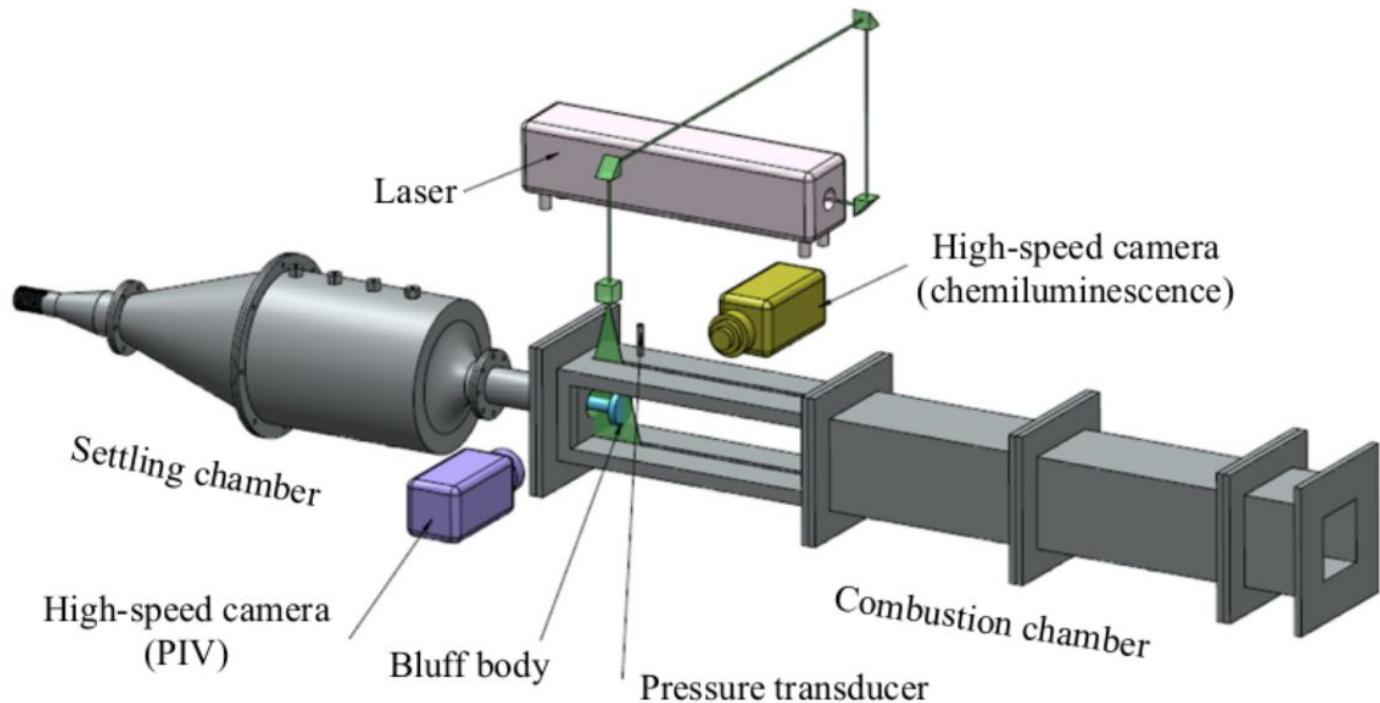
Complex networks provide a convenient framework to work with a large number of interactions



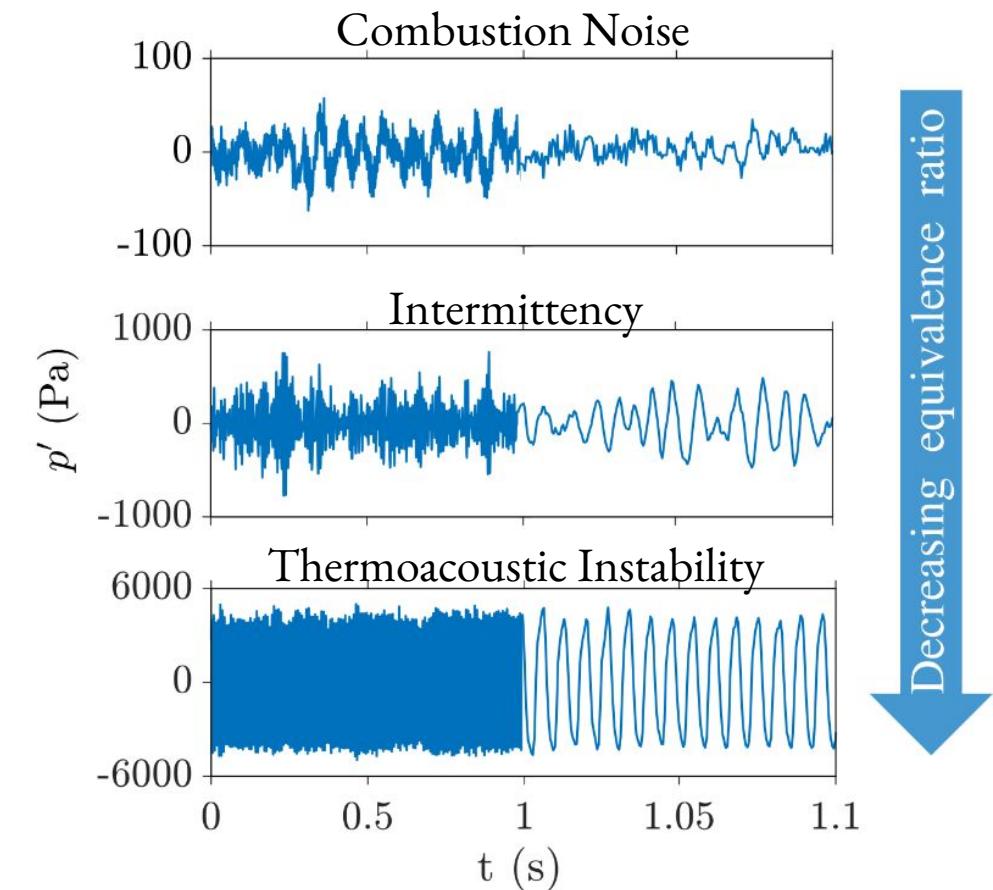
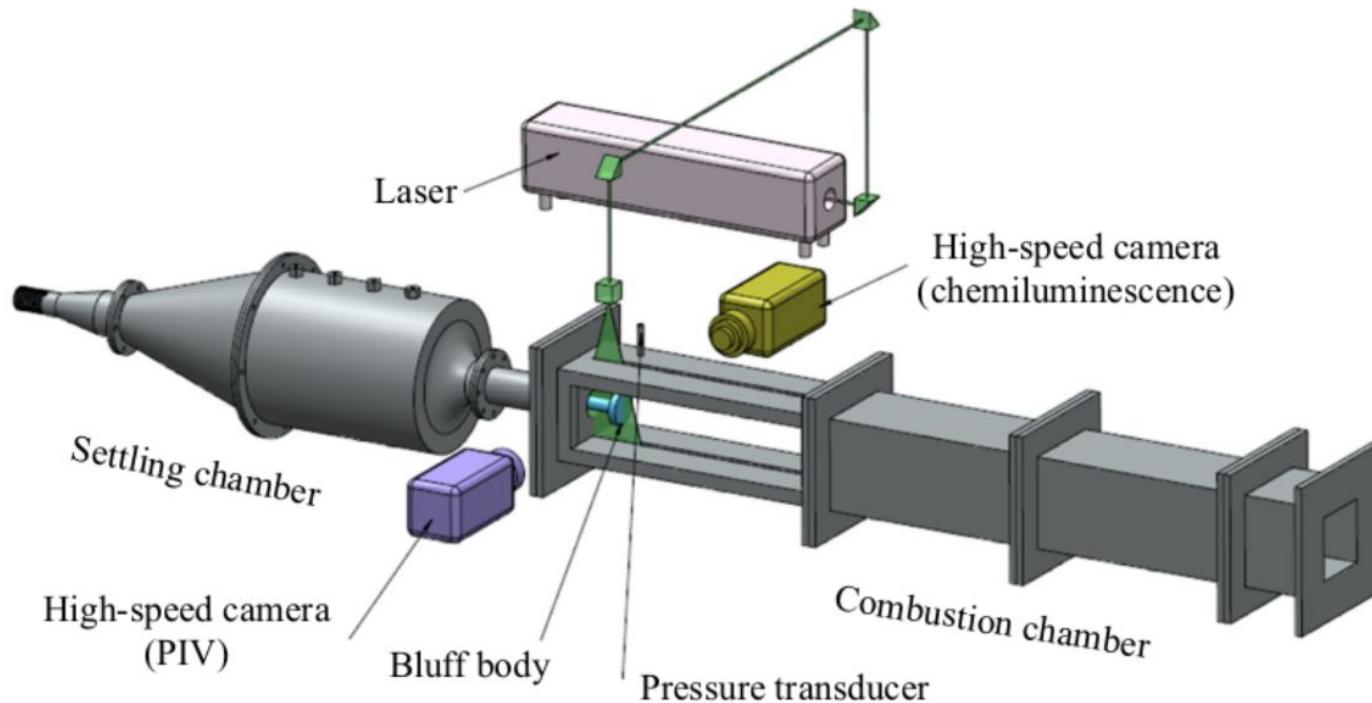
45×60 cells
 ≈ 1.5 million interactions



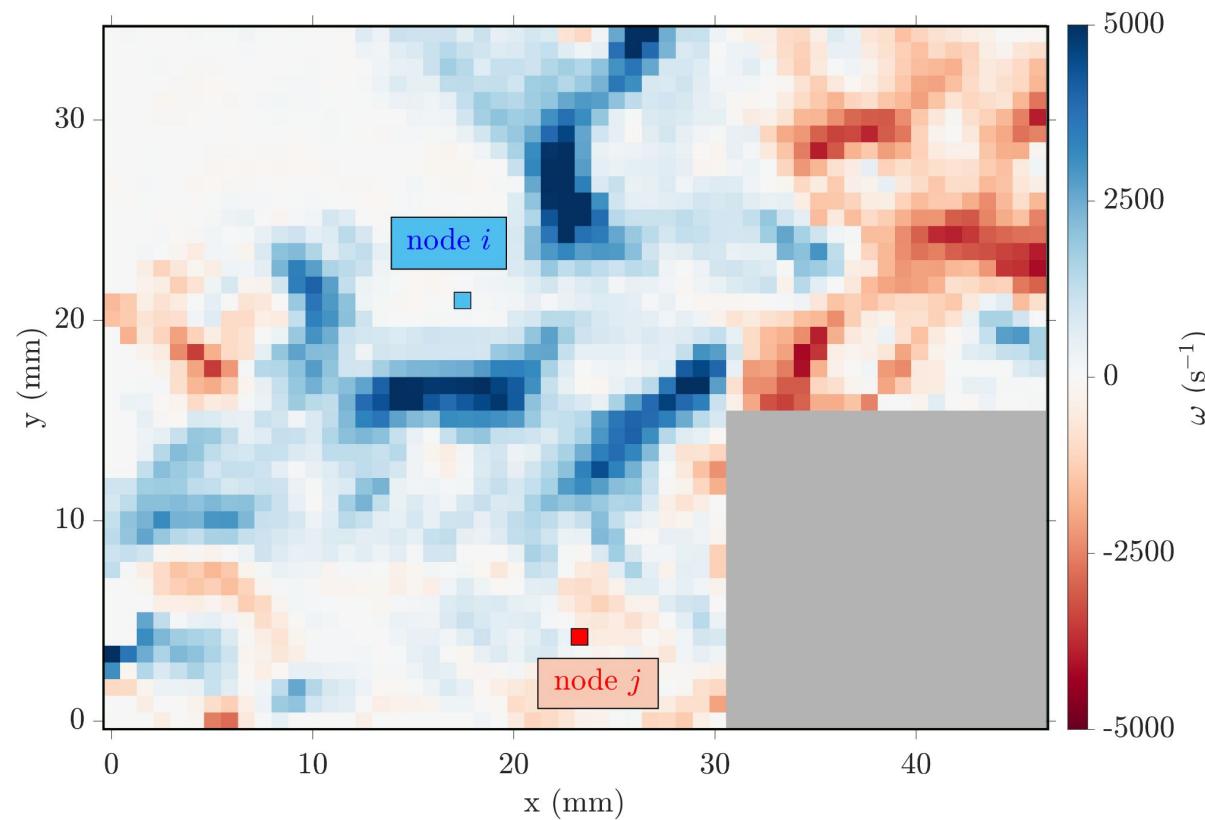
Bluff-body stabilized turbulent combustor



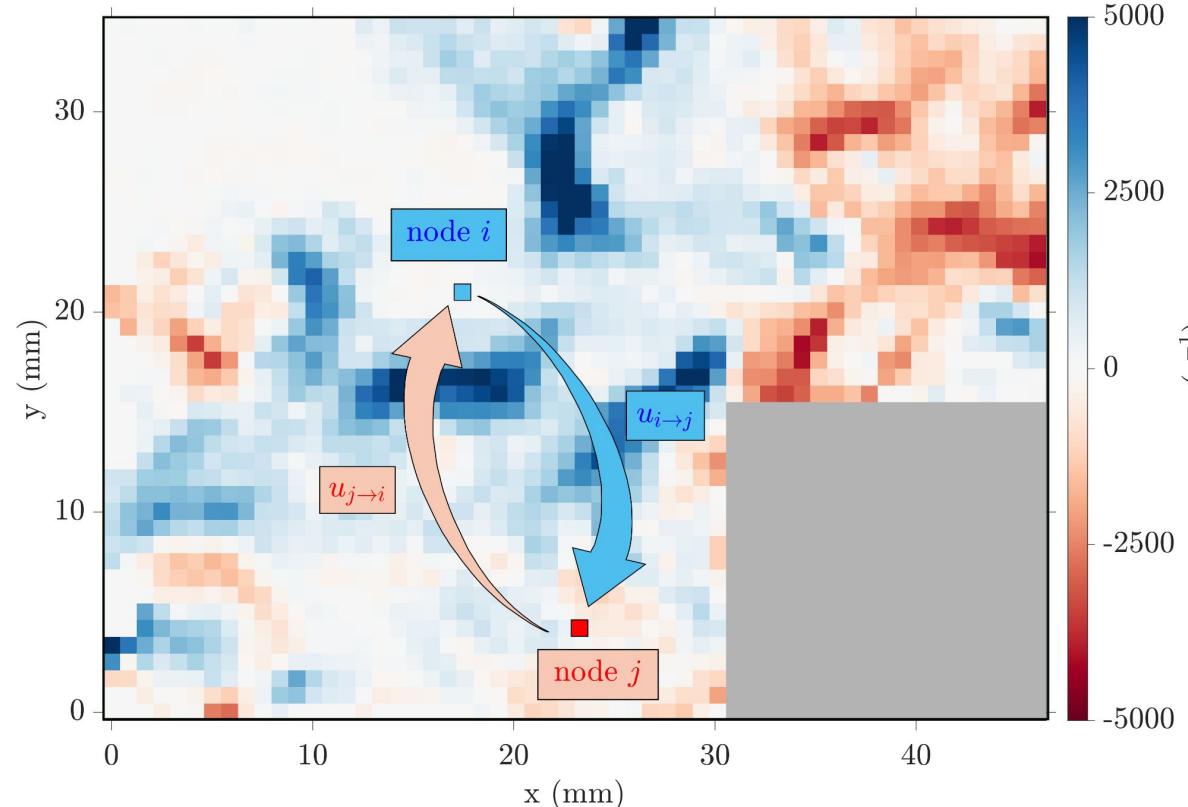
Bluff-body stabilized turbulent combustor - states of combustion noise, intermittency, and thermoacoustic instability



Cells of PIV computation domain - nodes of a complex network

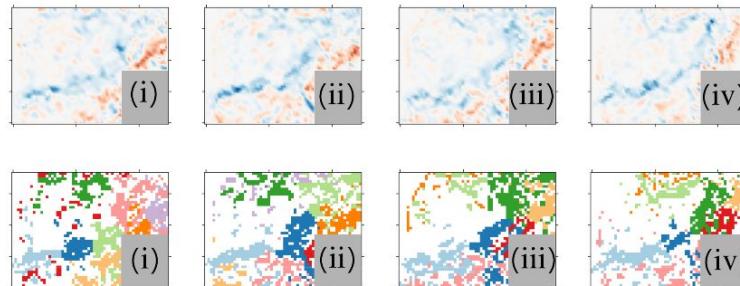
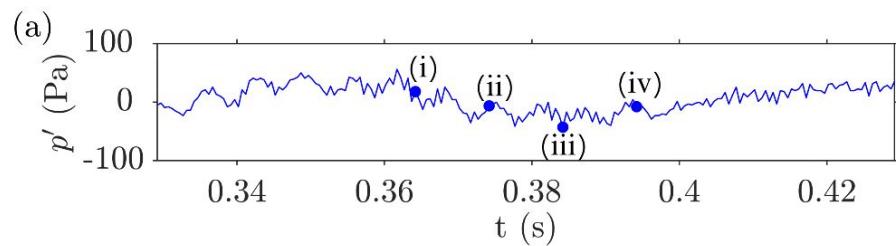


Induced velocity calculated from Biot-Savart law - directed links of a weighted complex network

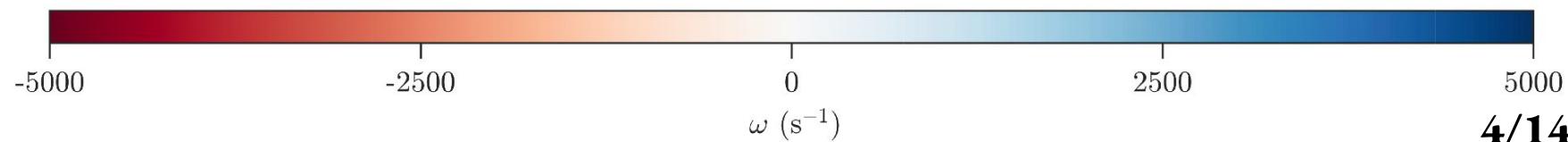


$$u_{i \rightarrow j} = \frac{1}{2\pi} \int_{S_i} \frac{\omega_i(\mathbf{r}', t) \times (\mathbf{r}_j - \mathbf{r}'_i)}{\|\mathbf{r}_j - \mathbf{r}'_i\|_2^2} dS_i$$

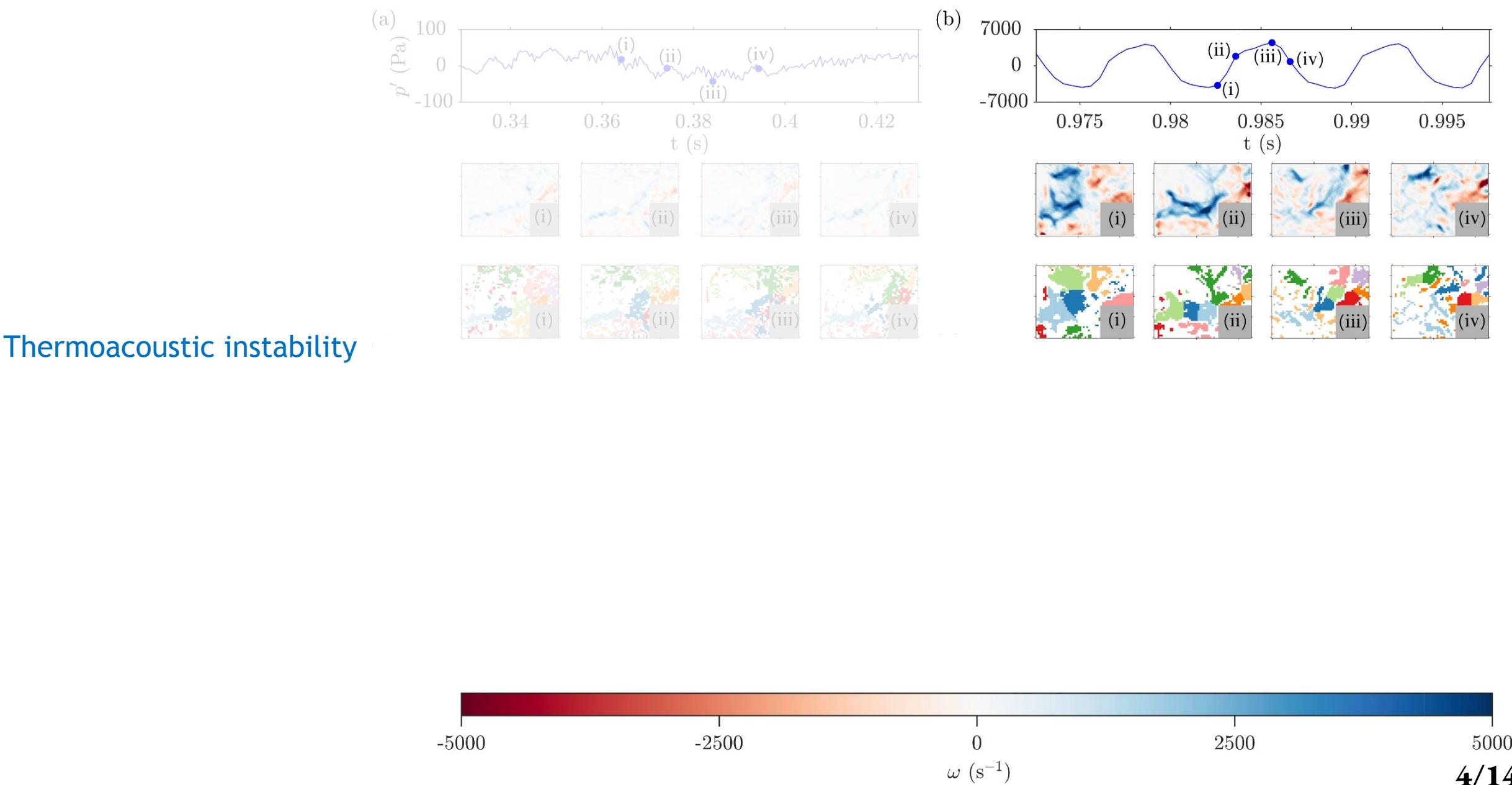
Vortical communities during different dynamical states



Combustion noise

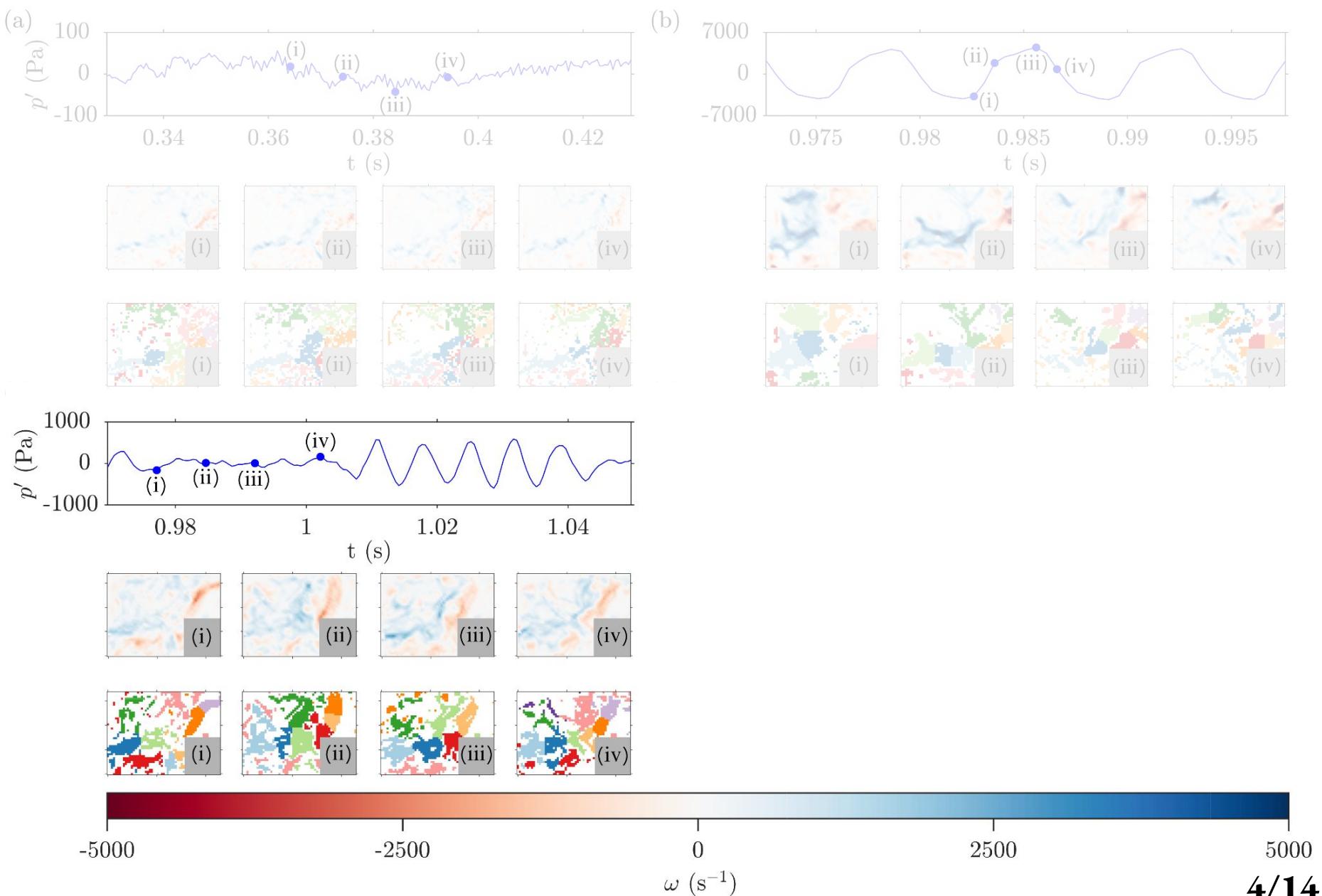


Vortical communities during different dynamical states



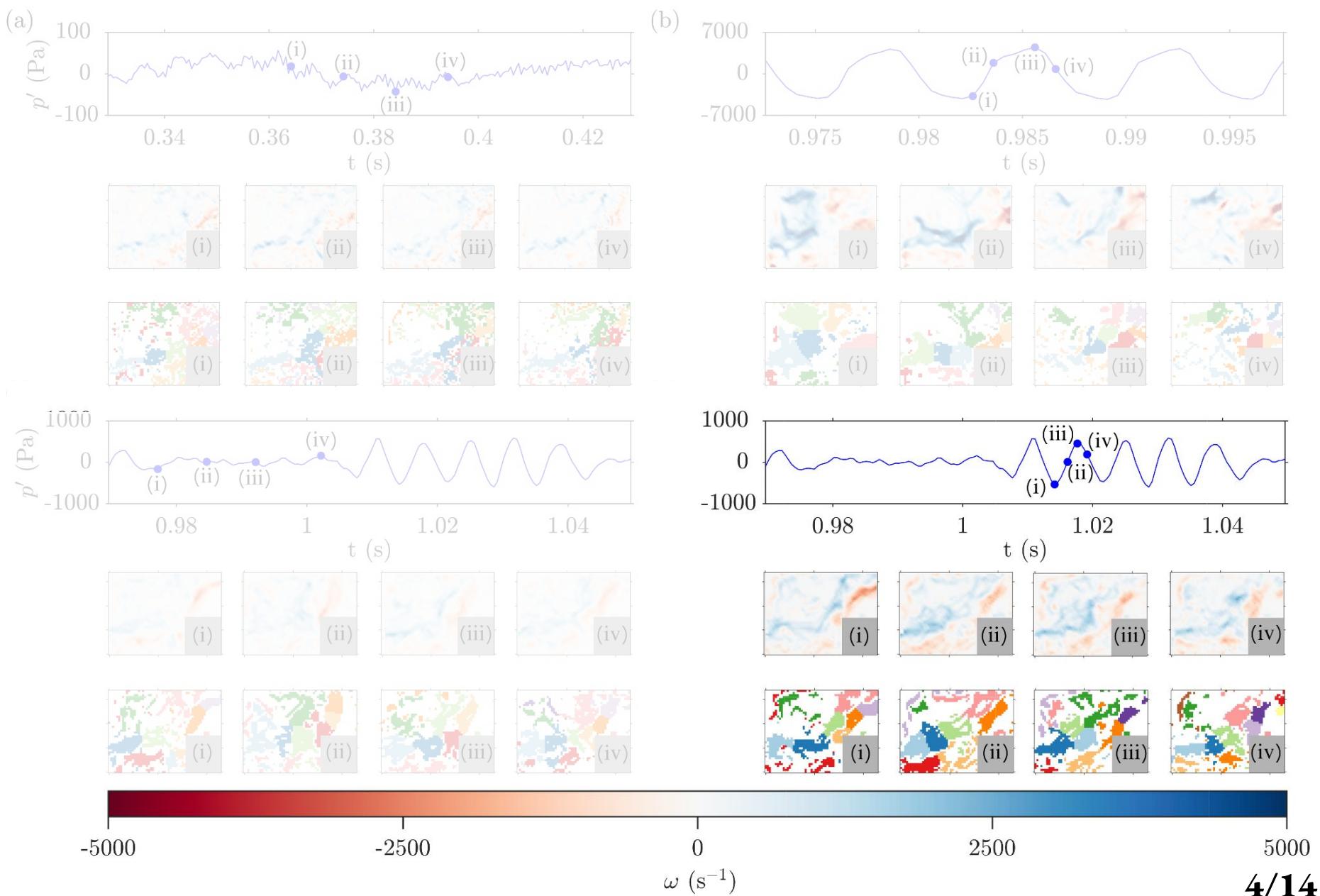
Vortical communities during different dynamical states

Aperiodic epoch of intermittency

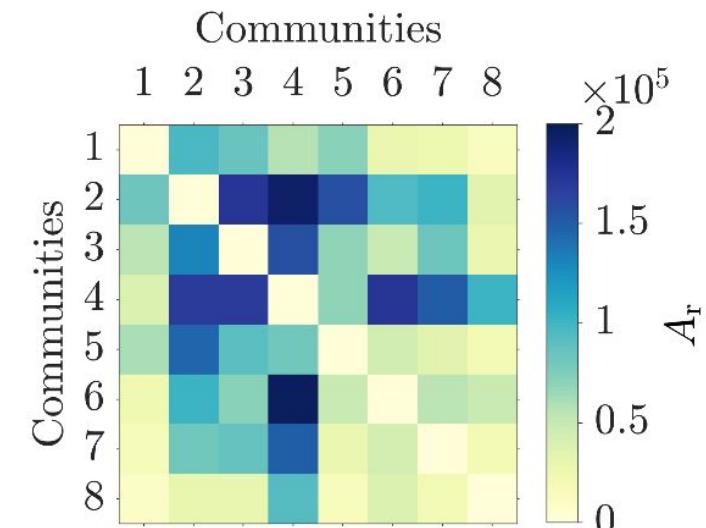
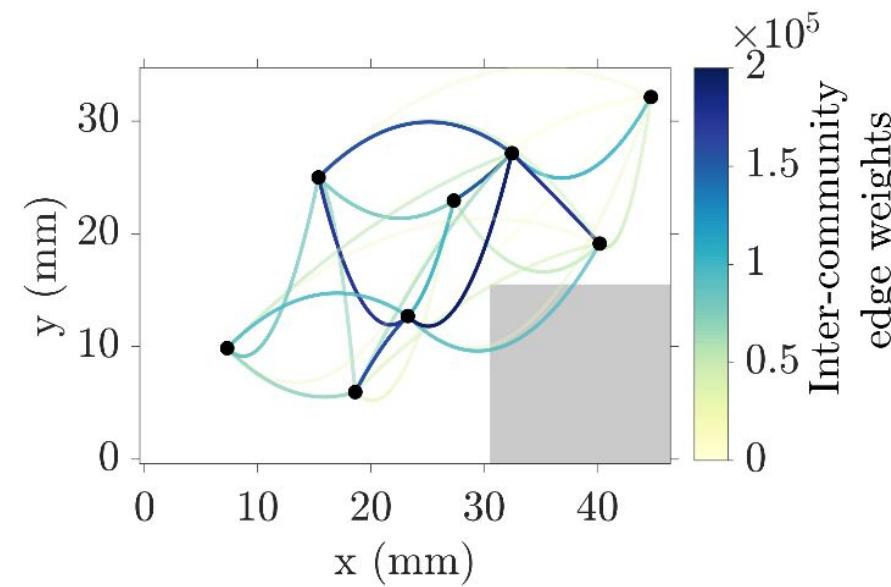
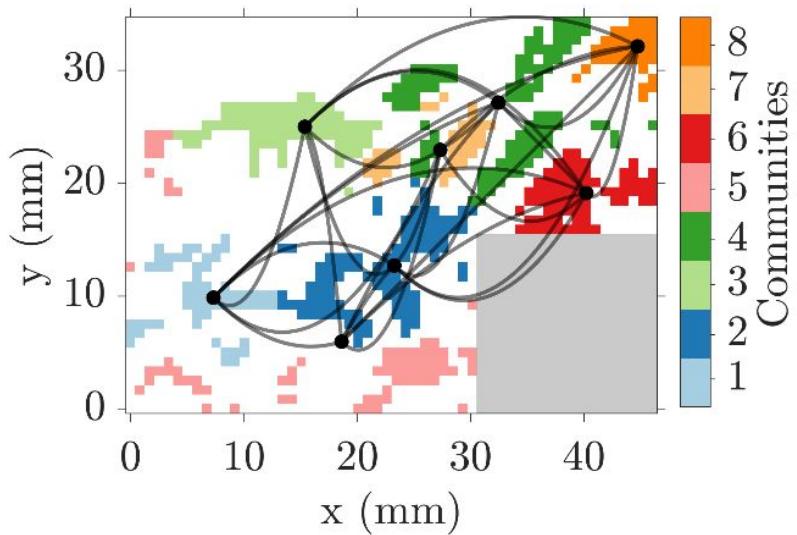


Vortical communities during different dynamical states

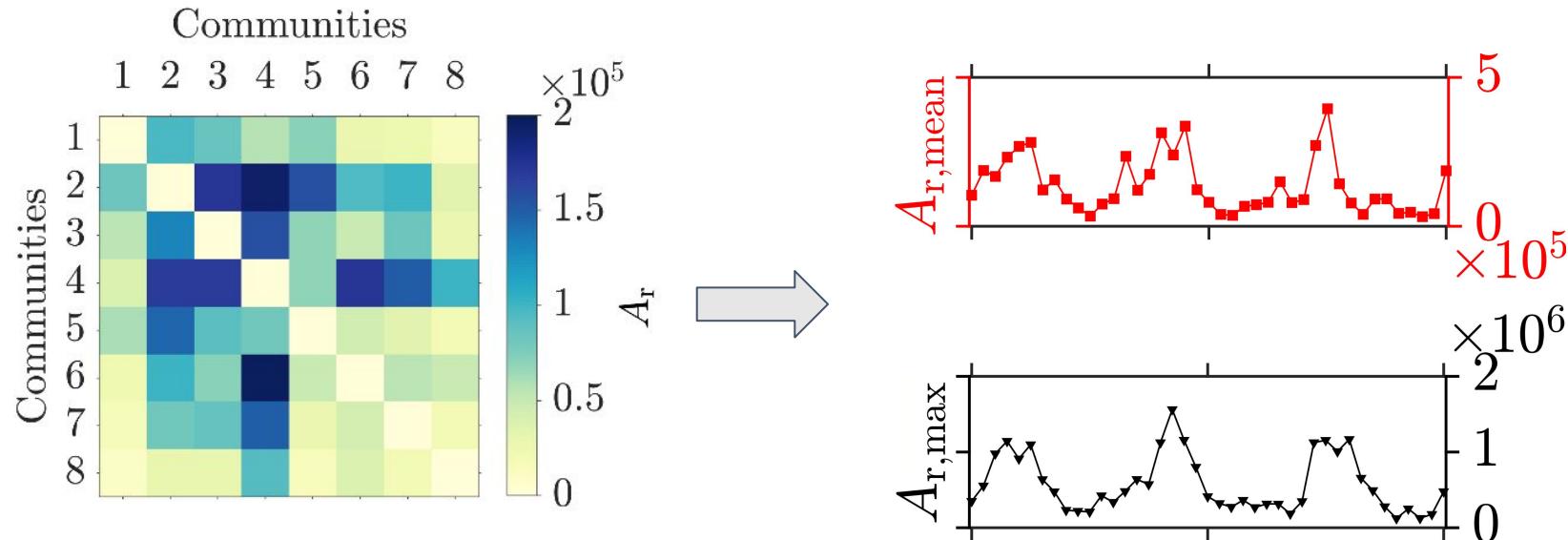
Periodic epoch of intermittency



At each time instant, communities are condensed through their weighted centroids to form **inter-community reduced networks**



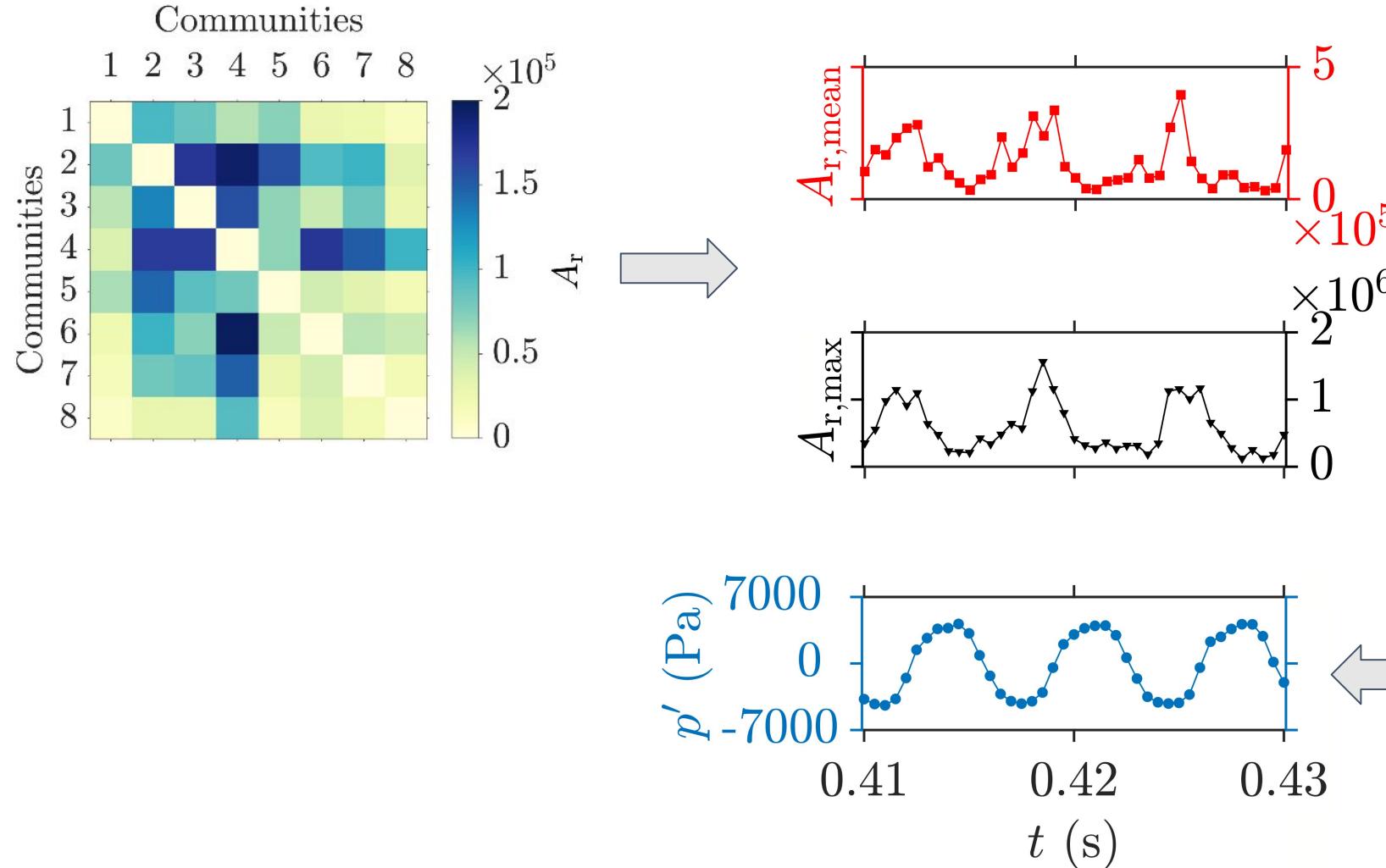
Network measures considered - mean and maximum of the reduced adjacency matrix



Average of all
inter-community interactions

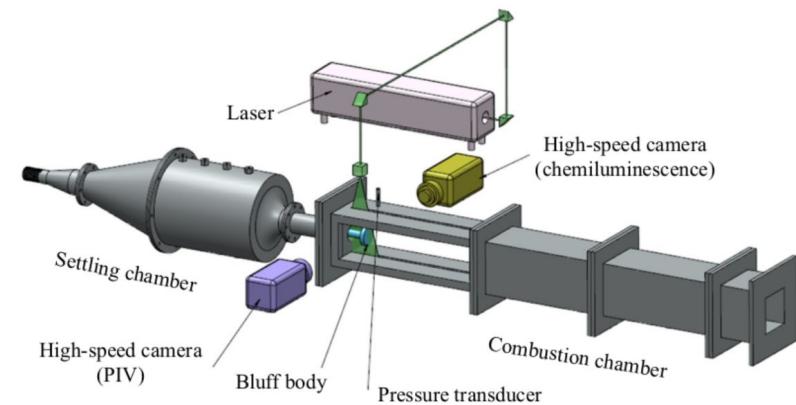
Maximum of all
inter-community interactions

Evaluate correlation between temporal evolution of network measures and acoustic pressure fluctuations

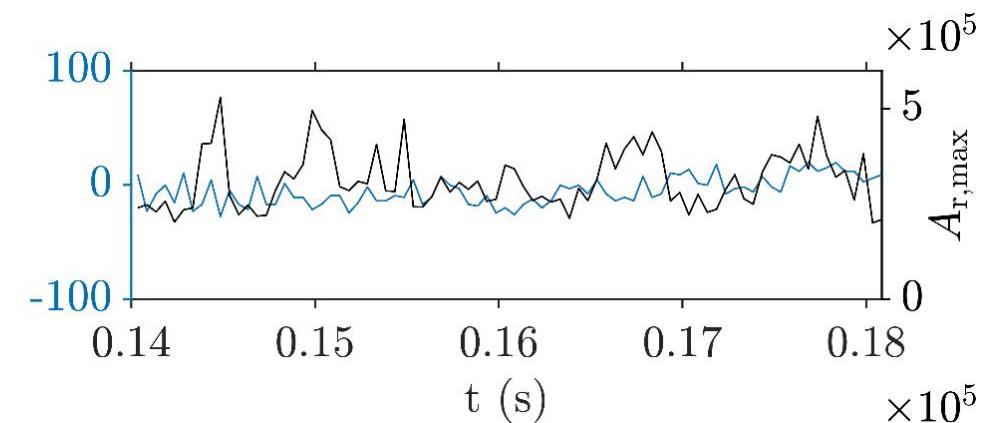
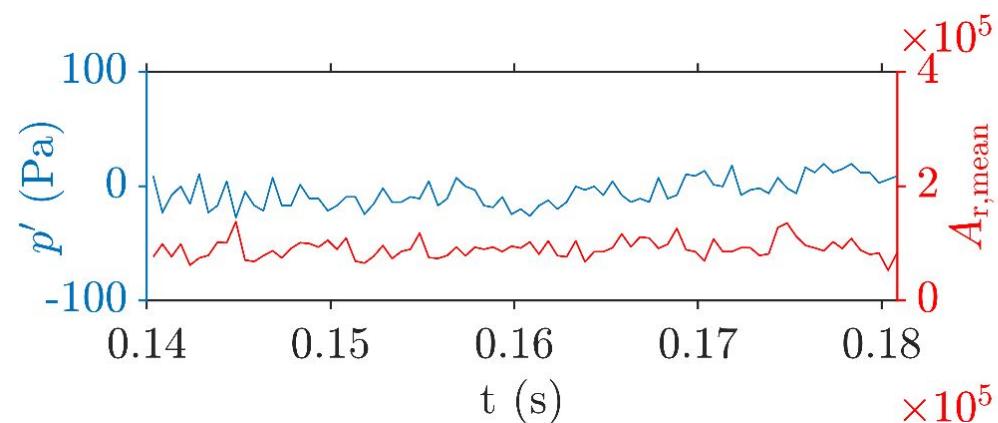


Average of all
inter-community interactions

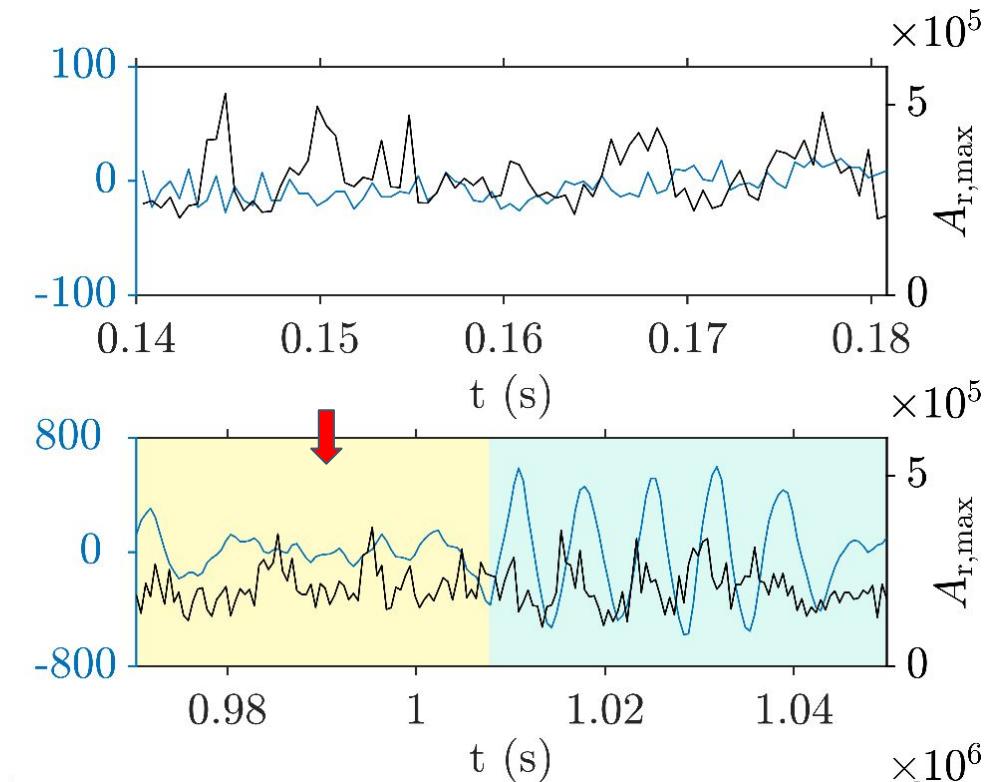
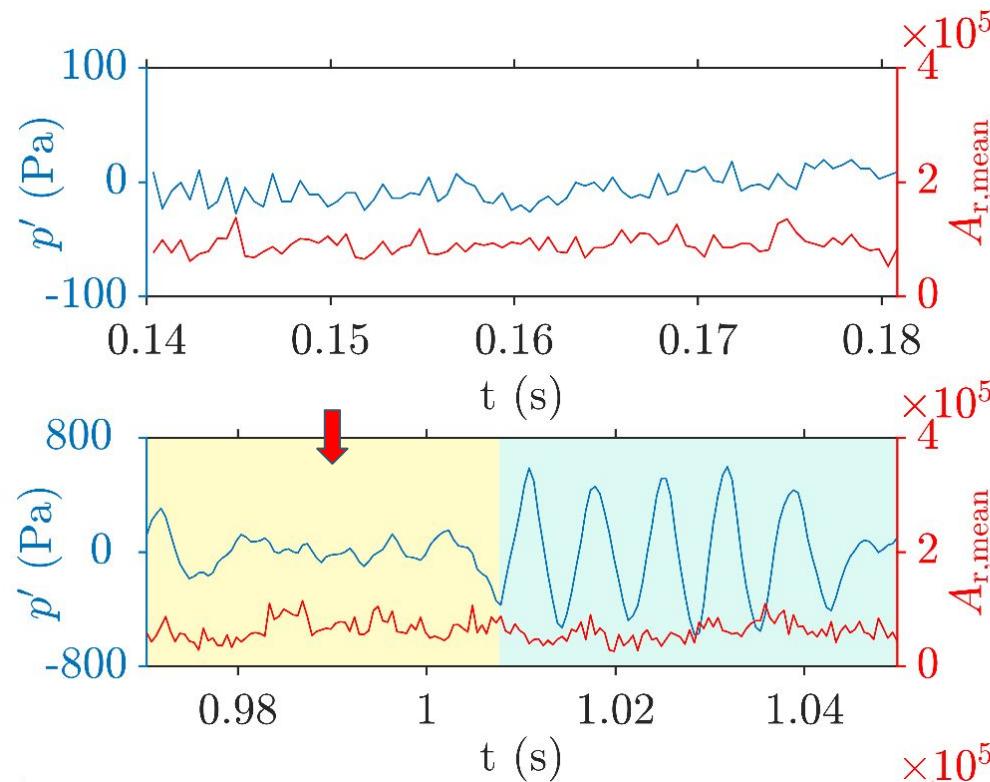
Maximum of all
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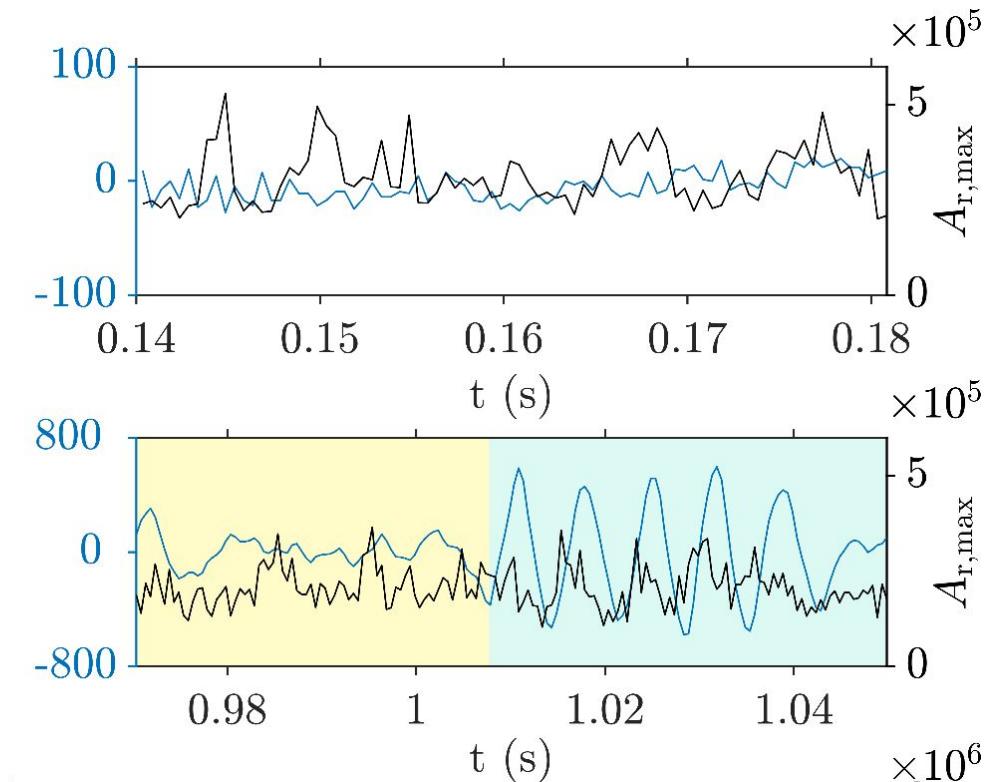
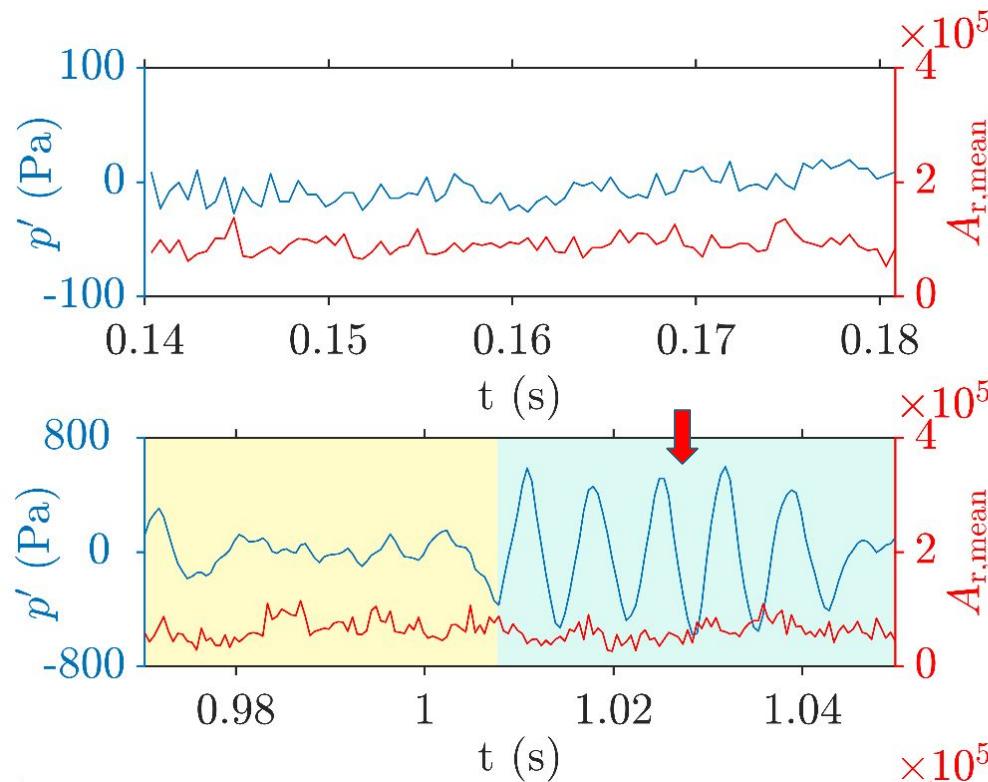
Combustion noise - aperiodic dynamics of networks measures



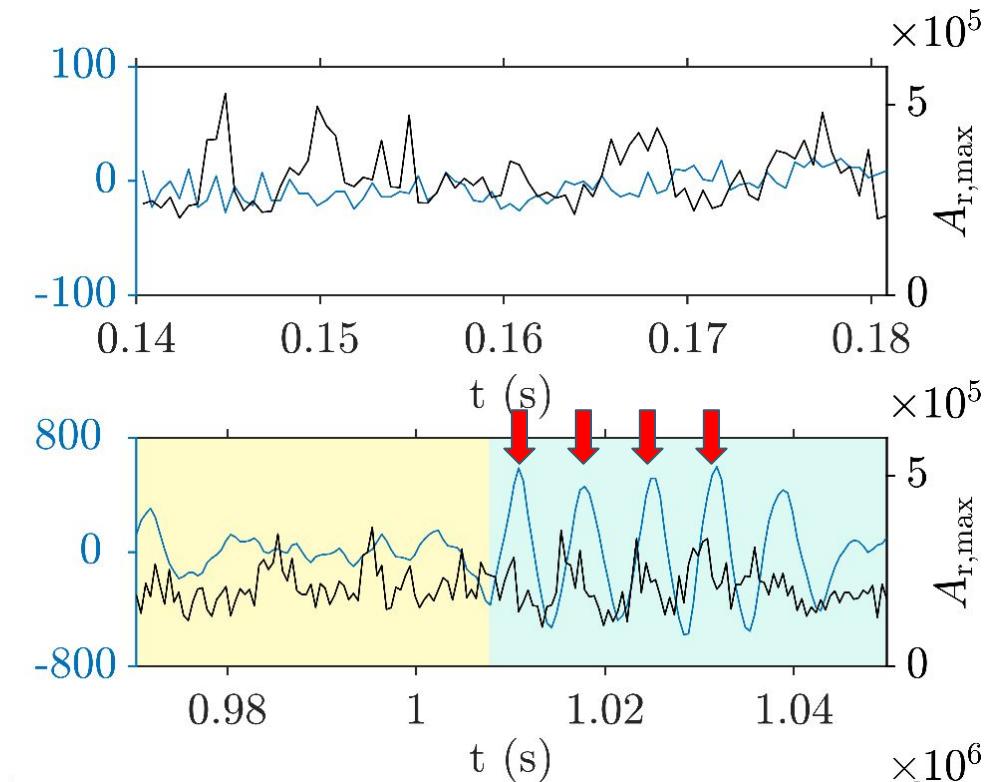
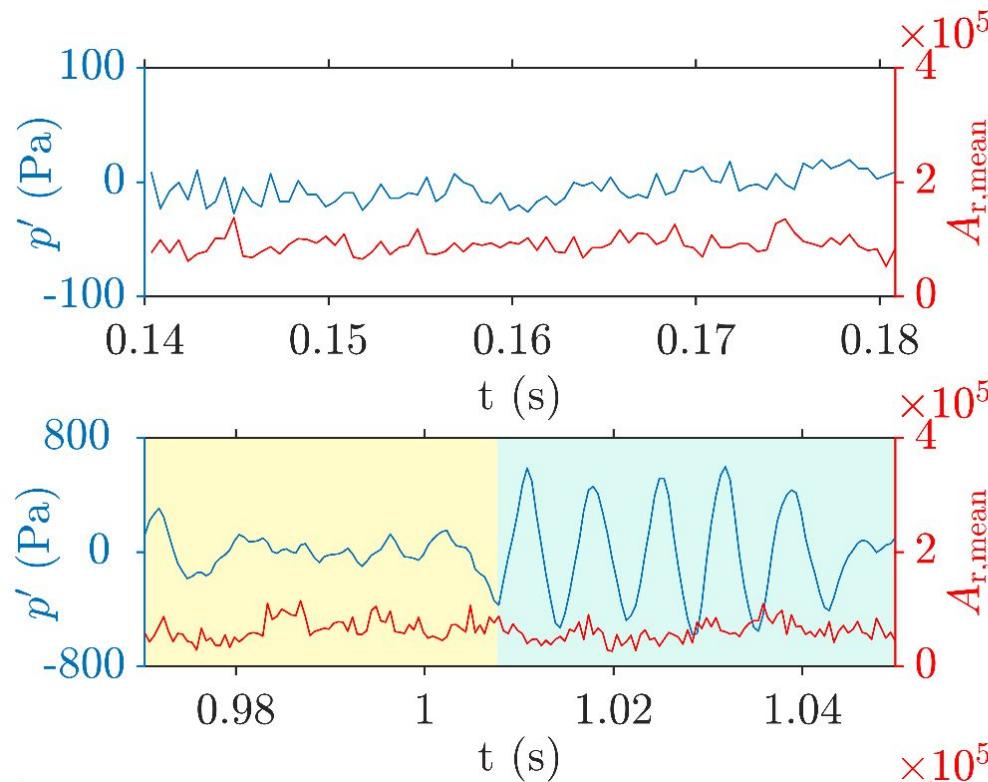
Intermittency - network measures are aperiodic during the aperiodic epoch of intermittency



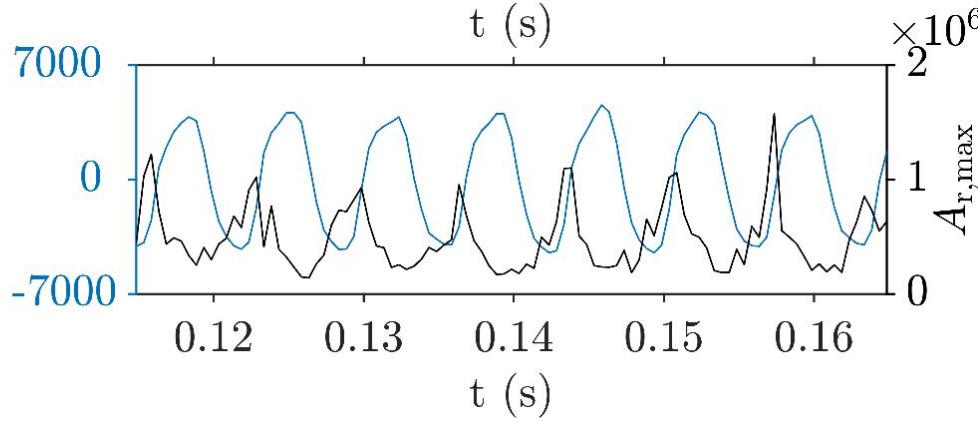
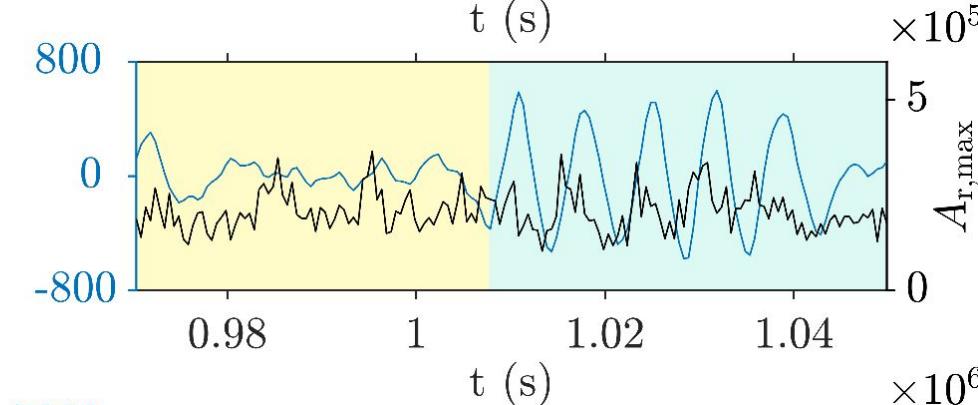
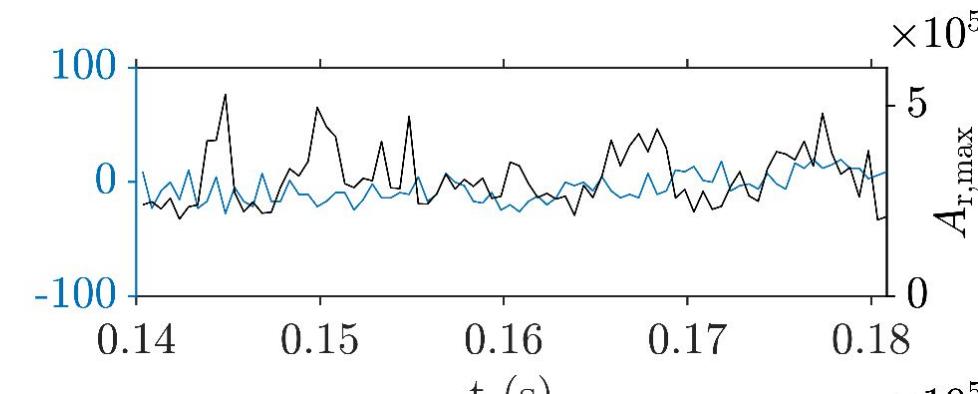
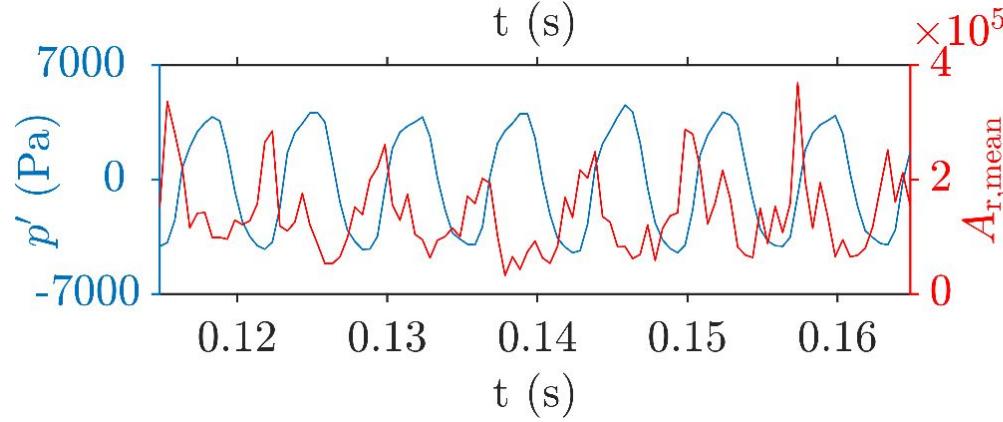
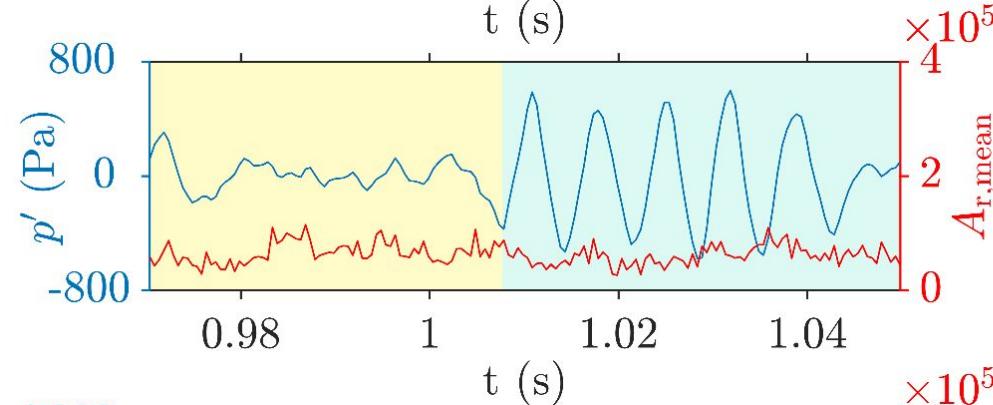
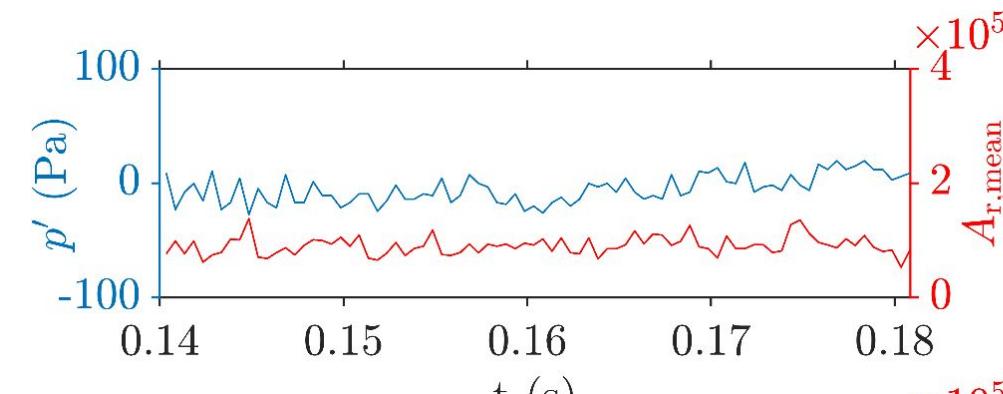
Intermittency - taking average of inter-community interactions smears out the periodic information of the flow field



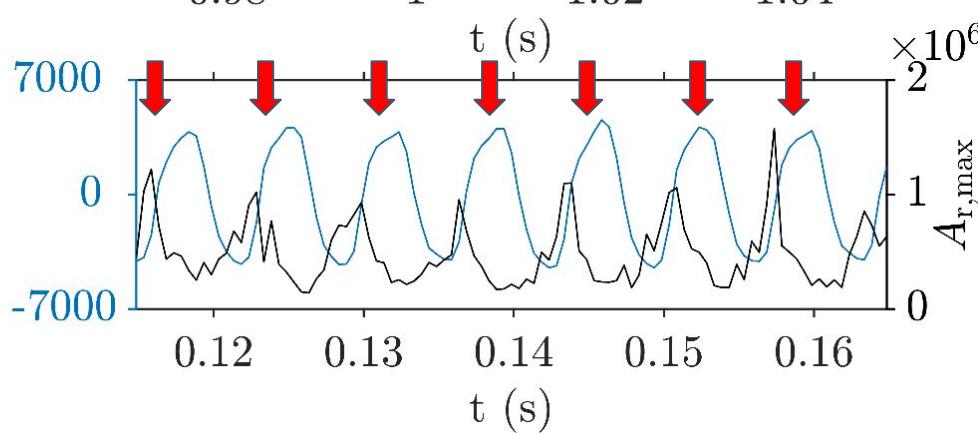
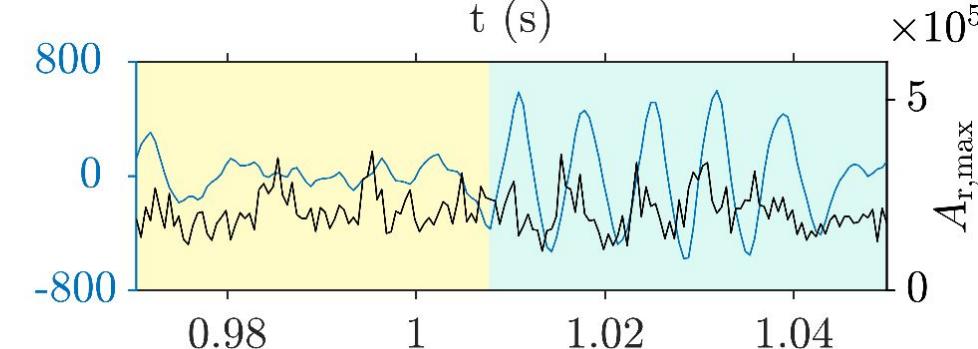
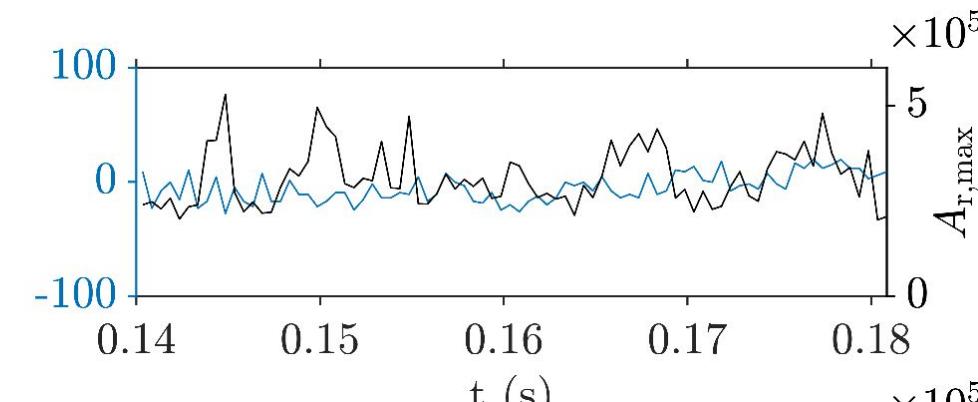
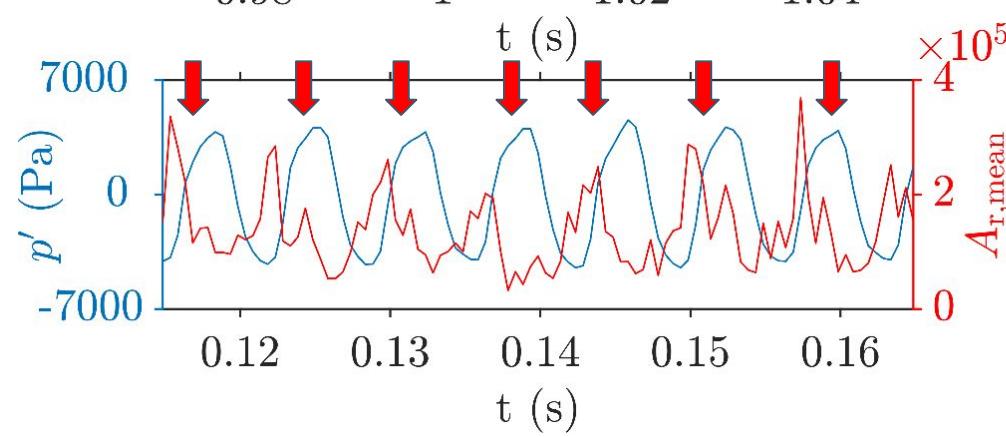
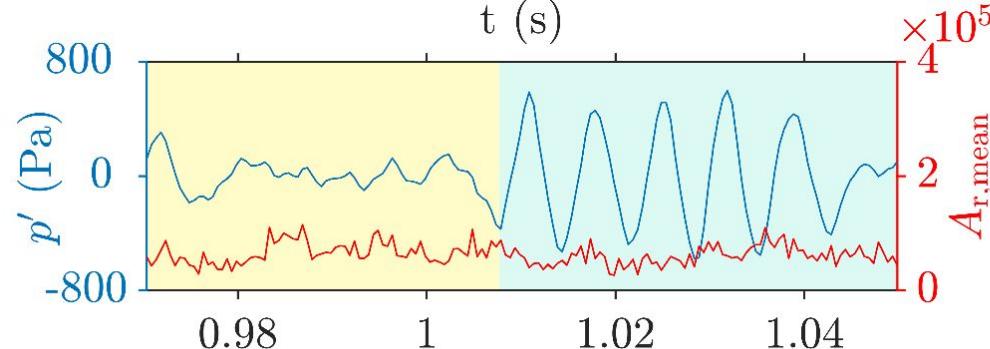
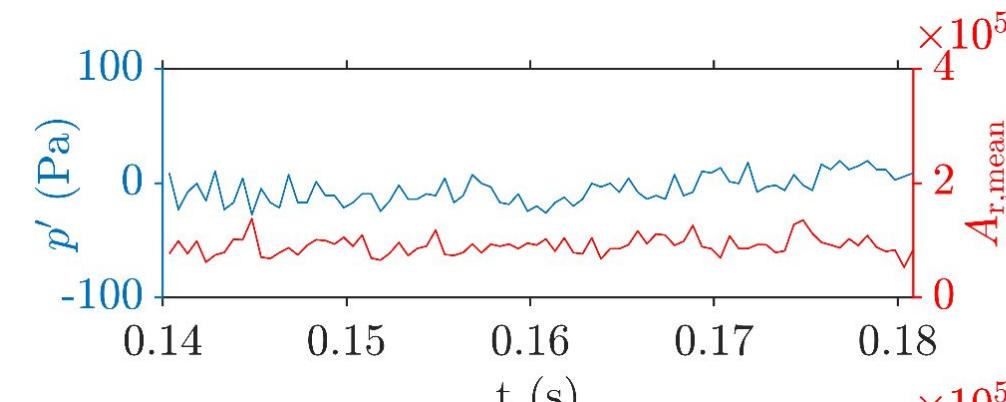
Intermittency - maximum inter-community interactions captures the periodicity of acoustics during the periodic epoch



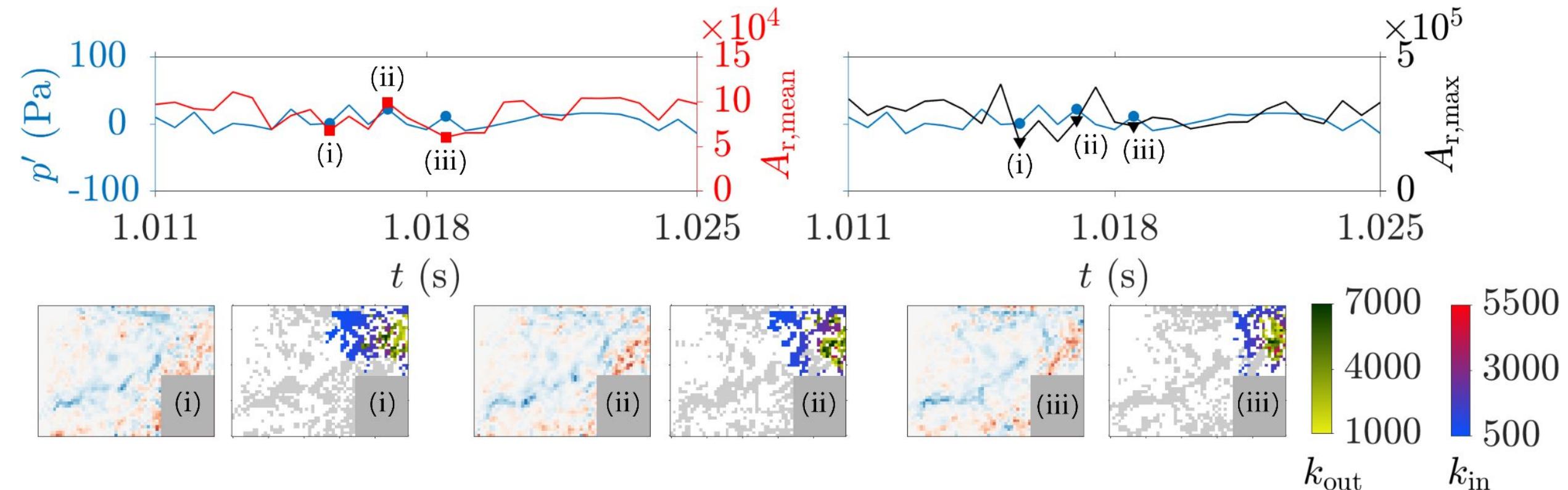
Thermoacoustic instability - network measures are periodic



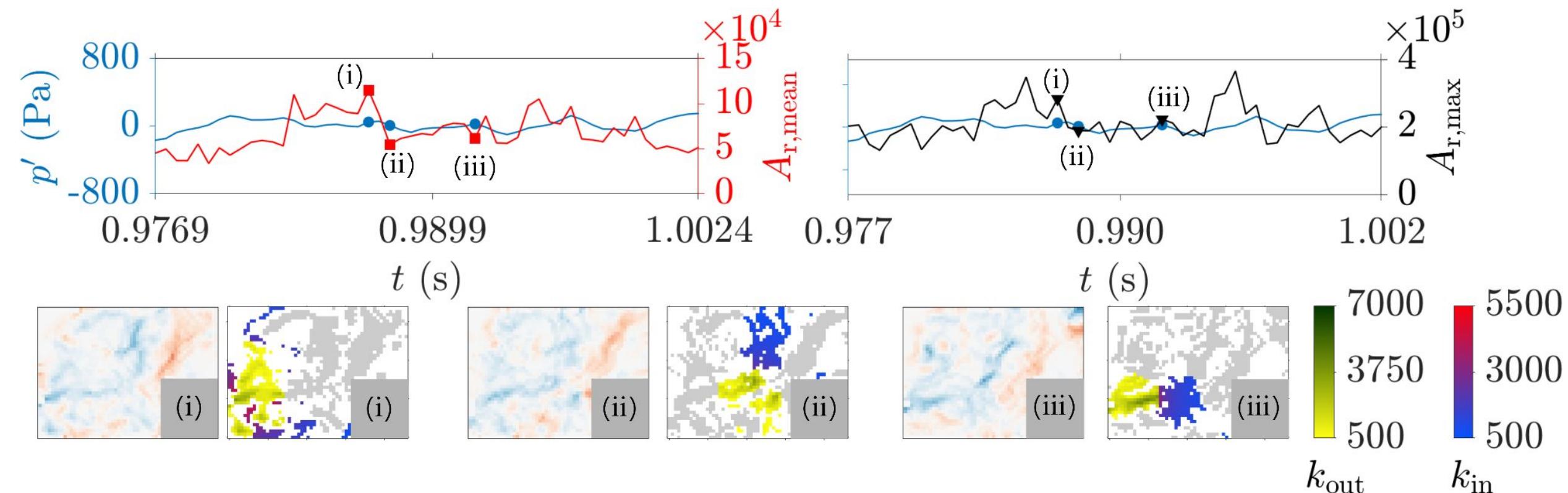
Thermoacoustic instability - significant delayed correlation between acoustics and network measures



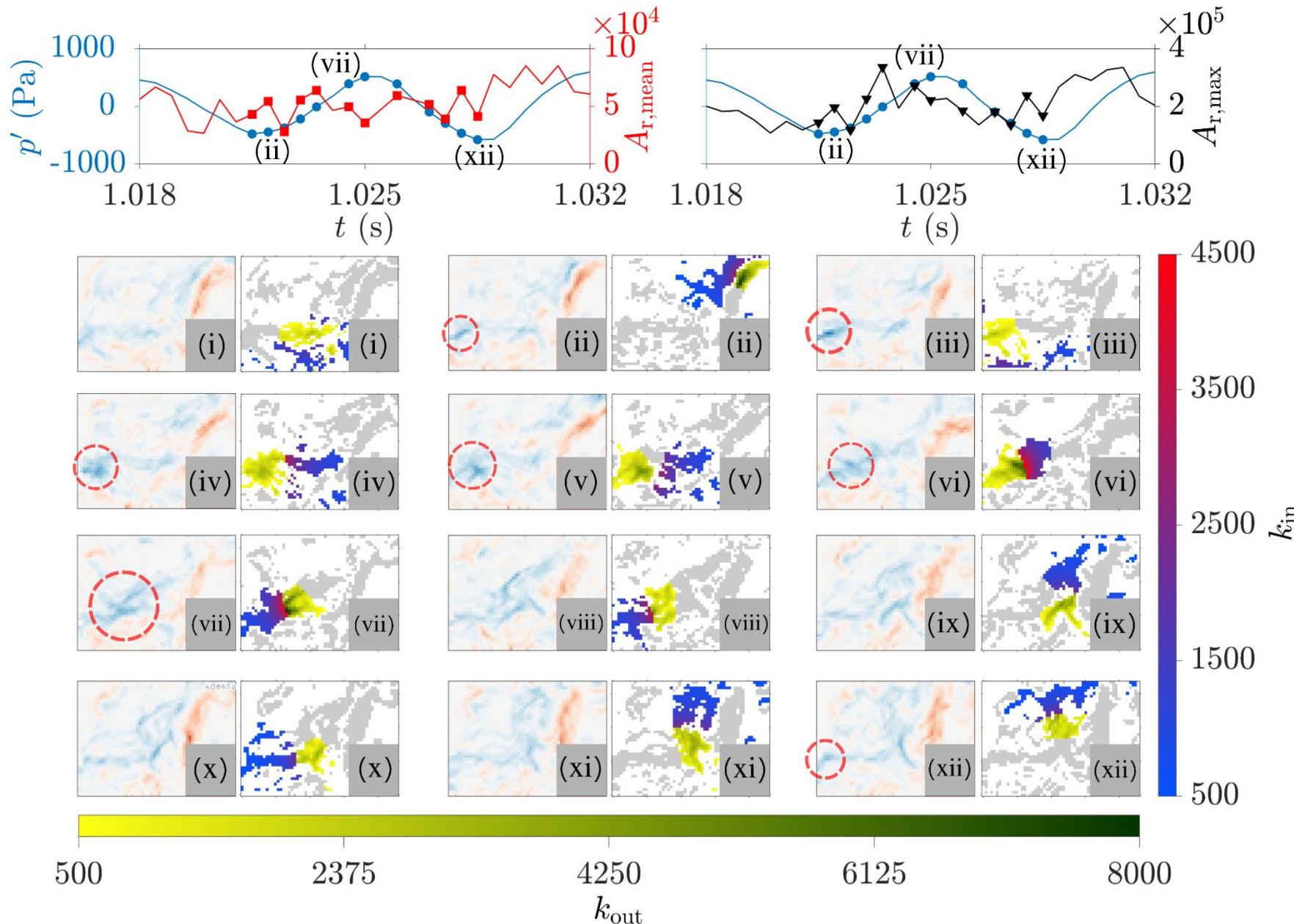
Combustion noise - significant vortex shedding from the upstream tip of bluff body



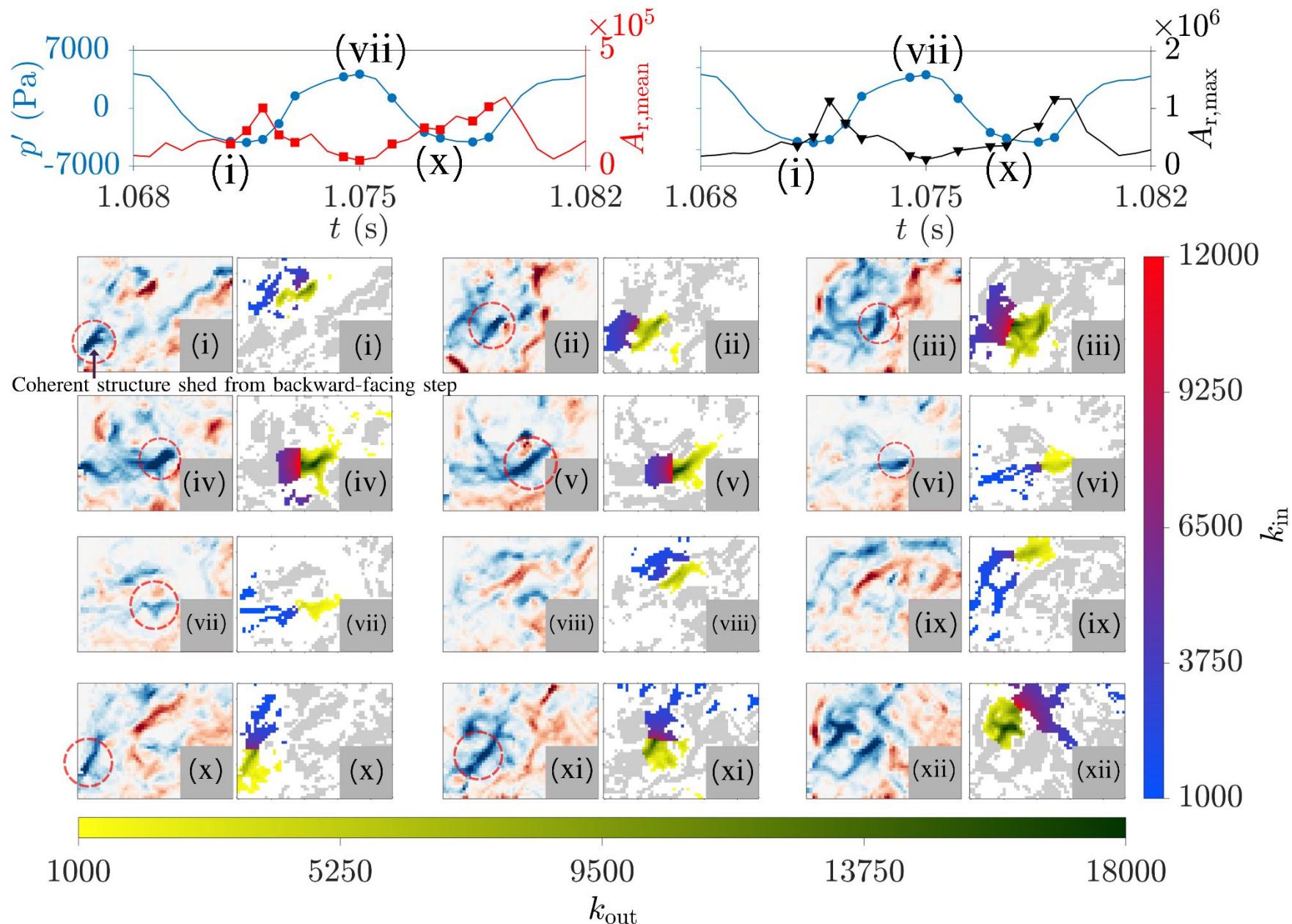
Aperiodic epoch of intermittency - aperiodic temporal variation of network measures



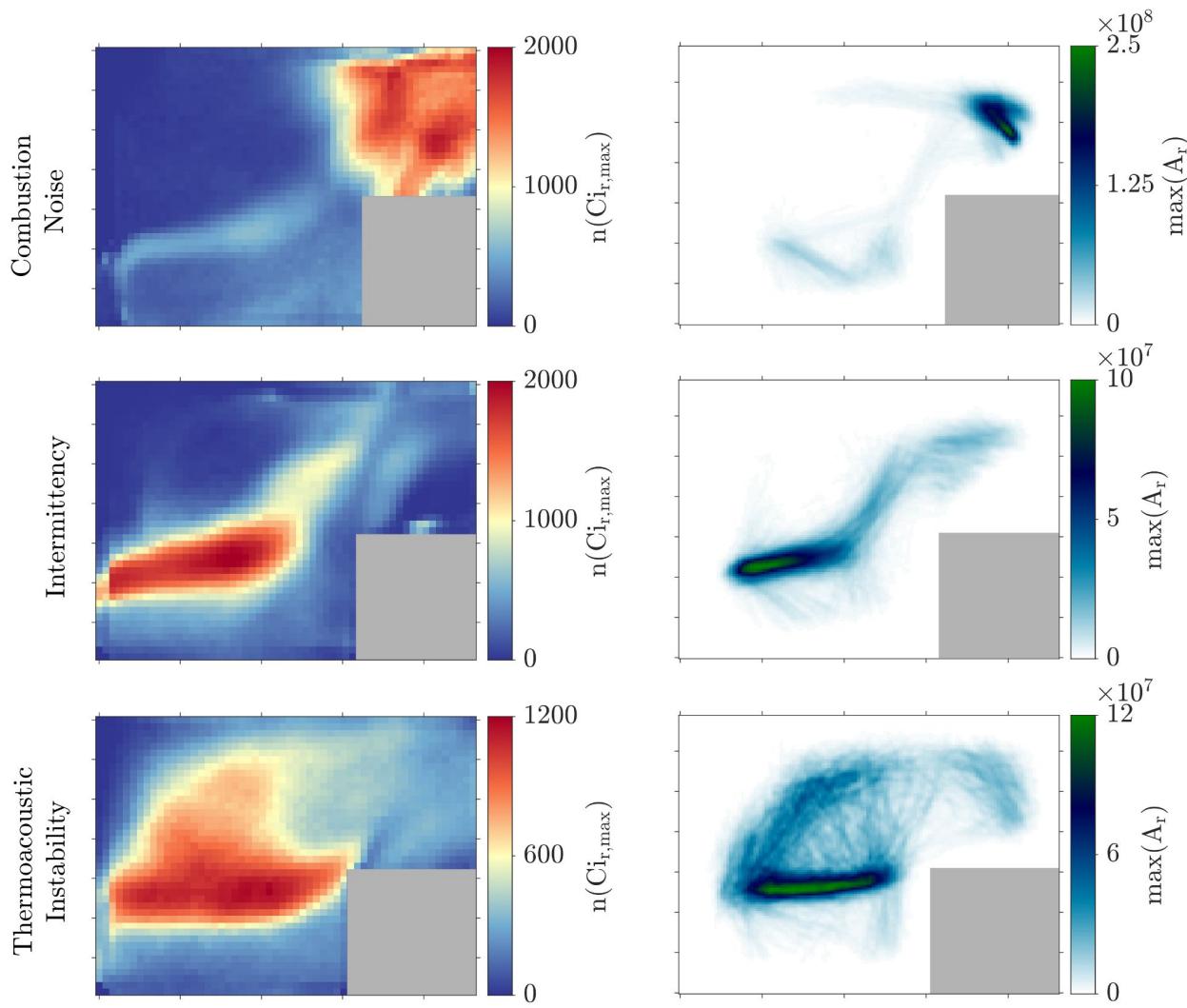
Periodic epoch of intermittency - periodic emergence of vortices



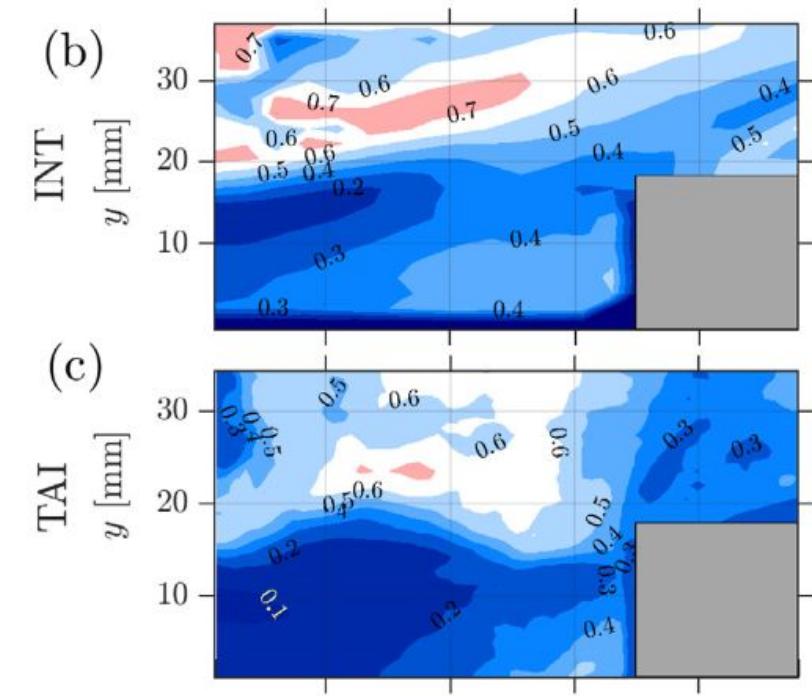
Thermoacoustic instability - periodic dynamics of network measures



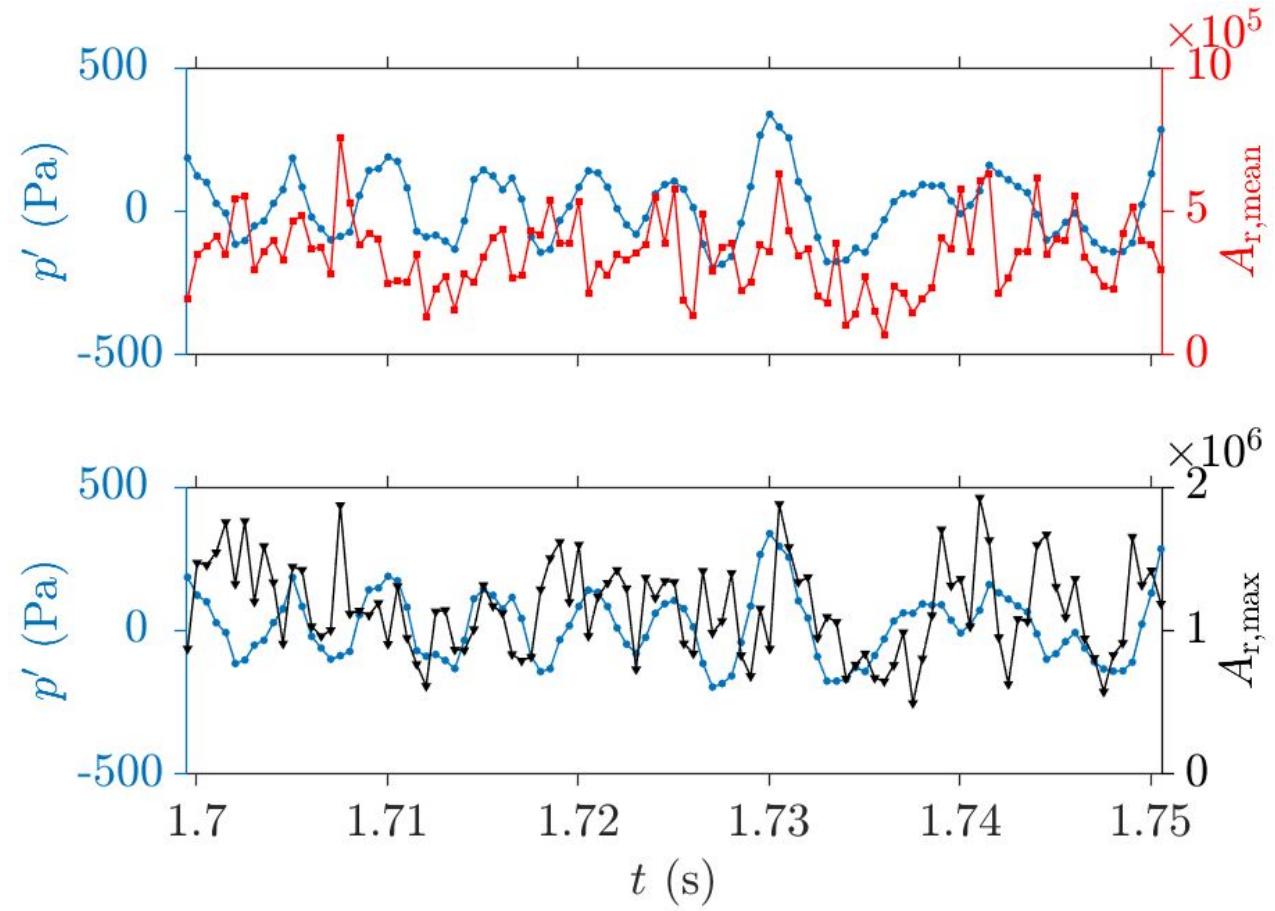
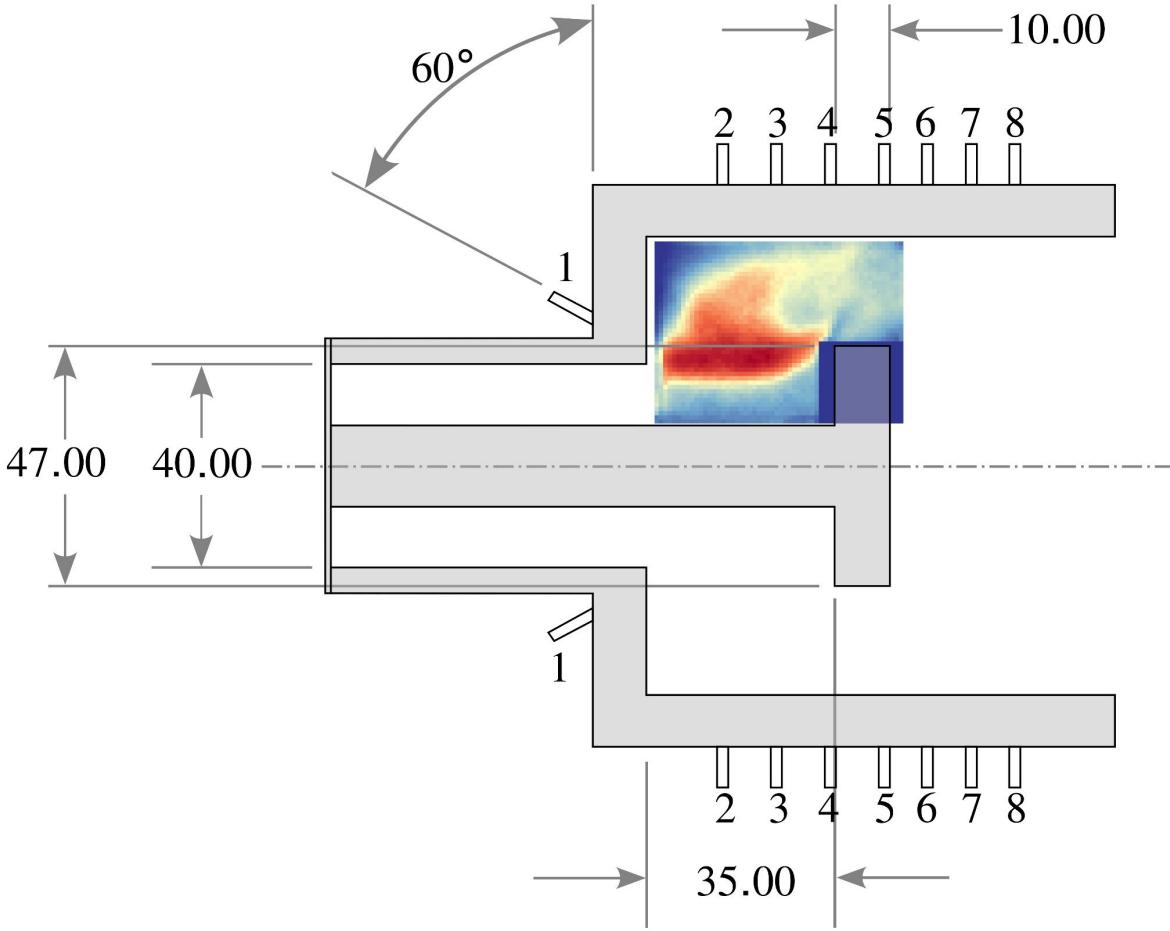
Critical regions - probability distribution of communities with largest inter-community interactions



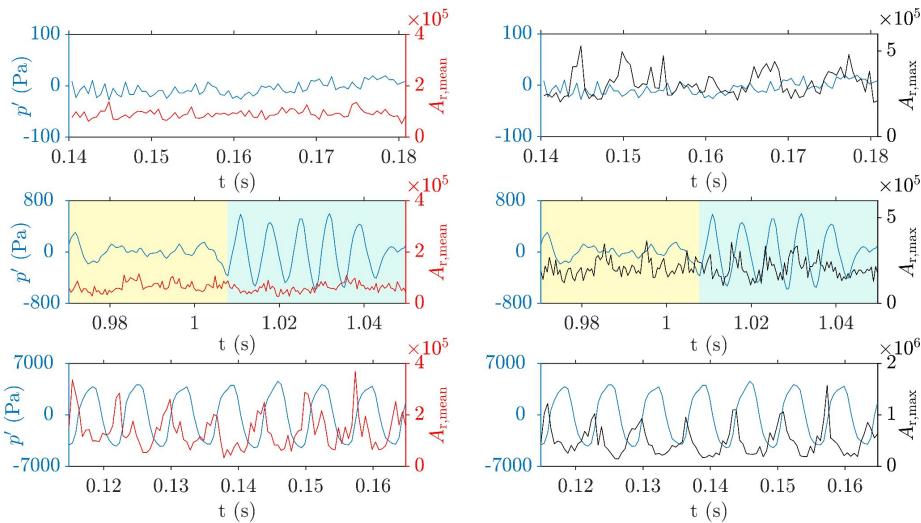
Hurst exponent (Roy et al.,
Combust. Flame, 2021)



Smart passive control - mitigation of thermoacoustic instability via air microjets

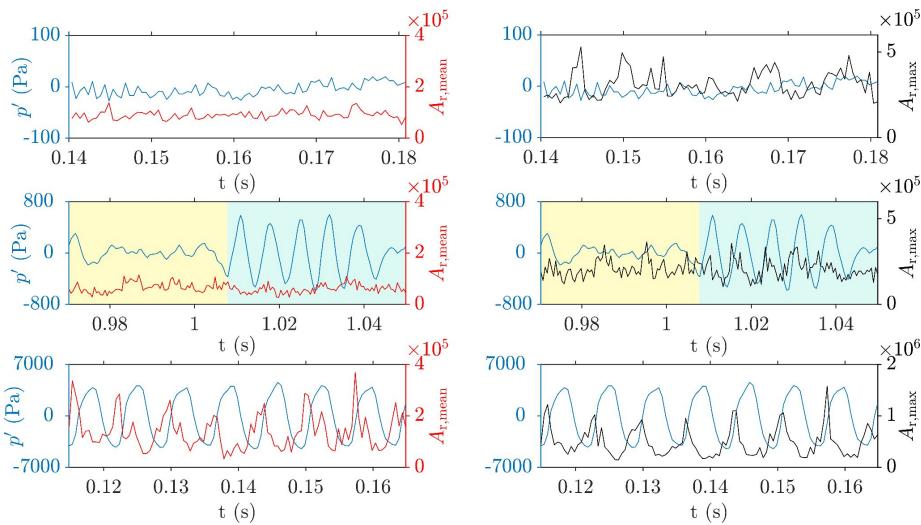


Summary

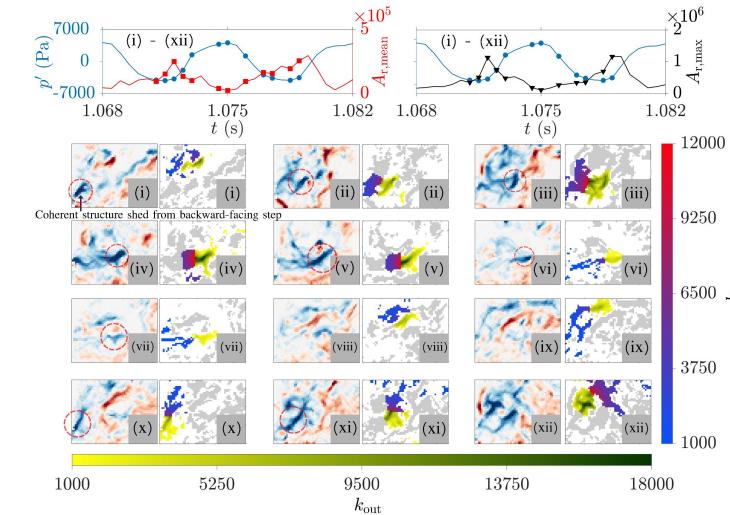


Interplay between
vortical
interactions and
acoustics
quantified via
vortical network
measures

Summary

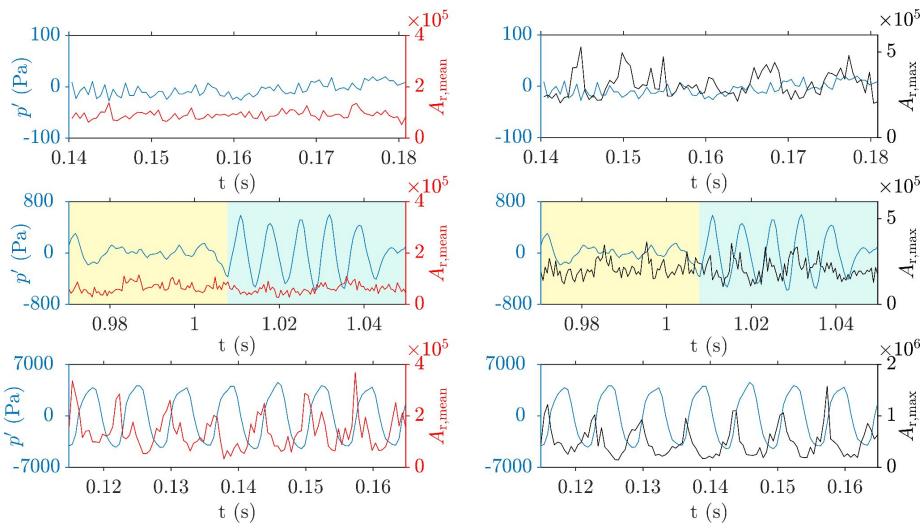


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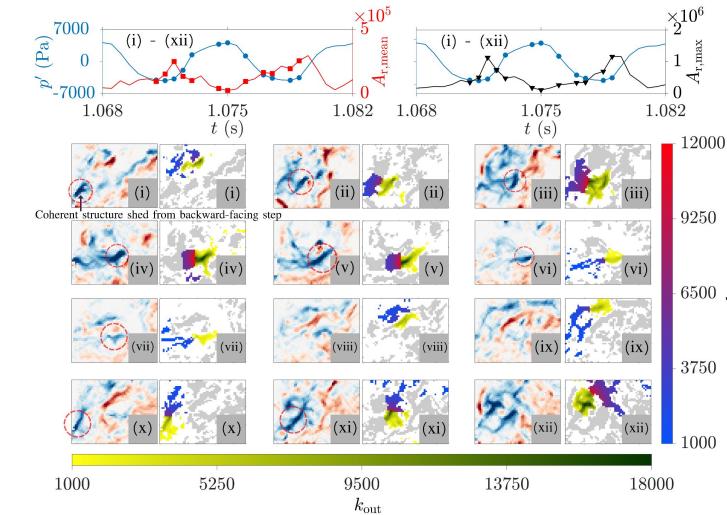


Temporal evolution
of influential
vortical
communities in the
reaction field of
the combustor

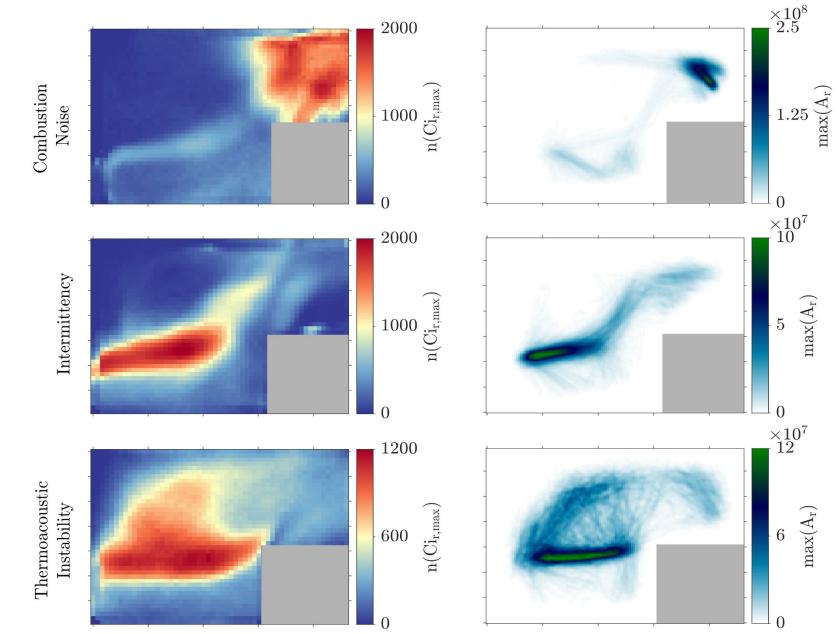
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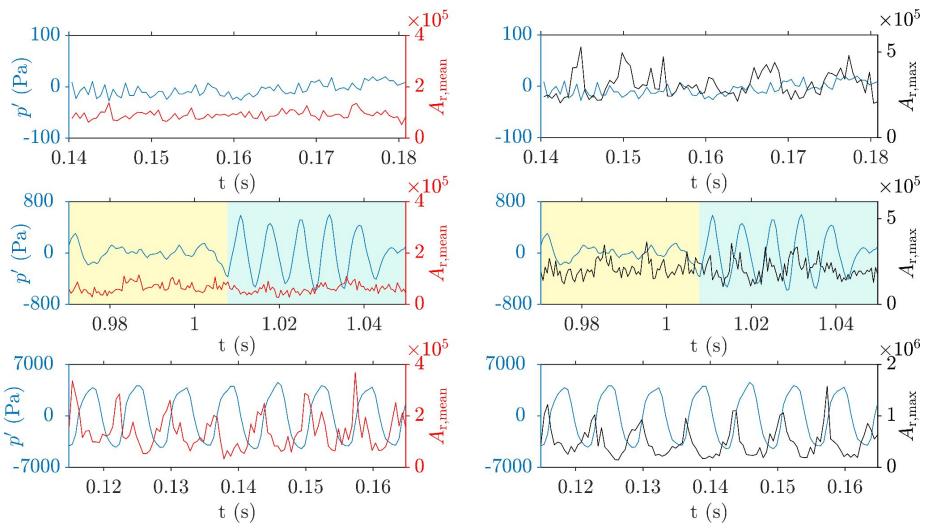


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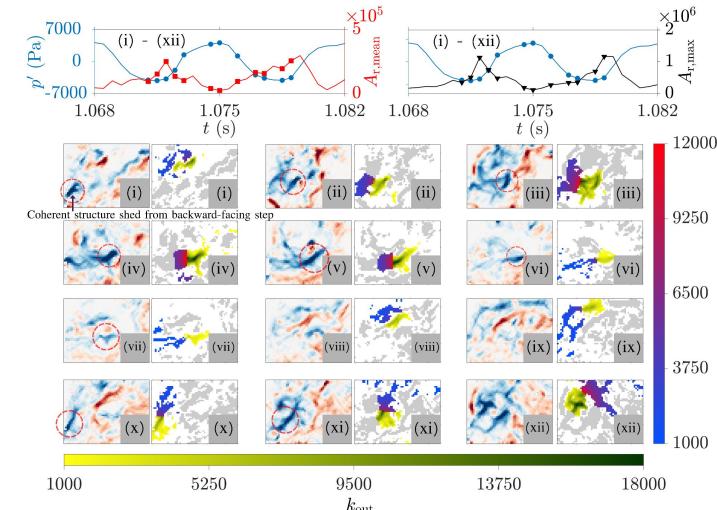


Spatial probability
of locating most
influential
communities during
the state of
thermoacoustic
instability

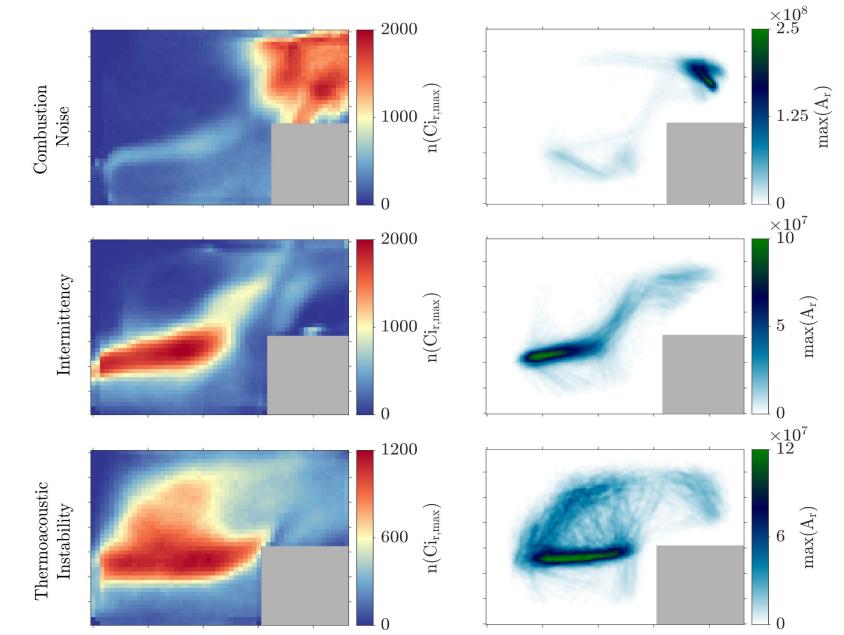
Summary



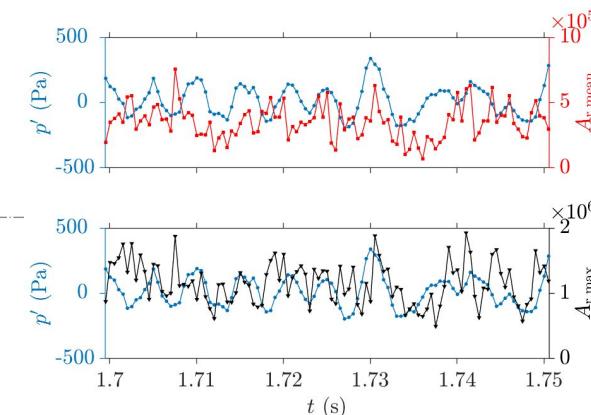
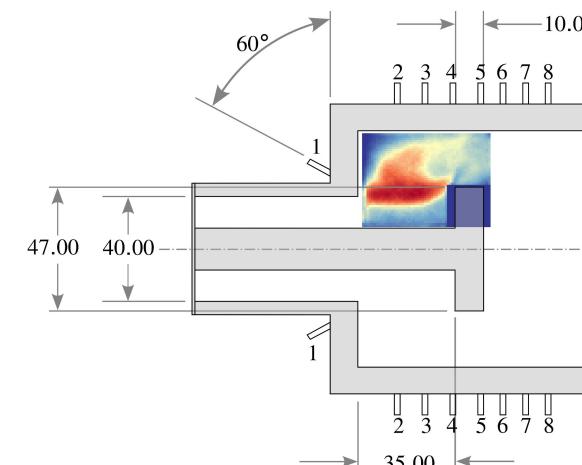
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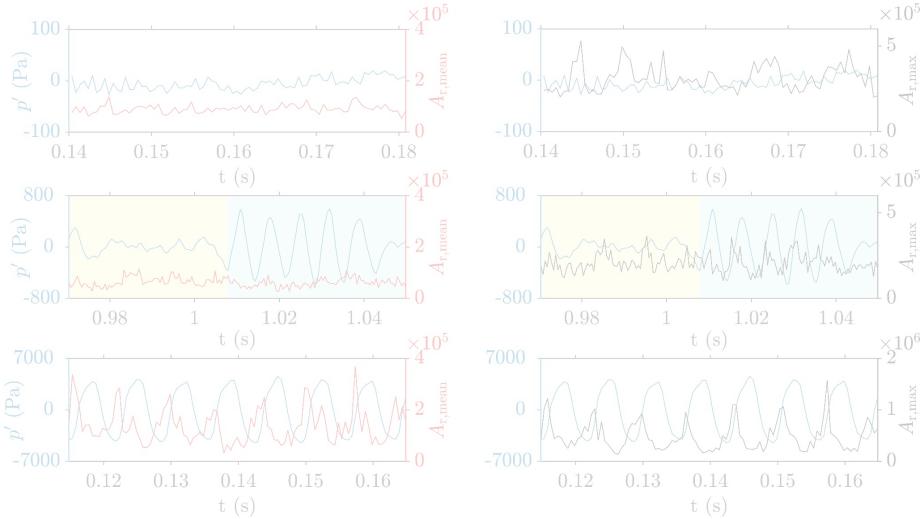
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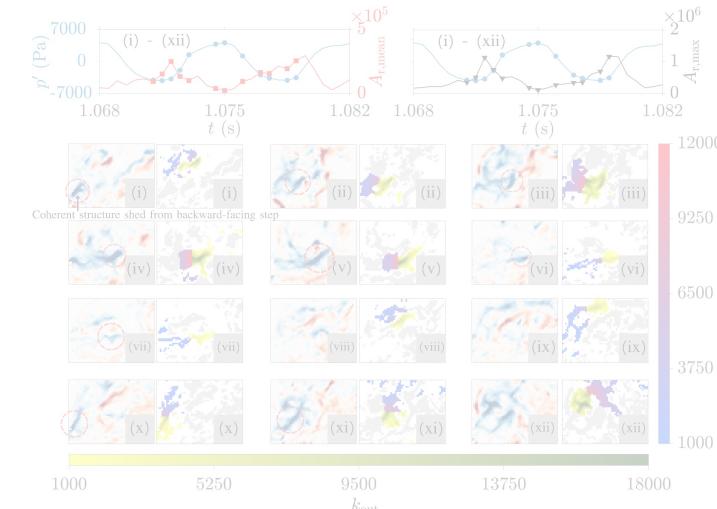
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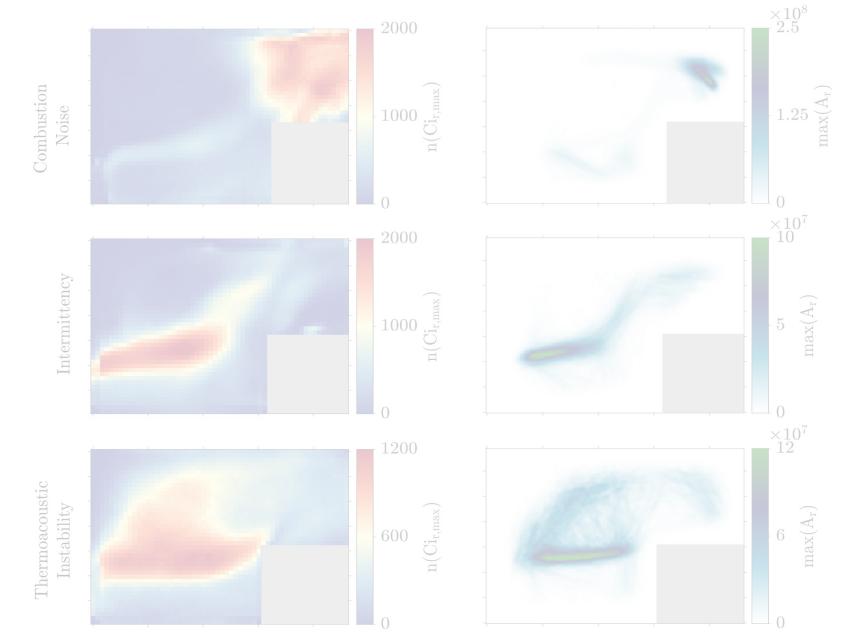


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Temporal evolution
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Thank you



Spatial probability
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