Assignment - 3 (UNIT-1)

Do all the questions-

1-Define with example

- (a)Orthogonal matrix
- (b)Hermitian matrix
- (c)Unitary matrix
- (d)Symmetric matrix
- (e) Triangular matrix

2-IF A =
$$\begin{bmatrix} 2 & 4 \\ 5 & 1 \end{bmatrix}$$
 and B = $\begin{bmatrix} 3 & 6 \\ 8 & 7 \end{bmatrix}$ find 3A+4B.

3-Find
$$A^2$$
 for the given matrix $A = \begin{bmatrix} 1 & 2 & 3 \\ 4 & 3 & 2 \\ 3 & 1 & 4 \end{bmatrix}$

4-Find the inverse of
$$\begin{bmatrix} 2 & 5 & 3 \\ 3 & 1 & 2 \\ 1 & 2 & 1 \end{bmatrix}$$

5-Solve the system of equation using matrices

$$3x+2y+4z=7$$
, $2x+y+z=4$, $x+3y+5z=2$

6-Find the inverse of the following matrix using elementary transformation

$$\begin{bmatrix} 1 & 3 & 3 \\ 1 & 4 & 3 \\ 1 & 3 & 4 \end{bmatrix}$$

7-Find the rank and nullity of the matrix
$$\begin{bmatrix} 1 & 2 & 3 \\ 1 & 4 & 2 \\ 2 & 6 & 5 \end{bmatrix}$$

8-Test the consistency of the system of given equations and if possible find the solution

$$4x-2y+6z = 8$$
, $x+y-3z = -1$, $15x-3y+9z = 21$

9-Find the characteristic roots and corresponding eigen vectors for the matrix

$$\begin{bmatrix} 2 & 2 & 1 \\ 1 & 3 & 1 \\ 1 & 2 & 2 \end{bmatrix}$$

- 10-Verify Cayley-Hamilton Theorem for the matrix $\mathbf{A}=\begin{bmatrix}2&-1&1\\1&2&1\\1&-1&2\end{bmatrix}$ and hence find A^{-1} .
- 11-Find the eigen values of the matrix A = $\begin{bmatrix} 0 & 1 & 2 \\ 1 & 0 & -1 \\ 2 & -1 & 0 \end{bmatrix}$

12-If A =
$$\begin{bmatrix} 1 & 2 & 0 \\ 3 & 1 & 5 \\ 2 & 4 & -3 \end{bmatrix}$$
 Find $A^3 + A^2 + A$.

- 13-Find transpose conjugate matrix A = $\begin{bmatrix} 1 2i & 2 + 3i & 3 4i \\ 4 + 5i & 5 6i & 6 + 7i \\ 8 & 7 8i & 9 \end{bmatrix}$
- 14-Prove (2,3,4), (0,1,2), (-1,1,-1) are linearly independent.
- 15-Reduce the matrix A = $\begin{bmatrix} 1 & 2 & -1 & 4 \\ 2 & 4 & 3 & 4 \\ 1 & 2 & 3 & 4 \end{bmatrix}$ to normal form and compute rank .

$$-1 - 2 6 - 7$$