8 PUZZLE PROBLEM

To design a graph search agent and understand the use of a hash table, queue in state space search.

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I. PROBLEM STATEMENT

- A. Write a pseudocode for a graph search agent. Represent the agent in the form of a flow chart. Clearly mention all the implementation details with reasons.
- B. Write a collection of functions imitating the environment for Puzzle-8.
- C. Describe what is Iterative Deepening Search.
- D. Considering the cost associated with every move to be the same (uniform cost), write a function which can backtrack and produce the path taken to reach the goal state from the source/initial state.
- E. Generate Puzzle-8 instances with the goal state at depth "d".
- F. Prepare a table indicating the memory and time requirements to solve Puzzle-8 instances (depth "d") using your graph search agent.

II. SOLUTIONS

1) Write a pseudo code for a graph search agent. Represent the agent in the form of a flow chart. Clearly mention all the implementation details with reasons.

cnode: Pointer to current node. gnode: Pointer to goal node.

Path: Contain path from root to goal.

Data: Data storage(Queue, Stack)(initiallized with root).

H1: To track explored node(Hash). H2: To track to explore nodes(Hash).

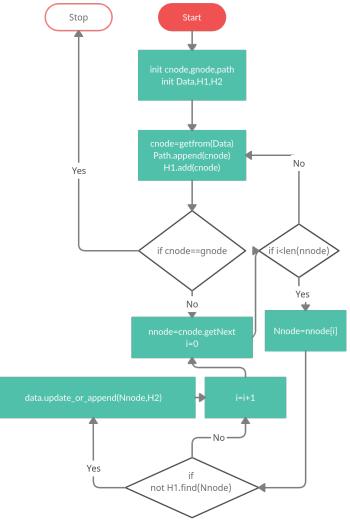
getfrom(Data): Gets one node out from data. Path.append(Node): Append one node in path.

H1.add(Node): Adds node in hash table.

cnode.getNext: List of all next possible states.

H1.find(Node): Return true when Node is in hash table. data.update_or_append(Node,H): Update node using H when Node.cost<Data.node.cost, else just add to data.

Fig. 1. Graph search agent



2) Write a collection of functions imitating the environment for Puzzle-8.

```
class Node:
      #Initilise the node
      def __init__(self,puzzle,tmp=0):
           self.children=list()
           self.parent=None
           self.puzzle=list()
           self.x=0
           self.setPuzzle(puzzle)
           self.tmp=tmp
           self.next=None
10
           #Children: contain nodes to children
           #Parent points to the parent of current
        node
           #Puzzle contain state
           #X contain location of blank
14
           #tmp contain cost to node from source
15
           #next used in hashing in case 2 nodes
16
       have same hashing
       #Inserts state into self state from given
       state
      def setPuzzle(self,puzzle):
18
           for i in range(len(puzzle)):
19
20
               self.puzzle.append(puzzle[i])
       #Check if current state is goal state
      def goalTest(self):
           return self.puzzle==goal
       #Perform right move
24
      def moveToRight(self,p,i):
25
           #p is state
26
           #i is current blank place
28
           if i%3<2:#Check if not right most</pre>
               pc=[]
29
               self.copyPuzzle(pc,p)
30
               temp=pc[i+1]
32
33
               pc[i+1]=pc[i]
               pc[i]=temp
34
35
               child=Node(pc,self.tmp+1)
36
               self.children.append(child)
37
38
               child.parent=self
39
       #Perform left move
      def moveToLeft(self,p,i):
40
           if i%3>0:
41
               pc=[]
42
43
               self.copyPuzzle(pc,p)
44
               temp=pc[i-1]
45
               pc[i-1]=pc[i]
46
47
               pc[i]=temp
48
               child=Node(pc,self.tmp+1)
49
               self.children.append(child)
50
               child.parent=self
51
       #Perform up move
52
53
      def moveToUp(self,p,i):
54
           if i-3>=0:
               pc=[]
55
               self.copyPuzzle(pc,p)
56
57
58
               temp=pc[i-3]
59
               pc[i-3]=pc[i]
               pc[i]=temp
60
61
               child=Node(pc,self.tmp+1)
62
63
               self.children.append(child)
64
               child.parent=self
       #Perform down move
65
66
       def moveToDown(self,p,i):
          if i+3<len(self.puzzle):</pre>
67
               pc=[]
```

```
self.copyPuzzle(pc,p)
69
                temp=pc[i+3]
72
                pc[i+3]=pc[i]
73
               pc[i]=temp
74
                child=Node(pc,self.tmp+1)
75
76
                self.children.append(child)
               child.parent=self
77
       #Print puzzle
78
79
       def printPuzzle(self):
           for i in range(len(self.puzzle)):
80
81
                if i%3==0:
                    print('\n')
82
               print (self.puzzle[i], end=" ")
83
       #Return true when p is same as current
84
       def isSamePuzzle(self,p):
85
86
           samePuzzle=True
           for i in range(len(p)):
87
                if self.puzzle[i]!=p[i]:
88
89
                   samePuzzle=False
90
           return samePuzzle
       #Explore current node
91
92
       def expandNode(self):
           #get position of blank tile
93
94
           for i in range(len(self.puzzle)):
95
                if self.puzzle[i] == 0:
96
                    self.x=i
           #make move for them
97
           self.moveToRight(self.puzzle, self.x)
98
QQ.
           self.moveToLeft(self.puzzle,self.x)
100
           self.moveToUp(self.puzzle,self.x)
           self.moveToDown(self.puzzle,self.x)
101
       #Copy contents from b to a
102
       def copyPuzzle(self,a,b):
103
104
           for i in range(len(b)):
               a.append(b[i])
105
#PriorityQueue is used to get smallest always
  from queue import PriorityQueue
108 #To return first element of given parameter
109 def data(n):
           return n[0]
110
   #appends path from n to root in path
111
def pathTrace(path,n):
           print("\nTracing path...")
114
           current=n
           path.append(current)
115
           while (current.parent!=None):
116
               current=current.parent
               path.append(current)
118
119 #Heuristic function
  def heuristic_for_misplaced_tiles(p):
120
       cost = 0
121
       for i in range(len(p)):
           if p[i]!=goal[i] and p[i]!=0:
124
               cost+=1
       return cost
125
126 #BestFirst search
   class BestFirst:
127
       #Algo starts here
128
129
       def bestfirst(self,root):
           pathToSolution=[]
130
           #To Explore and explored
131
132
           openList=[]
           closedList=[]
133
           #Append root in to explore
134
135
           openList.append((0,root))
           #Goal flag
136
           goalFound=False
           #Till toExplore is not empty or goal
138
       not found
           while len(openList)!=0 and goalFound==
139
       False:
```

```
#Sort to explore list as per data
       attribute
               openList=sorted(openList, key=data)
141
               #get minimum
142
               _,currentNode=openList[0]
143
               #Append to explored
144
               closedList.append(currentNode)
145
               #Remove from to explore
146
               openList.pop(0)
147
148
               #Explore current node
               currentNode.expandNode()
149
               #stores cost, node pair
150
               mis=[]
151
               for i in range(len(currentNode.
       children)):
                   #append child node with its
       cost from goal node to children node
                   mis.append((
154
       heuristic_for_misplaced_tiles(currentNode.
       children[i].puzzle),currentNode.children[i
       ]))
155
               #Process all children of explored
       node
               for i in range(len(currentNode.
156
       children)):
                    #Take ith child
157
                    currentChild=currentNode.
158
       children[i]
159
                    #Check if its a goal
                    if currentChild.goalTest():
                        #Trace path from current
161
       node to root and append it in
       pathToSolution
                        print("\nGoal Found")
162
                        goalFound=True
163
                        pathTrace(pathToSolution,
164
       currentChild)
165
                   #If child node is not yet
166
       explored or in to explore then add it to,
       to explore list
                    if (self.contains(openList,
167
       currentChild, "gg") == False and self.contains
       (closedList, currentChild, "ff") ==False):
                       openList.append(mis[i])
168
           #Return path from goal to root (Reverse)
169
           return pathToSolution
170
       #Check if lis(list) contains c(Node) with s
       (mode)
       def contains(self, lis, c, s):
           #Flag
           contains=False
174
           for i in range(len(lis)):
               #open list have cost and node
176
               if s=="gg":
                   _, l=lis[i]
178
179
               #closed list only have node
180
               else:
                   l=lis[i]
181
               #Return true when 1 and c have same
        puzzle(State) attribute
183
               if l.isSamePuzzle(c.puzzle) == True:
                   contains=True
184
           #Return flag
185
           return contains
187 #Execution starts here
188 #Source
puzzle=[1,2,4,3,0,5,7,6,8]
190 #Goal
goal=[0,1,2,3,4,5,6,7,8]
192 root=Node(puzzle)
ui=BestFirst()
194 solution=ui.bestfirst(root)
195 #Solution is from goal to root so reverse it
```

Listing 1. Collection of functions for environment for puzzle-8

Output steps using BestFirst

```
2 Goal Found
4 Tracing path...
5 1 2 4
6 3 0 5
7 7 6 8
9 *****Next move******* 0
10 1 2 4
11 3 5 0
12 7 6 8
13
14 *****Next move******* 1
15 1 2 0
16 3 5 4
17 7 6 8
18
19 ******Next move******* 2
20 1 0 2
21 3 5 4
22 7 6 8
24 *****Next move******* 3
25 0 1 2
26 3 5 4
27 7 6 8
29 ******Next move******* 4
30 3 1 2
31 0 5 4
32 7 6 8
33
34 ******Next move******* 5
35 3 1 2
36 5 0 4
37 7 6 8
39 ******Next move******* 6
40 3 1 2
41 5 6 4
42 7 0 8
44 *****Next move******* 7
45 3 1 2
46 5 6 4
47 0 7 8
49 *****Next move******* 8
50 3 1 2
51 0 6 4
52 5 7 8
53
54 *****Next move******* 9
55 3 1 2
56 6 0 4
57 5 7 8
59 ******Next move******* 10
60 3 1 2
61 6 4 0
```

```
62 5 7 8
64 *****Next move******* 11
65 3 1 2
66 6 4 8
67 5 7 0
69 ****** Next move****** 12
70 3 1 2
71 6 4 8
72 5 0 7
74 *****Next move******* 13
75 3 1 2
76 6 4 8
77 0 5 7
79 ******Next move******* 14
80 3 1 2
81 0 4 8
82 6 5 7
83
84 *****Next move******* 15
85 3 1 2
86 4 0 8
87 6 5 7
89 *****Next move****** 16
90 3 1 2
91 4 5 8
92 6 0 7
93
94 *****Next move******* 17
95 3 1 2
96 4 5 8
97 6 7 0
99 *****Next move******* 18
100 3 1 2
101 4 5 0
102 6 7 8
104 *****Next move******* 19
105 3 1 2
106 4 0 5
107 6 7 8
109 ***** Next move***** 20
110 3 1 2
111 0 4 5
112 6 7 8
113
114 *****Next move****** 21
115 0 1 2
116 3 4 5
117 6 7 8
```

3) Describe what is Iterative Deepening Search.

We have BFS but it takes lot of memory to execute, but will give solution no matter what.

Then we have DFS which require less memory to execute, but it may or may not give solution.

Idea is to combine BFS algorithm's reliability and DFS algorithm's memory consumption. In iterative deepening search, we do level wise DFS.

First perform DFS for level 0 which is root and check if it is matching to our goal, if not then we just increase level to 1.

Perform the DFS up to level 1, when next node is out of graph then we stop. [2]

Lets take one example:

Suppose our goal is n10 node, At start we go with level 0 DFS, where we encounter only n1 and we check if n1 is equal to goal(n10), which is not so we go to level level 1.

At level 1 we encounter 4 nodes which are n1,n2,n3 and n4, so apply DFS on n1, which is to compare if n1 is goal then n2, n3 and n4 respectively. As no goal is found so we go to next level.

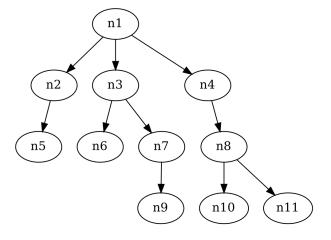
For level 2 we apply DFS on n1, so comparison sequence will be like this, n1,n2,n5,n3,n6,n7,n4,n8. Here also we dont find goal so head to next level.

For level 3 we apply DFS on n1, so comparison sequence will be like this, n1,n2,n5,n3,n6,n7,n9,n4,n8,n10. Here we find n10 which is goal state so we can stop here.

Advantages:

- 1. Always finds optimal solution as it scans by level.
- 2. Less memory required as its a level wise DFS.

Fig. 2. Tree for example



4) Considering the cost associated with every move to be the same (uniform cost), write a function which can backtrack and produce the path taken to reach the goal state from the source/ initial state.

```
class Node:
      #Initilise the node
      def __init__(self,puzzle,tmp=0):
           self.children=list()
           self.parent=None
           self.puzzle=list()
           self.x=0
           self.setPuzzle(puzzle)
           self.tmp=tmp
0
           self.next=None
10
           #Children: contain nodes to children
           #Parent points to the parent of current
       node
           #Puzzle contain state
13
           #X contain location of blank
14
           #tmp contain cost to node from source
15
           #next used in hashing in case 2 nodes
16
      have same hashing
      #Inserts state into self state from given
       state
18
      def setPuzzle(self,puzzle):
19
           for i in range(len(puzzle)):
20
               self.puzzle.append(puzzle[i])
      #Check if current state is goal state
21
      def goalTest(self):
23
           return self.puzzle==goal
      #Perform right move
24
25
      def moveToRight(self,p,i):
           #p is state
26
           #i is current blank place
           if i%3<2: #Check if not right most
               pc=[]
29
               self.copyPuzzle(pc,p)
30
31
32
               temp=pc[i+1]
               pc[i+1]=pc[i]
33
               pc[i]=temp
34
35
36
               child=Node(pc, self.tmp+1)
37
               self.children.append(child)
               child.parent=self
38
      #Perform left move
39
40
      def moveToLeft(self,p,i):
           if i%3>0:
41
42.
               pc=[]
               self.copyPuzzle(pc,p)
43
44
45
               temp=pc[i-1]
46
               pc[i-1]=pc[i]
               pc[i]=temp
47
48
               child=Node(pc,self.tmp+1)
49
               self.children.append(child)
50
51
               child.parent=self
      #Perform up move
52
      def moveToUp(self,p,i):
53
           if i-3>=0:
54
               pc=[]
55
               self.copyPuzzle(pc,p)
56
57
               temp=pc[i-3]
58
               pc[i-3]=pc[i]
59
60
               pc[i]=temp
61
               child=Node(pc,self.tmp+1)
62.
63
               self.children.append(child)
               child.parent=self
64
      #Perform down move
```

```
def moveToDown(self,p,i):
            if i+3<len(self.puzzle):</pre>
68
                []=pg
69
                self.copyPuzzle(pc,p)
 70
71
                temp=pc[i+3]
72
                pc[i+3]=pc[i]
73
                pc[i]=temp
74
                child=Node(pc,self.tmp+1)
75
                self.children.append(child)
76
77
                child.parent=self
78
       #Print puzzle
       def printPuzzle(self):
79
            for i in range(len(self.puzzle)):
80
                if i%3==0:
81
                    print('\n')
82
                print (self.puzzle[i], end=" ")
83
       #Return true when p is same as current
84
       def isSamePuzzle(self,p):
85
86
            samePuzzle=True
87
            for i in range(len(p)):
                if self.puzzle[i]!=p[i]:
88
                    samePuzzle=False
89
            return samePuzzle
90
       #Explore current node
91
       def expandNode(self):
92
93
            #get position of blank tile
            for i in range(len(self.puzzle)):
94
                if self.puzzle[i] == 0:
95
96
                    self.x=i
            #make move for them
97
            self.moveToRight(self.puzzle,self.x)
98
            self.moveToLeft(self.puzzle, self.x)
            self.moveToUp(self.puzzle,self.x)
100
            self.moveToDown(self.puzzle,self.x)
101
102
       #Copy contents from b to a
       def copyPuzzle(self,a,b):
103
            for i in range(len(b)):
104
                a.append(b[i])
105
106
107 #For hashing
108 from collections import OrderedDict
109 dict=OrderedDict
{\ensuremath{\text{HG}}}\textsc{o} #Get all nodes in path from n to root node
def pathTrace(path, n):
           current=n
            path.append(current)
114
            while (current.parent!=None):
                current=current.parent
115
                path.append(current)
116
   #Class to perform uniform search
117
  class uninformedSearch:
118
       #Hashing function
119
       def hashing(self,x):
120
            hash_val=0
            # simply sum of index*state
            for i in range(len(x)):
                hash_val += (i+1) **x[i]
124
            return hash_val
125
126
       #Perform uniform search
127
       def bfs(self,root):
            #No of explored nodes
128
129
            explored=0
            #No of children faced
130
131
            child=0
132
            #No of children put in memory at start
       root is in memory
            childm=1
133
134
            #Maximum memory needed for program
135
            maxm=childm
136
            #Stored solution path here
137
            pathToSolution=[]
```

```
#2 hash tables (Dictionary)
                                                                                   childm+=1
138
                                                           190
           #To explore
                                                                                    #Update maxm required
139
                                                           191
           openList=dict()
                                                                                    if childm>maxm:maxm=childm
140
                                                           192
141
           #Explored
                                                           193
                                                                       return pathToSolution, explored, child,
           closedList=dict()
142
                                                                  maxm
           #Adding root to to explore list
                                                                       #pathToSolution: contain path from goal
143
                                                           194
           openList[self.hashing(root.puzzle)]=
                                                                    to root
       root
                                                                       #explored: Number of nodes explored
                                                           195
           #Falg if goal found
                                                                       #child: Number of child faced
145
                                                           196
           goalFound=False
                                                                       #maxm: Maximum memory(Nodes) required
146
                                                           197
           #Check if current is goal state and
                                                                  to run code
147
       print it
                                                                  #Check if lis(HashTable) contains c(
                                                           198
           if root.goalTest():
                                                                  CurrentNode) with s(MODE)
148
                                                                  def con(self, lis, c, s):
                print("\nGoal Found")
149
                                                           199
               goalFound=True
                                                                       #Check if node is present in dictionary
150
                                                           200
                                                                    for hash value
                #Get path from current node(Goal)
151
       to source
                                                                       if lis.get(self.hashing(c.puzzle)) !=
                                                           201
               pathTrace(pathToSolution,root)
152
                                                                  None:
                                                                           #Check if node at hash value is
                return pathToSolution, explored,
                                                           202
       child, childm
                                                                   same
           #Stop when there is nothing to explore
                                                                           if lis[self.hashing(c.puzzle)].
154
                                                           203
       or goal is found
                                                                   isSamePuzzle(c.puzzle):
           while len(openList)!=0 and goalFound==
                                                                               #Update cost to node if needed
                                                           204
       False:
                                                                  and in open list
                                                                               if s=="open" and lis[self.
156
                #Get one node from list which
                                                           205
       contain node to explore
                                                                  hashing(c.puzzle)].tmp>c.tmp:
                _, currentNode=openList.popitem(last
                                                                                   lis[self.hashing(c.puzzle)
       =False)
                                                                  1.tmp=c.tmp
                                                           207
                #One node is out of memory
                                                                                   lis[self.hashing(c.puzzle)
158
                childm-=1
                                                                   ].parent=c.parent
                #Get hast value for that one node
                                                                                   lis[self.hashing(c.puzzle)
160
                                                           208
                chash=self.hashing(currentNode.
                                                                  ].children=c.children
161
       puzzle)
                                                                               #Node is alredy in list, so
                                                           209
                #Mark node as explored as this node
162
                                                                  true
        is going to be explored
                                                                               return True
               #It may have same hash also so
                                                                           #if same hash for 2 or more nodes
163
       check next
                                                                           else:
164
               if closedList.get(chash)!=None:
                                                                                #temporar pointer
                                                                               tmp1=lis[self.hashing(c.puzzle)
                    tmp1=closedList.get(chash)
165
                                                           214
                    while tmp1.next!=None:tmp1=tmp1
166
                                                                               #Check all pointers
       .next
                    tmp1.next=currentNode
                                                           216
                                                                               while tmp1.next!=None:
167
                else:closedList[chash]=currentNode
                                                           217
                                                                                   tmp1=tmp1.next
168
                #Explore the node
                                                                                    if tmp1.isSamePuzzle(c.
169
                                                           218
                currentNode.expandNode()
170
                                                                  puzzle):
                #Increament counter for explored
                                                                                        #Update cost to node if
                                                           2.19
                explored+=1
                                                                    needed and in open list
                #For all childrens check goal state
                                                                                        if s=="open" and tmp1.
                                                           220
174
               for i in range(len(currentNode.
                                                                  tmp>c.tmp:
       children)):
                                                                                            tmp1.tmp=c.tmp
                    #take ith child
175
                                                                                            tmp1.parent=c.
                    currentChild=currentNode.
                                                                  parent
176
       children[i]
                                                                                            tmp1.children=c.
                    #Child is faced in process so
                                                                  children
       increment counter
                                                                                        #Node is alredy in list
                                                           224
                    child+=1
178
                                                                   , so true
                    #Check if this is goal state
179
                                                                                        return True
                    if currentChild.goalTest():
                                                                                if(s=="open"):
                                                           226
180
                        goalFound=True
                                                                                   tmp1.next=c
181
                        #Get path to root
                                                                                    return True
182
                                                           228
                        pathTrace(pathToSolution,
                                                                       #False otherwise
                                                           229
183
       currentChild)
                                                           230
                                                                       return False
184
                                                           231
                    #Check if node in openList or
                                                           232 #Execution starts here
185
       closedList
                                                           233 #My randoly generated state
                                                           234 puzzle=[1,2,4,3,0,5,7,6,8]
                    if (self.con(openList,
186
       currentChild, "open") == False and self.con(
                                                           235 #My goal state
       closedList, currentChild, "closed") ==False):
                                                           236 goal=[0,1,2,3,4,5,6,7,8]
                        #If not then just append it
                                                           root=Node (puzzle)
187
        to open list
                                                           238 ui=uninformedSearch()
                        openList[self.hashing(
                                                           239 #Call uniform search
188
                                                           240 solution, explored, child, childm=ui.bfs (root)
       currentChild.puzzle)]=currentChild
                        #So its added to open list
                                                           241 #Reverse it as solution is reverse(from goal to
189
       so memory++
                                                                 source)
```

```
242 solution.reverse()
243 #Print solution
if len(solution)>0:
245
      for i in range(len(solution)):
         print("\n\n\nMove",i)
246
          solution[i].printPuzzle()
247
          if i<len(solution)-1:</pre>
             print("\n\n*****Next move
249
      print("\n\nDepth of solution is : ",
250
      solution[-1].tmp)
     print("\nTotal moves required : ",len(
      solution)-1)
      print("\nTotal nodes explored : ",explored)
252
      print("\nTotal childrens : ",child)
253
      print("\nTotal children in memory at once :
254
       ", childm)
print("\nNo path to solution is found")
```

Listing 2. 8-puzzle using Uniform Search

Output steps using Uniform

```
Move 0
2 1 2 4
3 3 0 5
4 7 6 8
6 *****Next move******
7 Move 1
8 1 2 4
9 3 6 5
10 7 0 8
12 *****Next move******
13 Move 2
14 1 2 4
15 3 6 5
16 7 8 0
18 *****Next move******
19 Move 3
20 1 2 4
21 3 6 0
22 7 8 5
24 *****Next move******
25 Move 4
26 1 2 0
27 3 6 4
28 7 8 5
30 *****Next move******
31 Move 5
32 1 0 2
33 3 6 4
34 7 8 5
35
36 *****Next move******
37 Move 6
38 0 1 2
39 3 6 4
40 7 8 5
41
42 *****Next move******
43 Move 7
44 3 1 2
45 0 6 4
46 7 8 5
48 *****Next move******
49 Move 8
50 3 1 2
51 6 0 4
```

```
52 7 8 5
54 *****Next move******
55 Move 9
56 3 1 2
57 6 4 0
58 7 8 5
60 *****Next move******
61 Move 10
62 3 1 2
63 6 4 5
64 7 8 0
66 *****Next move******
67 Move 11
68 3 1 2
69 6 4 5
70 7 0 8
72 *****Next move******
73 Move 12
74 3 1 2
75 6 4 5
76 0 7 8
78 *****Next move******
79 Move 13
80 3 1 2
81 0 4 5
82 6 7 8
84 *****Next move******
85 Move 14
86 0 1 2
87 3 4 5
88 6 7 8
90 Depth of solution is: 14
91 Total moves required:
92 Total nodes explored: 3457
93 Total childrens: 9562
94 Total children in memory at once : 2163
```

5) Generate Puzzle-8 instances with the goal state at depth "d".

```
#Same as before but return nodes at given depth
class configurations:
      #For hashing
      def hashing(self,x):
          hash_val=0
           for i in range(len(x)):
              hash_val += (i+1) * *x[i]
          return hash_val
      #To get nodes at depth depth
      def dbfs(self,root,depth):
10
           #root: Root node
          #depth: Depth at which to return nodes
          explored=0
          child=0
14
          childm=0
16
          maxm=0
          #This stores nodes which have required
      depth
18
          solutions=[]
          pathToSolution=[]
19
          openList=dict()
20
          closedList=dict()
21
          openList[self.hashing(root.puzzle)]=
          goalFound=False
24
           #Check if current depth of root is same
       as required
          if root.tmp==depth:
25
               goalFound=True
26
               #Node is found, return path to it
27
       from source
               pathTrace(pathToSolution,root)
28
29
               solutions.append(pathToSolution)
               return solutions
          while len(openList)!=0 and goalFound==
31
      False:
               _,currentNode=openList.popitem(last
32
      =False)
               chash=self.hashing(currentNode.
      puzzle)
3.4
               if closedList.get(chash)!=None:
                   tmp1=closedList.get(chash)
35
                   while tmp1.next!=None:tmp1=tmp1
36
                   tmp1.next=currentNode
37
               else:closedList[chash]=currentNode
38
               currentNode.expandNode()
39
               explored+=1
40
               for i in range (len (currentNode.
41
      children)):
42
                   currentChild=currentNode.
      children[i]
                   #Skip nodes which are above
43
      depth
                   if currentChild.tmp>depth:
44
45
                       goalFound=True
                       #Go out as we got what we
46
      needed
47
                       break
                   child+=1
48
49
                   if (self.con(openList,
      currentChild, "open") == False and self.con(
      closedList, currentChild, "closed") ==False):
                       openList[self.hashing(
      currentChild.puzzle)]=currentChild
51
                       childm+=1
                       if childm>maxm:maxm=childm
52
                       #If node matches with depth
53
       then add it to solutions
                      if currentChild.tmp==depth:
54
                           pathTrace(
```

```
pathToSolution, currentChild)
                            solutions.append(
       pathToSolution)
57
                            pathToSolution=[]
58
           return solutions
59
           #Check if lis(HashTable) contains c(
60
       CurrentNode) with s(MODE)
       def con(self, lis, c, s):
61
           #Check if node is present in dictionary
62
        for hash value
           if lis.get(self.hashing(c.puzzle)) !=
63
       None:
               #Check if node at hash value is
64
               if lis[self.hashing(c.puzzle)].
65
       isSamePuzzle(c.puzzle):
                   #Update cost to node if needed
66
       and in open list
                   if s=="open" and lis[self.
67
       hashing(c.puzzle)].tmp>c.tmp:
                        lis[self.hashing(c.puzzle)
       1.tmp=c.tmp
69
                        lis[self.hashing(c.puzzle)
       ].parent=c.parent
                        lis[self.hashing(c.puzzle)
70
       ].children=c.children
                   #Node is alredy in list, so
       true
72
                    return True
               #if same hash for 2 or more nodes
               else:
74
75
                    #temporar pointer
                   tmp1=lis[self.hashing(c.puzzle)
76
                    #Check all pointers
77
                   while tmp1.next!=None:
78
79
                       tmp1=tmp1.next
                        if tmp1.isSamePuzzle(c.
80
       puzzle):
                            #Update cost to node if
81
        needed and in open list
                            if s=="open" and tmp1.
82
       tmp>c.tmp:
83
                                tmp1.tmp=c.tmp
                                tmp1.parent=c.
84
       parent
                                tmp1.children=c.
85
       children
                            #Node is alredy in list
86
       , so true
                            return True
87
                    if(s=="open"):
88
                        tmp1.next=c
89
                        return True
           #False otherwise
91
92
           return False
94 #Execution starts here
95 puzzle=[0,1,2,3,4,5,6,7,8]
96 d=8
97 show=10
98 root=Node (puzzle)
99 ui=configurations()
solutions=ui.dbfs(root,d)
print("Found", len(solutions), "solutions or
       configurations with depth",d,"\nShowing top
        :", show)
for i in range(len(solutions)):
       if len(solutions[i])>0:
103
           print("\n\nSolution",i+1,"with depth",d
104
           solutions[i][0].printPuzzle()
105
     if i<len(solutions)-1 and i<show-1:</pre>
106
```

Listing 3. Functions to generate 8 puzzle instances with depth d

Output top 10 solutions with depth 8

```
Found 114 solutions or configurations with
      depth 8
2 Showing top: 10
3 Solution 1 with depth 8
4 2 5 0
5 1 3 4
6 6 7 8
8 ******Next solution********
9 Solution 2 with depth 8
10 2 3 5
11 1 0 4
12 6 7 8
14 *****Next solution******
15 Solution 3 with depth 8
16 1 2 5
17 6 3 4
18 7 8 0
20 *****Next solution******
21 Solution 4 with depth 8
22 1 2 5
23 6 0 4
24 7 3 8
25
26 *****Next solution******
27 Solution 5 with depth 8
28 1 5 4
29 3 2 8
30 6 7 0
32 *****Next solution******
33 Solution 6 with depth 8
34 3 1 5
35 2 0 4
36 6 7 8
38 *****Next solution******
39 Solution 7 with depth 8
40 3 1 5
41 6 2 4
42 0 7 8
44 *****Next solution******
45 Solution 8 with depth 8
46 1 2 5
47 3 0 7
48 6 8 4
50 *****Next solution******
51 Solution 9 with depth 8
52 1 2 0
53 3 7 5
54 6 8 4
56 *****Next solution******
57 Solution 10 with depth 8
58 1 2 5
59 7 0 4
60 3 6 8
```

6) Prepare a table indicating the memory and time requirements to solve Puzzle-8 instances (depth "d") using your graph search agent.

```
import time as t
2 import sys
3 node_size=sys.getsizeof(Node
      ([0,1,2,3,4,5,6,7,8]))
4 #Tabular format
5 goal=[0,1,2,3,4,5,6,7,8]
6 print("\\begin{center}")
7 print("\\begin{tabular}{ |c|c|c| }")
8 print("Init state & Time(msec) & Memory\\\")
10 #Solutions is list of instances of 8-puzzle
n for i in solutions:
      count+=1
12
      tmp=t.time()
13
    puzzle=i[0].puzzle
     root=Node(puzzle)
15
16
      ui=uninformedSearch()
     solution, explored, child, childm=ui.bfs (root)
17
      #to devide in half
18
19
      if count==35:
          print("\\end{tabular}")
20
          print("\\end{center}")
          print("\\begin{center}")
22
          print("\\begin{tabular}{ |c|c|c| }")
23
      print("Init state & Time(msec) & Memory
\\\\")
      if solution[0].tmp==d:
25
         print("text{", solution[-1].puzzle,"} &
      ", int((t.time()-tmp)*1000000), " & ", childm*
      node_size,end="\\\\n")
27 print("\\end{tabular}")
print("\\end{center}")
```

Listing 4. To generate table of memory and time

Output Table

Init state	Time(msec)	Memory
text [2, 5, 0, 1, 3, 4, 6, 7, 8]	2992	3528
text [2, 3, 5, 1, 0, 4, 6, 7, 8]	7930	6384
text [1, 2, 5, 6, 3, 4, 7, 8, 0]	3051	3528
text [1, 2, 5, 6, 0, 4, 7, 3, 8]	7608	7112
text [1, 5, 4, 3, 2, 8, 6, 7, 0]	4118	5544
text [3, 1, 5, 2, 0, 4, 6, 7, 8]	4641	5208
text [3, 1, 5, 6, 2, 4, 0, 7, 8]	6667	6216
text [1, 2, 5, 3, 0, 7, 6, 8, 4]	4260	4760
text [1, 2, 0, 3, 7, 5, 6, 8, 4]	6371	6216
text [1, 2, 5, 7, 0, 4, 3, 6, 8]	5102	5712
text [1, 2, 5, 4, 0, 8, 3, 6, 7]	4903	5600
text [1, 2, 0, 3, 8, 5, 6, 4, 7]	6658	5824
text [1, 2, 5, 3, 8, 7, 6, 4, 0]	8205	5768
text [1, 2, 5, 6, 3, 8, 0, 4, 7]	5725	5880
text [1, 5, 0, 3, 2, 8, 6, 4, 7]	4883	4872
text [0, 1, 5, 3, 2, 8, 6, 4, 7]	4673	4816
text [3, 1, 4, 5, 0, 2, 6, 7, 8]	6357	5096
text [3, 1, 4, 6, 5, 2, 0, 7, 8]	6465	6048
text [0, 5, 4, 1, 3, 2, 6, 7, 8]	4750	5488
text [1, 5, 4, 6, 3, 2, 0, 7, 8]	4502	5488
text [1, 5, 4, 3, 7, 2, 6, 8, 0]	4515	4816

Init state	Time(msec)	Memory
text [4, 2, 5, 1, 3, 8, 6, 7, 0]	4483	6048
text [4, 3, 0, 1, 5, 2, 6, 7, 8]	3867	5208
text [4, 3, 2, 1, 5, 8, 6, 7, 0]	3949	5152
text [4, 3, 2, 1, 7, 5, 6, 8, 0]	3444	4480
text [4, 3, 2, 1, 7, 5, 0, 6, 8]	3935	4480
text [1, 4, 2, 6, 0, 3, 7, 8, 5]	4078	4592
text [1, 4, 0, 6, 3, 2, 7, 8, 5]	4493	6048
text [1, 4, 0, 6, 5, 2, 7, 3, 8]	4442	5880
text [1, 4, 2, 6, 5, 8, 7, 3, 0]	4406	5880
text [0, 4, 2, 1, 6, 5, 7, 3, 8]	4477	5824
text [1, 4, 2, 7, 6, 5, 0, 3, 8]	4132	4704
text [1, 2, 0, 6, 4, 5, 7, 3, 8]	3790	4984
text [0, 1, 2, 6, 4, 5, 7, 3, 8]	3658	4984
text [0, 4, 2, 1, 3, 7, 6, 8, 5]	4253	5376
text [1, 4, 2, 6, 3, 7, 0, 8, 5]	4060	5432
text [1, 2, 0, 3, 4, 7, 6, 8, 5]	3332	4312
text [0, 1, 2, 3, 4, 7, 6, 8, 5]	3947	4256
text [1, 4, 2, 3, 8, 7, 0, 6, 5]	3347	4312
text [0, 1, 4, 3, 7, 2, 6, 8, 5]	3113	3920
text [1, 7, 4, 3, 0, 2, 6, 8, 5]	5289	6328
text [1, 4, 0, 7, 5, 2, 3, 6, 8]	4036	5432
text [1, 4, 2, 7, 5, 8, 3, 6, 0]	4031	5432
text [1, 2, 0, 7, 4, 5, 3, 6, 8]	4111	4704
text [0, 1, 2, 7, 4, 5, 3, 6, 8]	3545	4704
text [1, 4, 2, 7, 6, 5, 3, 8, 0]	3550	4704
text [4, 2, 0, 1, 7, 5, 3, 6, 8]	3009	3920
text [4, 7, 2, 1, 0, 5, 3, 6, 8]	6476	6664
text [4, 3, 1, 5, 0, 2, 6, 7, 8]	5295	5040
text [4, 3, 1, 6, 5, 2, 0, 7, 8]	5234	5936
text [3, 5, 0, 4, 2, 1, 6, 7, 8]	3042	3976
text [3, 5, 1, 4, 2, 8, 6, 7, 0]	5394	5488
text [0, 5, 1, 3, 4, 2, 6, 7, 8]	4133	5432
text [3, 5, 1, 6, 4, 2, 0, 7, 8]	4157	5488
text [3, 5, 1, 4, 7, 2, 6, 8, 0]	3538	4760
text [3, 5, 1, 4, 7, 2, 0, 6, 8]	4099	4760
text [3, 1, 2, 5, 0, 8, 4, 6, 7]	5011	5488
text [0, 1, 2, 3, 5, 8, 4, 6, 7]	4488	5992
text [3, 1, 0, 4, 8, 2, 6, 5, 7]	4162	5712
text [3, 1, 2, 4, 8, 7, 6, 5, 0]	3286	4256
text [3, 1, 2, 6, 4, 8, 0, 5, 7]	5217	5768
text [3, 2, 0, 4, 1, 8, 6, 5, 7]	145050	4704
text [0, 3, 2, 4, 1, 8, 6, 5, 7]	6787	4760
text [0, 2, 5, 3, 4, 1, 6, 7, 8] text [3, 2, 5, 6, 4, 1, 0, 7, 8]	6798 6681	5152
text [5, 2, 5, 6, 4, 1, 6, 7, 8] text [0, 3, 5, 4, 2, 1, 6, 7, 8]	3854	5152
_	5151	4032
text [3, 2, 5, 4, 7, 1, 6, 8, 0] text [3, 2, 5, 4, 7, 1, 0, 6, 8]	7434	3976 4032
text [3, 2, 5, 4, 7, 1, 0, 6, 8] text [3, 2, 5, 4, 1, 8, 0, 6, 7]	8552	3808
text [3, 2, 5, 4, 1, 8, 6, 6, 7] text [3, 2, 5, 4, 0, 8, 6, 1, 7]	11505	6888
text [3, 2, 3, 4, 0, 8, 0, 1, 7] text [4, 3, 2, 6, 1, 5, 7, 8, 0]	9118	3752
text [4, 3, 2, 6, 1, 5, 7, 8, 0] text [4, 3, 2, 6, 0, 5, 7, 1, 8]	9634	7392
text [3, 1, 2, 6, 4, 7, 0, 8, 5]	9235	5376
text [3, 2, 0, 4, 1, 7, 6, 8, 5]	9645	4200
text [0, 3, 2, 4, 1, 7, 6, 8, 5]	5359	4256
	2207	

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