B.TECH/CSE/4TH SEM /CSEN 2201/2016 2016

DESIGN AND ANALYSIS OF ALGORITHMS (CSEN 2201)

Time Allotted: 3 hrs

Full Marks: 70

Figures out of the right margin indicate full marks.

Candidates are required to answer Group A and any 5 (five) from Group B to E, taking at least one from each group.

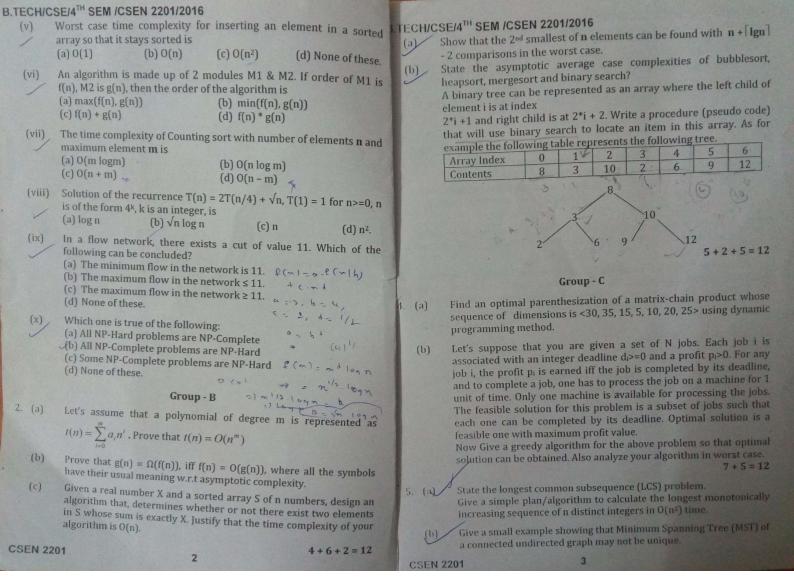
Candidates are required to give answer in their own words as far as practicable.

Group - A (Multiple Choice Type Questions)

	Choos	e the correct altern	atives for the fo	ollowing:	10	× 1 = 10
	(i)	The number of edhaving 19 connects (a) 19 (b) 8	ted component	forest of a g s is 80	raph with 10	
	(ii)	In the KMP algorithm for pattern matching, the suffix function $\sigma(x)$ is theest of the pattern P that is also a of x. (a) large, prefix, suffix (b) small, prefix, suffix (c) large, suffix, prefix (d) large, suffix, prefix				
	(iii)	For simultaneous elements, the num (a) $3 \lfloor n/2 \rfloor$	sly finding the ber of compari (b) 2n	isons require	ed is at most	num of n
	(iv)	A student proved that the longest path problem is NP-complete by reducing it to another already known NP-complete problem named set-cover problem. His teacher said the proof is not correct and did not give him any marks. Which of the following is true - (a) The teacher does not understand NP-completeness as it is a difficult chapter. (b) The student got a wrong answer about the hardness of longest path problem.				

student.

(d) The teacher is biased and hence did not give marks to the



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What is the main difference between the Kruskal's and Prim's algorithm?

State the time complexity of the Prim's algorithm for both cases where we use (i) an array, (ii) a heap to implement the priority queue.

(2+4) + (2+2+2) = 12

Group - D

(a) A sequence of n operations is performed on a data structure. The cost of ith operation is $C(i) = i^2$, if i is an exact power of 3 = 3, otherwise.

Calculate the exact expression for cost for n successive operations. Use Aggregate Analysis to determine the amortized cost per operation.

- (b) Give the asymptotic complexities for string matching using finite automata and KMP algorithm. Define the terms used in the expression.
- (c) Give the pseudo code for identifying the strongly connected components in a graph.

You can use DFS(G) as a procedure that is already available to you. DFS(G) stands for Depth First Search on graph G.

6+(1+1)+4=12

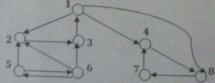
(a) Given the following:

String S: bacbabababacaca

Pattern P: ababaca

Show how Knuth-Morris-Pratt algorithm works to solve the string matching problem for the above case

(b) / Consider the following graph G = (V, E):



Find the strongly connected components of the above graph. Also justify that the strategy that you have applied here produces the strongly connected components in O (V + E) time.

6 + (4+2) = 12

CSEN 2201

4

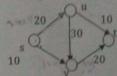
CH/CSE/4TH SEM /CSEN 2201/2016 Group - E

Define P, NP, NP-Complete and NP-Hard problems. Show that VERTEX-COVER problem is NP-Complete.

Give a polynomial-time 2-approximation algorithm for vertex cover problem and also prove that the algorithm indeed achieves that factor.

(2+4) + 6 = 12

(a) Apply FORD-FULKERSON algorithm on the following flow network to find the maximum flow in the network. s & t denotes source & destination and the weights associated with every edge represents capacity of the respective edge.



(b) Define the following terms in the context of optimization problems

(i) Polynomial-time approximation scheme

(ii) Fully polynomial-time approximation scheme (FPTAS)

8+(2+2)=12