Assignment-3

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Abstract—This document contains the procedure to evaluate the determinant

Download the python code from

https://github.com/ankuraditya13/EE5609-Assignment3

and latex-file codes from

https://github.com/ankuraditya13/EE5609-Assignment3

1 Problem

Evaluate the following determinant

$$\begin{vmatrix} a-b & b-c & c-a \\ b-c & c-a & a-b \\ c-a & a-b & b-c \end{vmatrix} = 0$$
 (1.0.1)

2 Solution

Let,
$$|\mathbf{A}| = \begin{vmatrix} a - b & b - c & c - a \\ b - c & c - a & a - b \\ c - a & a - b & b - c \end{vmatrix}$$
 (2.0.1)

Applying row transformation in above determinant we get,

$$\begin{vmatrix} a-b & b-c & c-a \\ b-c & c-a & a-b \\ c-a & a-b & b-c \end{vmatrix} \xrightarrow{R_1 \leftarrow R_1 + R_2 + R_3} (2.0.2)$$

$$\begin{vmatrix} 0 & 0 & 0 \\ b-c & c-a & a-b \\ c-a & a-b & b-c \end{vmatrix} (2.0.3)$$

$$\begin{vmatrix} 0 & 0 & 0 \\ b - c & c - a & a - b \\ c - a & a - b & b - c \end{vmatrix}$$
 (2.0.3)

From equation (2.0.3) one of the row of $|\mathbf{A}|$ is zero

$$\implies |\mathbf{A}| = 0 \tag{2.0.4}$$