

Sorting

Dictionary is important

① merge sort →

def mergesort(l, lt)

if $lt \leq 1$:
return l

mid = $lt // 2$

left = l[:mid]

right = l[mid:]

mergesort(left, mid)

mergesort(right, lt - mid)

i=j=k=0

while i < mid and j < lt - mid:

if right[j] < left[i]:

l[k] = right[j]

j+=1

else

l[k] = left[i]

i+=1

k+=1

if i == mid:

l[k:] = right[j:]

else

l[k:] = left[i:]

return l

lt → length of array to sort.

mid will be length of left

lt - mid will be length of right
array.

Time Complexity

= $O(n \log n)$.

Problem statement -

Count no. of inversions or no. of adjacent swaps required to sort an integer array.

def mergecount(l, lt):

if lt == 1:

return 0

mid = lt // 2

left = l[:mid]

right = l[mid:]

c = mergecount[left, mid] + mergecount[right, lt - mid]

i = j = k = 0

while i < mid and j < lt - mid:

if right[j] < left[i]:

c += mid - i

l[k] = right[j]

j += 1

else

l[k] = left[i]

i += 1

k += 1

if i == mid:

~~else~~

l[k:] = right[j:]

else

l[k:] = left[i:]

return c

Quicksort

```

def Quicksort(l, low, high):
    if low == high:
        return
    if high > low:
        mid = partition(l, low, high)
        quicksort(l, low, mid - 1)
        quicksort(l, mid + 1, high)

```

Driver code

```

l = [-]
quicksort(l, 0, n)
print(l)

```

```

def quicksort(array, l, r):
    if l >= r:
        return
    mid = partition(array, l, r)
    quicksort(array, l, mid - 1)
    quicksort(array, mid + 1, r)

```

def partition(array, l, r):

pivot = array[r]

i = l - 1

for j in range(l, r):

if array[j] <= pivot:

i += 1

array[i], array[j] = array[j], array[i]

~~array[i+1], array[r] = array[r], array[i+1]~~

array[i+1], array[r] = array[r], array[i+1]

return i + 1

Maximum contiguous subarray problem

```
def findmaximum(l):
```

```
lt = len(l)
```

```
curres = l[0]
```

```
res = l[0]
```

```
for i in range(1, lt):
```

```
    if l[i] > l[i] + curres:
```

```
        curres = l[i]
```

```
        res = max(curres, res)
```

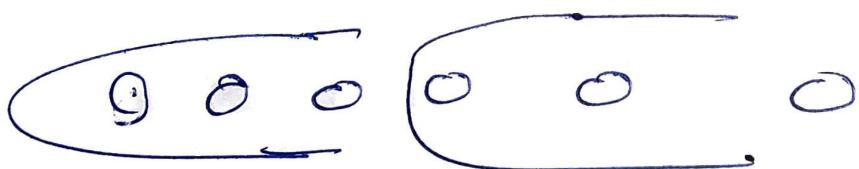
```
    else
```

```
        curres = l[i] + curres
```

```
        res = max(curres, res)
```

```
return res.
```

Kadane's Algo



(String Manipulation)

problem \rightarrow Given a string, count total number of palindromic substrings in this.

solution \rightarrow There will be total $\frac{n(n+1)}{2}$ substrings.

We will use dynamic programming.

Ex- abcba

$\{a, b, c, b, a, b, a, bcb, bab, aba, abcba\}$

output \rightarrow 11 string end at

	a	b	c	b	a	b	a
a	T	F	F	F	T	F	F
b	None	T	F	T	F	F	F
c	None	None	T	F	F	F	F
b	None	None	None	T	F	T	F
a	None	None	None	None	T	F	T
b	None	None	None	None	None	T	F
a	None	None	None	None	None	None	T

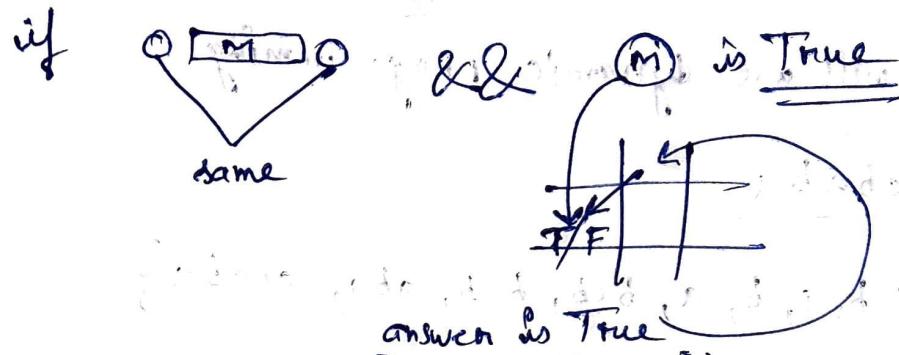
string started from.

Logic \rightarrow For a sequence to be palindromic, the necessary and sufficient condition is \rightarrow first and last letter are same and the part in between them must be palindromic.

step \rightarrow ① We create a 2-D array of size $n \times n$. with all having value None.

② For all single letter sequence, we make value at that index as True.

- ③ For all sequence of length 2, if both letters are same, make make the value at that index as True else make False.
- ④ Now traverse the 2-D array diagonally from the 3rd Column and first row.



- ⑤ return total no. of True values in the 2-D array.

Code

```
def countpalin(l, n, array):
    p = 2
    for i in range(n-2):
        k = 0
        for j in range(p, n):
            if l[k] == l[j]:
                if array[k+1][j-1] == True:
                    array[k][j] = True
                else:
                    array[k][j] = False
            else:
                k += 1
        p += 1
    for i in range(n-1):
        array[i][i] = False
    k = 0
```

res = 0

```
for i in range(0, n):
    for j in range(i, n):
        if array[i][j] == True:
            res += 1
```

return res.

Driver Code

n = int(input()) # length of string

s = input() # given string.

import numpy as np

temp = np.array([None]*n)*n) → creating 2-D array.

for i in range(n):

temp[i][i] = True

make all single length string
array value as True.

for i in range(0, n-1):

if s[i] == s[i+1]:

→ For all string of length 2 -

temp[i][i+1] = True

else

temp[i][i+1] = False

print(countpalin(s, n, temp))

longest common subsequence problem

→ Given two strings find the longest common subsequence of both (not necessarily consecutive sequence). (strings of equal length)
this can be solved using DP.

Code →

def lcs(s1, s2, n):

n = length of strings

Column 1 = [0] * (n+1)

Column 2 = [0] * (n+1)

for j in range(0, n):

 for i in range(0, n):

 if s1[i] == s2[j]:

 column2[i+1] = 1 + column1[i]

 else

 column2[i+1] = max(column1[i+1], column2[i])

column1, column2 = column2, column1

return column1[-1]

=

Ex -

	A	N	K	U	X	P	
A	0	0	0	0	0	0	0
R	0	1	1	2	2	2	2
X	0	1	1	2	2	3	3
P	0	1	1	2	2	3	4
R	0	1	1	2	2	3	4
X	0	1	1	2	2	3	4

result will be 4 & AKXP.

* in code we could have also used 2-d array as shown above but we used two columns to reduce space complexity & time complexity (to create 2-d array with all value non-zero or zero).

(KMP Algorithm)

used for pattern matching.

```
def prefixfunction(l, n):  
    border = 0  
    s = [0]*n  # final returns array  
    s[0] = 0  
    for i in range(1, n):  
        while border > 0 and l[i] != l[border]:  
            border = s[border-1]  
        if l[i] == l[border]:  
            border += 1  
        else:  
            border = 0  
        s[i] = border
```

return s.

Now to find pattern in text, we do

pattern + "\$" + text
↓
a process We will do prefixfunction on this string.

pattern +

Ex -

pattern : abababiciabixialbiabiy
text : 0012012012340

(Dynamic Programming)

① Hacker's problem -

→ Given a list of integers

→ find maximum sum of numbers present in list which are non adjacent to each other.

```
def sum(l):
```

```
    lt = len(l)
```

```
    temp_array = [0] * lt
```

```
    temp_array[0] = max(0, l[0])
```

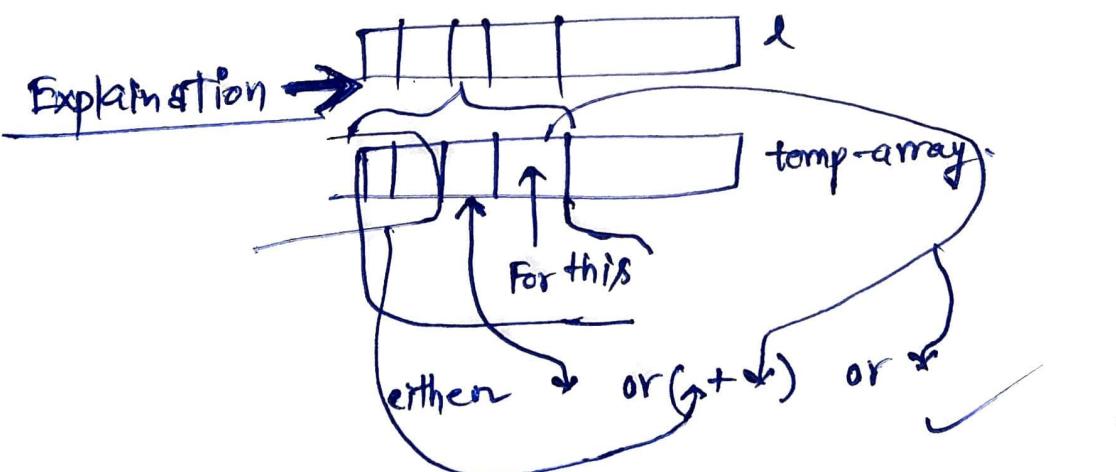
```
    temp_array[1] = max(0, l[0], l[1])
```

```
    for i in range(2, lt):
```

```
        temp_array[i] = max(temp_array[i-1], temp_array[i-2]+l[i], l[i])
```

```
    return max(max(temp_array), 0)
```

* you can also choose no (zero) numbers.



(Stack and Queue)

Next smaller element to right left!

Given an array. We have to find an array of length, the size of the original array which gives us the index of next smaller element of a given element in an array. If no such element is found put -1 at that place.

Ex -

input \rightarrow

1	-1	0	2	-7
0	1	2	3	4

output \rightarrow

-1	-1	1	(2)	-1
0	1	2	3	4

def nsel(l):

lt = len(l)

stackValue = [l[0]]

stackIndex = [0]

res = [-1]

for i in range(1, lt):

while len(stack) != 0 and stackValue[-1] >= l[i]:

stackValue.pop()

stackIndex.pop()

if len(stack) == 0:

res.append(-1)

stackValue.append(l[i])

stackIndex.append(i)

return res

else:

res.append(stackIndex[-1])

stackValue.append(l[i])

stackIndex.append(i)

return res

def medianstr(l):

lt = len(l)

res = [-1]

stackValue = [l[-1]]

stackIndex = [lt-1]

for i in range(lt-2, -1, -1):

while len(stack) != 0 and stackValue[-1] >= l[i]:

stackIndex.pop()

stackValue.pop()

if len(stack) == 0:

res.append(-1)

stackIndex.append(i)

stackValue.append(l[i])

else:

res.append(stackIndex[-1])

stackIndex.append(i)

stackValue.append(l[i])

[0] = rechte Seite.

[1-] = linke

return res[:: -1].

ngetr

def ngetr(l):

lt = len(l)

stackValue = [l[lt-1]]

stackIndex = [lt-1]

res = [lt]

for i in range(lt-2, -1, -1):

while len(stackIndex) != 0 and stackValue[-1] <= l[i]:

(i, stackIndex[-1]) knappe aus

(i, stackIndex[-1]) bringe auf rechte

(i, stackIndex[-1]) bringe auf linke

stackIndex.pop()
stackValue.pop()

if len(stack) == 0 :

res.append(-1)

stackIndex.append(i)

stackValue.append(l[i])

else :

res.append(stackIndex[-1])

stackIndex.append(i)

stackValue.append(l[i])

return res[3:-1]

next greater element to left :- find this problem in gfg

def ngetl(l):

lt = len(l)

res = [-1]

stackIndex = [0]

stackValue = [l[0]]

for i in range(1, lt):

 while len(stackIndex) != 0 and stackValue[-1] <= l[i]:
 stackIndex.pop()
 stackValue.pop()

 if len(stackIndex) == 0 :

 res.append(-1)

 stackIndex.append(i)

 stackValue.append(l[i])

 else :

 res.append(stackIndex[-1])

 stackIndex.append(i)

 stackValue.append(l[i])

return res

HackerRank Problem (poisonous plants)

problem statement →

Given an array of Integers.
 (1) If there is a stack of 2 or more elements, then the top element will be removed.
 (2) If there is a stack of 1 element, then it will be kept.

Ex →

4	2	9	7	0	1	5	8	11	22
*	*	*	*	*	*	*	*	*	*

day 1 →

4	2	7	0
↓			

day 2 →

4	2	0
↓		

day 3 → Nothing will happen

Explanation → solution can be solved by list of stacks

step ① →

4	2	9	7	0	1	5	8	11	22
*	*	*	*	*	*	*	*	*	*

step ② → delete 1st element of every stack except 1st one.

4	2	7	0						
*	*	*	*	*	*	*	*	*	*

step ③ → see if any stack can be merge.

→ 2 Here No because $1 < 2 < 7$

step 4 → repeat step ② until length of list of stacks = 1

(1) Initialize stack

(2) Append 1

(3) Append 2

→ 1 is result

Trie

Class Node :

```
def __init__(self):  
    self.child = {}  
    self.isend = False
```

Class Trie :

```
def __init__(self):  
    self.root = Node(); self.words = []
```

```
def insert(self, word):  
    it = len(word)  
    start = self.root  
    for char in range(it): word  
        if char in start.child:  
            start = start.child[char]
```

```
else:  
    Newnode = Node()  
    start.child[char] = Newnode  
    start = New node
```

start.isend = True

```
def search(self, word):  
    start = self.root  
    for char in word:  
        if start.child[char] in start.child:  
            start = start.child[char]
```

```
else:  
    return False
```

return True

```
def telllastnode(self, word) # ex: bird
```

start = self.root

for char in word:

if char in start.childdic:

start = start.childdic[char]

else

return None

return start

```
def finalprint(self, pre, node): # return a list of words starting with a prefix (pre) -
```

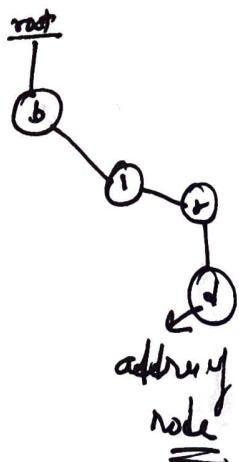
if node.end == True

self.words.append(pre)

~~for~~

for i in node.childdic:

self.finalprint(pre+i, node.childdic[i])



Linked List

Singly linked list node

```
class Node :
```

```
    def __init__(self, value)  
        self.value = value  
        self.next = None
```

```
class LinkedList :
```

```
    def __init__(self) :
```

```
        self.head = None  
        self.tail = None
```

```
    def insert(self, value) :
```

```
        if self.head == None :  
            node = Node(value)
```

```
            self.head = node(value) node
```

```
            self.tail = self.head address of new node created  
            node
```

```
        temp = self.head
```

```
        node = Node(value)
```

```
        while temp.next != None :
```

```
            temp = temp.next
```

```
        temp.next = node
```

```
        self.tail = node.
```

* Be carefull about end (edge cases) on every problem.

Ex - Reverse a linked list

① Delete a node

→ Insert at a position

→ and check temp.next

Priority Queue

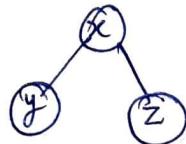
Courses

Binary tree like structure.

Also called heap.

Minheap and maxheap.

property →



$x \geq y$ and $x \geq z \Rightarrow$ (maxheap)

$x \leq y$ and $x \leq z \Rightarrow$ (minheap)

minheap

class Heap:

def __init__(self):

self.l = []

self.count = 0 # no. of elements in heap

def parent(self, i): # i → index in list(heap).

return (i-1)//2

def leftchild(self, i):

return 2*i + 1

def rightchild(self, i):

return 2*i + 2

def swap(self, a, b):

self.l[a], self.l[b] = self.l[b], self.l[a]

def shiftUp(self, i):

if i == 0:

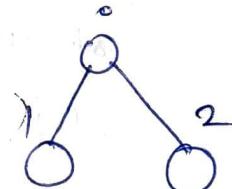
return

par = self.parent(i)

if self.l[par] > self.l[i]:

self.swap(par, i)

self.shiftUp(par)



```
def insert(self, num):  
    self.l.append(num)  
    self.count += 1  
    self.shiftup(self.count - 1)
```

```
def shiftdown(self, i):  
    temp = i  
    lt = self.leftchild(i)  
    if self.count - 1 >= lt and self.l[lt] < self.l[temp]:  
        temp = lt  
    rt = self.rightchild(i)  
    if self.count - 1 >= rt and self.l[rt] < self.l[temp]:  
        temp = rt
```

```
    if i != temp:  
        self.swap(i, temp)  
        self.shiftdown(temp)
```

```
def buildheap(self):  
    if self.count <= 1:  
        return
```

```
    start = self.parent(self.count - 1)
```

```
    for i in range(start, -1, -1):  
        self.shiftdown(i)
```

```
def sortlist(self):  
    if self.count <= 1:  
        return  
    self.buildheap()  
    temp = self.count
```

```
for i in range (self.count-1) :
```

```
    self.swap (0, self.count-1)
```

```
    self.count -= 1
```

```
    self.shiftdown (0)
```

```
self.count = temp
```

```
def changepriority (self, i, new) :
```

```
    if new > self.l[i] :
```

```
        self.l[i] = new
```

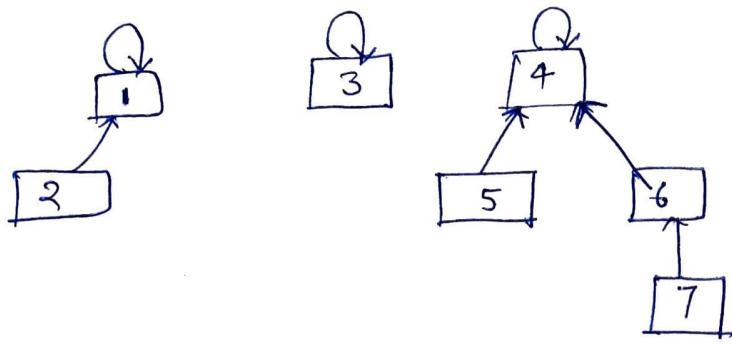
```
        self.shiftdown (i)
```

```
    else :
```

```
        self.l[i] = new
```

```
        self.shiftup (i)
```

Disjoint set



* There are three groups given.

*

```
def find(node): # in which group, this  
    if node.parent == node:  
        return node.group  
    return find(node.parent)
```

```
class node:
```

```
    def __init__(self):  
        self.value = value  
        self.parent = self  
        self.child = {}  
        self.group = value
```

~~union by compression~~

```
def union(a, b): # a is  
    temp = a  
    while temp.parent != temp:  
        temp = temp.parent
```

```
    b.parent = temp  
    b.group = temp.group
```

~~combining two~~