

OFFER PERSONALIZATION USING TEMPORAL CONVOLUTIONS AND MULTI-OBJECTIVE OPTIMIZATION

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ABSTRACT

Lately, personalized marketing has become important for retail/e-retail firms due to significant rise in online shopping and market competition. Increase in online shopping and high market competition has led to an increase in promotional expenditure for online retailers, and hence, rolling out optimal offers has become imperative to maintain balance between number of transactions and profit. In this paper, we propose our approach to solve the offer optimization problem at the intersection of consumer, item and time in retail setting. To optimize offer, we first build a generalized non-linear model using Temporal Convolutional Network to predict the item purchase probability at consumer level for the given time period. Secondly, we establish the functional relationship between historical offer values and purchase probabilities obtained from the model, which is then used to estimate offer-elasticity of purchase probability at consumer item granularity. Finally, using estimated elasticities, we optimize offer values using constraint based multi-objective optimization technique. This paper describes our detailed methodology and presents the results of modelling and optimization across categories.

1 INTRODUCTION

In most retail settings, promotions play an important role in boosting the sales and traffic of the organisation. Promotions aim to enhance awareness when introducing new items, clear leftover inventory, bolster customer loyalty, and improve competitiveness. Also, promotions are used on a daily basis in most retail environments including online retailers, supermarkets, fashion retailers, etc. A typical retail firm sells thousands of items in a week and needs to design offer for all items for the given time period. Offer design decisions are of primary importance for most retail firms, as optimal offer roll out can significantly enhance the business' bottom line.

Most retailers still employ a manual process based on intuition and past experience of the category managers to decide the depth and timing of promotions. The category manager has to manually solve the promotion optimization problem at consumer-item granularity, i.e., how to select an optimal offer for each period in a finite horizon so as to maximize the retailer's profit. It is a difficult problem to solve, given that promotion planning process typically involves a large number of decision variables, and needs to ensure that the relevant business constraints or offer rules are satisfied. The high volume of data that is now available to retailers presents an opportunity to develop machine learning based solutions that can help the category managers improve promotion decisions.

In this paper, we propose deep learning with multi-objective optimization based approach to solve promotion optimization problem that can help retailers decide the promotions for multiple items while accounting for many important modelling aspects observed in retail data. The ultimate goal here is to maximize net revenue and consumer retention rate by promoting the right items at the right time using the right offer discounts at consumer-item level. Our contributions in this paper include a) Temporal Convolutional Neural Network architecture with hyperparameter configurations to predict the item purchase probability at consumer level for the given time period. b) Design and implementation of F_1 -maximization algorithm which optimises for purchase probability cut-off at consumer level. c) Methodology to estimate offer elasticity of purchase probability at consumer item granularity. d) Constraint based multi-objective optimization technique to estimate optimal offers at consumer-item granularity.

2 RELATED WORK

In the past few years, various works have been done to solve Promotion Optimization problem. Closer to our work is ?, which presents study over the impact linear optimization on promotion planning. The paper proposes general classes of demand functions (including multiplicative and additive), which incorporate the post-promotion dip effect, and can be estimated from sales data. They then propose a linear integer programming to solve Promotion Optimization problem. We propose a neural network based solution to first predict the item purchase probability, then estimate the offer-elasticity of purchase probability at consumer item granularity, and finally apply dynamic programming approach to solve Promotion Optimization problem.

3 METHODOLOGY

We built separate models for each category, as we understand that consumer purchase pattern and personalized marketing strategies might vary with categories.

3.1 MODELLING

In our model setup, we treat each relevant consumer-item as an individual object and shape them into bi-weekly time series data based on historical transactions, where the target value at each time step (2 weeks) takes a binary input, 1/0 (purchased/non purchased). *Relevancy* of the consumer-item is defined by items transacted by consumer during training time window. Our *Positive samples* (purchased/1) are time steps where consumer did transact the item, whereas *Negative samples* (non purchased/0) are the time steps where the consumer did not buy that item. We apply sliding windows testing routine for generating out of time results. The time series is split into 3 parts - train (48 weeks), validation (2 weeks) and test (2 weeks). All our models are built in a multi-object fashion for an individual category, which allows the gradient movement to happen across all consumer-item combinations split in batches. This enables cross-learning to happen across consumers/items. A row in time series is represented by

$$y_{cit} = h(i_t, c_t, \dots, c_{t-n}, ic_t, \dots, ic_{t-n}, d_t, \dots, d_{t-n}) \quad (1)$$

where y_{cit} is purchase prediction for consumer 'c' for item 'i' at time 't'. 'n' is the number of time lags. i_t denotes attributes of item 'i' like category, department, brand, color, size, etc at time 't'. c_t denotes attributes of consumer 'c' like age, sex and transactional attributes at time 't'. c_{t-n} denotes the transactional attributes of consumer 'c' at a lag of 't-n' time steps. ic_t denotes transactional attributes such as basket size, price, offer, etc. of consumer 'c' towards item 'i' at time 't'. d_t is derived from datetime to capture trend and seasonality at time 't'.

3.1.1 FEATURE ENGINEERING

Based on available dataset, we generate multiple features for the modelling activity. Some of the feature groups we perform our experiments are:

Datetime: We use transactional metrics at various temporal cuts like week, month, etc. Datetime related features capturing seasonality and trend are also generated. **Consumer-Item Profile:** We use transactional metrics at different granularities like consumer, item, and consumer-item. We also create features like Time since first order, Time since last order, time gap between orders, Reorder rates, Reorder frequency, Streak - user purchased the item in a row, Average position in the cart, Total number of orders. **Price/Promotions:** We use relative price and historical offer discount percentage to purchase propensity at varying price, and discount values. **Lagged Offsets:** We use statistical rolling operations like mean, median, variance, kurtosis and skewness over temporal regressors for different lag periods to generate offsets.

3.1.2 LOSS FUNCTION

Since we are solving Binary Classification problem, we believe that Binary Cross-Entropy should be the most appropriate loss function for training the models. We use the below formula to calculate Binary Cross-Entropy:

$$H_p = -\frac{1}{N} \sum_{i=1}^N y \cdot \log(p(y)) + (1 - y) \cdot \log(1 - p(y)) \quad (2)$$

here H_p represents computed loss, y is the target value (label), and $p(y)$ is the predicted probability against the target. The BCELoss takes non-negative values. We can infer from Equation 3 that Lower the BCELoss, better the Accuracy.

3.1.3 MODEL ARCHITECTURE

Traditional machine learning models may not be a suitable choice for modelling h (Equation 1) due to non-linear interactions between the features. Hence, we use Entity Embeddings + Temporal Convolutional Network (TCN) (Figure 1) architecture for building all the models across categories. Originally proposed in Lea et al. (2016), TCN can take a sequence of any length and map it to an output sequence of the same length. For this to accomplish, TCN uses a 1D fully-convolutional network (FCN) architecture, where each hidden layer is the same length as the input layer, and zero padding of length (kernel size-1) is added to keep subsequent layers the same length as previous ones. Also, the convolutions in the architecture are causal, meaning that there is no information leakage from future to past. To achieve this, TCN uses causal convolutions, convolutions where an output at time t is convolved only with elements from time t and earlier in the previous layer. For 1-D sequence input x and filter f the dilated convolution operation DC on element k of the sequence is defined as:

$$DC(k) = (x *_{d} f)(k) = \sum_{i=0}^{n-1} f(i) \cdot x_{k-d_i}, \text{ where } x \in \mathcal{R}^n \text{ and } f : \{0, \dots, n-1\} \rightarrow \mathcal{R} \quad (3)$$

where d is the dilation factor, n is the filter size, and $k-d_i$ accounts for the direction of the past. When $d = 1$, a dilated convolution reduces to a regular convolution. Using larger dilation enables an output at the top level to represent a wider range of inputs, thus effectively expanding the receptive field of a ConvNet.

As can be seen in Figure 1, Our network architecture comprises of 3 dilated Convolutions combined with entity embeddings. Post Convolutions and concatenation with embedding tensor, the created tensor flows through 3 fully connected ReLU layers yielding to sigmoid dense layer. To segregate static and temporal features, we group input tensor into 4 separate tensors, as can be seen in 1:

Static Categorical: These are categorical features that do not vary with time. This includes consumer attributes like sex, marital status and location along with different item attributes like category, department and brand. **Temporal Categorical:** These are categorical features that vary with time. It includes all the datetime related features like week, month of year, etc. **Static Continuous:** These features are static but continuous. This includes certain consumer attributes like age and weight, item attributes like size, and certain derived features like target encoded features. **Temporal Continuous:** These are time varying continuous features. All consumer and item related traditional attributes like number of orders, add to cart order, etc. falls under this bucket.

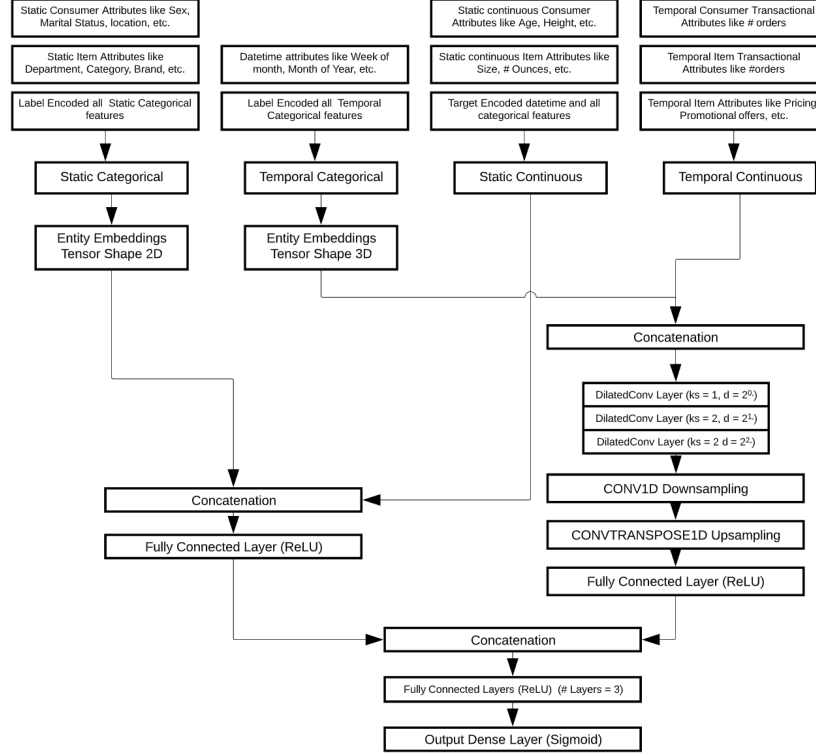
3.1.4 HYPERPARAMETER TUNING

We use documented best practices along with our experimental results to choose model hyperparameters. Hyperparameter Optimization is performed over validation dataset. We list some of the hyperparameters along with the values we tune for Deep neural network models.

Optimizer Parameters: RMSProp Bengio & CA (2015) and Adam are used as optimizers across model runs. The learning rate is experimentally tuned to $1e-3$. We also have weight decay of $1e-5$ which helps a bit in model Regularization. **Scheduler Parameters:** CyclicLR Smith (2017) and ReduceLROnPlateau Zaheer et al. (2018) Learning rates are used as schedulers across model runs. we use $1e-3$ as max lr and $1e-6$ as base lr for cyclical learning rate along with the step size being the function of length of train loader. ReduceLROnPlateau is tuned at $1e-6$ as min lr. **SWA:** Stochastic Weight Averaging (SWA) Izmailov et al. (2018) is used to improve generalization across Deep Learning models. SWA performs an equal average of the weights traversed by SGD with a modified learning rate schedule. We use $1e-3$ as SWA learning rate. **Parameter Average:** This is a method to average the neural network parameters of n best model checkpoints post training, weighted by validation loss of respective checkpoints.

Apart from these parameters we also iterate to tune network parameters like number of epochs, batch size, number of Fully Connected Layers, convnet parameters (kernel size, dilations, padding) and embedding sizes for the categorical features. Binary Cross-Entropy 3 is used as loss function for all the models trained across categories.

Figure 1: Temporal Convolutional Network (TCN)



3.2 F₁-MAXIMIZATION

Post stacking, we optimize for purchase probability threshold based on probability distribution at a consumer level using F₁-Maximization. This enables optimal thresholding of consumer level probabilities to maximize F₁ measure Lipton et al. (2014). To illustrate the above, let us say we generated purchase probabilities for 'n' items out of 'b' actually purchased items by consumer 'c'. Now, let us visualize the actuals and predictions (4) of 'n' predicted items for consumer 'c'.

$$A_c = [a_1, a_2, \dots, a_n] \forall a_j \in \{0,1\}, \quad P_c = [p_1, p_2, \dots, p_n] \forall p_j \in [0,1] \quad (4)$$

A_c represents the actuals for consumer 'c', with a_j being 1/0 (purchased/non purchased). P_c represents the predictions for consumer 'c' for the respective item, with p_j being probability value. 'n' represents total items for which the model generated purchase probabilities for consumer 'c'. Now we apply Decision rule D() which converts probabilities to binary predictions, as described below in Equation 5.

$$D(P_{r_c}) : P_c^{1 \times n} \rightarrow P'_c^{1 \times n} : p'_j = \begin{cases} 1 & p_j \geq P_{r_c} \\ 0 & \text{Otherwise} \end{cases} \quad (5)$$

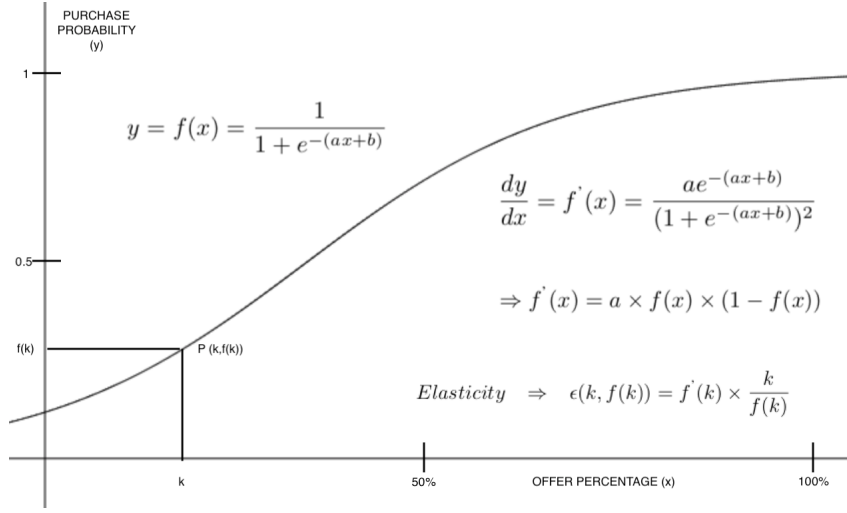
$$P'_c = [p'_1, p'_2, \dots, p'_n] \forall p'_j \in \{0,1\}, \quad k = \sum_{i=1}^n p'_i \quad (6)$$

P_{r_c} is the probability cut-off to be optimized for maximizing F₁ measure Lipton et al. (2014) for consumer 'c'. Decision rule D() converts probabilities P_c to binary predictions P'_c such that if p_j is less than P_{r_c} then p'_j equals 0, otherwise 1. 'k' is the sum of predictions generated post applying Decision rule D(). Now we solve for F₁ measure using equations and formulae described below.

$$V_{P_{r_c}} = P'_c \times A_c^T \Rightarrow \begin{pmatrix} p'_1 & \dots & p'_n \end{pmatrix} \times \begin{pmatrix} a_1 \\ \dots \\ a_n \end{pmatrix} \quad (7)$$

$$Precision_c = \frac{V_{P_{r_c}}}{k}, \quad Recall_c = \frac{V_{P_{r_c}}}{b}, \quad F_{1c} = \frac{2 \times Precision_c \times Recall_c}{Precision_c + Recall_c} \Rightarrow 2 * \frac{V_{P_{r_c}}}{k+b} \quad (8)$$

Figure 2: Purchase probability vs. Offer percentage



V_{Pr_c} represents the number of items with purchase probabilities greater than Pr_c which were actually purchased (True Positives). As can be seen, Formulae 8 is used to calculate Precision, Recall and F_1 -score for consumer 'c'.

$$\max_{V_{Pr_c}} 2 * \frac{V_{Pr_c}}{k + b} \quad , \quad \text{subject to: } Pr_c \in [0, 1] \quad (9)$$

Equation 9 represents the optimization function we solve to generate purchase predictions (1/0) for each consumer.

3.3 ELASTICITY FRAMEWORK

Post modelling, we establish the functional relationship between historical offer values and purchase probabilities obtained from the model, which is then used to estimate offer-elasticity of purchase probability at consumer item granularity. With multiple experiments and business insights we find sigmoid function (Figure 2) to be an apt choice to study the variation of purchase probability with offer percent.

$$f(x) = \frac{1}{1 + e^{-(ax+b)}} \quad , \quad f'(x) = a \times f(x) \times (1 - f(x)) \quad (10)$$

We also understand that parameters of the function will vary with categories, hence we learn separate parameters of sigmoid for each category. We use the sigmoid curve to estimate elasticities, the x-elasticity of y measures the fractional response of y to a fraction change in x, which can be written as:

$$x - \text{elasticity of } y : \epsilon(x, y) = \frac{dy/y}{dx/x} \quad (11)$$

We incorporate the equation 11 to determine the offer-elasticity of purchase probability. We use historical offer percent values at consumer-item granularity, identified using following criteria in that order: a) average of last 4 weeks non-zero offer percent values of the consumer-item combination b) average of historical non-zero offer percent values of the consumer-item combination c) average of last 4 weeks non-zero offer percent values of all same age consumer-item combinations within that category. Using Equations 10 and 11, we may establish the offer-elasticity of purchase probability equation 12 shown below, k being the offer percent and f(k) being purchase probability.

$$\epsilon(k, f(k)) = f'(k) \times \frac{k}{f(k)} \quad \Rightarrow \quad \epsilon(k, f(k)) = a \times k \times (1 - f(k)) \quad (12)$$

3.4 MULTI-OBJECTIVE OPTIMIZATION

Post estimation of offer-elasticity of purchase probability, for each category, we solve the below multi-objective optimization function (Equation 15) using dynamic programming approach which

converges after meeting the dual objective of a) Net Revenue (R_v) maximization and b) Consumer Retention Rate (R_r) maximization. Lets study the individual components of the optimization function in detail. Net Revenue from i^{th} consumer-item sample (R_{v_i}) can be expressed as Equation 13, and Consumer Retention Rate of i^{th} consumer-item sample (R_{r_i}) can be expressed as Equation 14.

$$R_{v_i} = [I_p - \frac{I_p}{100} \times (k \pm \eta \times k)] \times \mathbb{1}_c(f(k) \pm \eta \times \epsilon(k, f(k)) \times f(k)) \text{ , where } \eta \in (0, 1) \quad (13)$$

$$R_{r_i} = \mathbb{1}_c(f(k) \pm \eta \times \epsilon(k, f(k)) \times f(k)) \text{ , where } \mathbb{1}_c(x) := \begin{cases} 1 & x \geq c \\ 0 & \text{Otherwise} \end{cases} \quad (14)$$

I_p is the price of the i^{th} item, k being the offer percent and $f(k)$ being purchase probability. η is the change in offer percent k . $\mathbb{1}_c()$ denotes the Indicator function as can be seen in Equation 14. $\epsilon(k, f(k))$ denotes the k percent offer-elasticity of $f(k)$ purchase probability.

Now, using Equations 13 and 14, we formulate our constraint based multi-objective optimization function which calculates the optimal offer percent for each of the consumer-item sample, as can be seen below in Equation 15

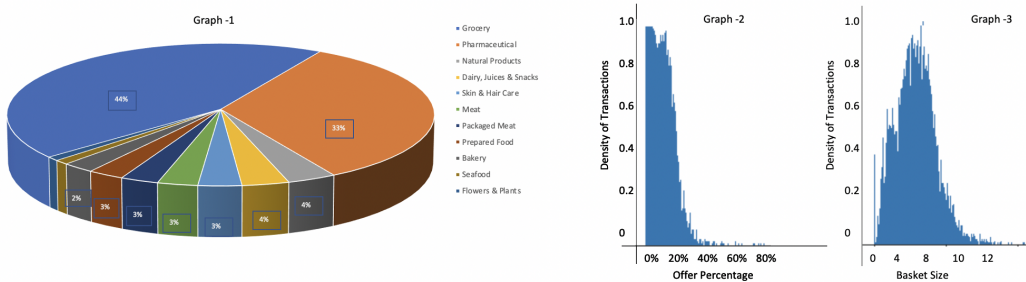
$$\begin{aligned} \max_{\eta, \lambda, \gamma} \quad & \lambda \sum_{i=1}^n R_{v_i} + \gamma \frac{1}{n} \sum_{i=1}^n R_{r_i} \\ \text{s.t.} \quad & \eta, \lambda, \gamma \in (0, 1) \\ & \lambda + \gamma = 1 \\ & \frac{1}{n} \sum_{i=1}^n R_{r_i} \geq R_{rc} \\ & (k \pm \eta \times k) \in (0, 50] \end{aligned} \quad (15)$$

Above in the equation, n is the total consumer-item samples modelled for a particular category. λ and γ are learned optimal weights for Net Revenue and Consumer Retention Rate respectively. R_{rc} denotes the Retention rate cut-off of category c . This is determined using the latest 2 weeks of consumer-item samples.

4 EXPERIMENTS AND RESULTS

We use kaggle dataset available at AmExpert 2019. Figure 7 shows the schema of the data we have used to build our models. As mentioned in Section 3, we use a maximum of 1 year data aggregated at bi-weekly level at consumer-item granularity. We split the data into three part train, validation and test based on our validation strategy. We generate consumer - item - bi-weekly data with purchase/ non purchase being the target , and use this data to train all our models.

Figure 3: Exploratory Data Analysis



4.1 EXPERIMENT SETUPS

We start with exploratory data analysis, looking at the data from various cuts. We study the variations of different features with our target (purchase/ non purchase). Some of our studies include category-

wise sales distribution, density of transactions with varying offer percent and density of transactions with varying basket size (Figure 3). We observe that Grocery and Pharmaceutical contributes to 77%. We also look at order probability variations at different temporal cuts like week, month and quarter, transactional metrics like total orders, total reorders, recency, gap between orders, at both consumer and item levels. We then perform multiple experiments with the above mentioned features and different hyperparameter configurations to land at reasonable hyperparameters to perform final experiments and present our results.

Figure 4: Category graphs

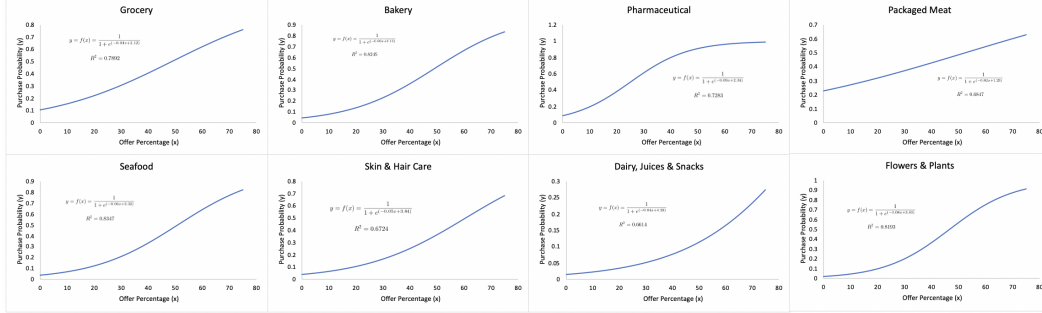
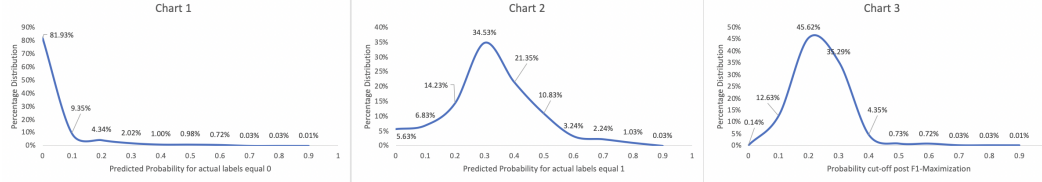


Figure 5: Probability Distributions



4.2 RESULTS AND OBSERVATIONS

Figure 4 shows the functional relationship of offer percentage with purchase probability obtained across different categories. It also contains the equations and goodness of fit in the form of R^2 for each category. Seafood and Bakery are the top 2 best fitted categories with R^2 values of 0.83 and 0.82 respectively. Figure 5 Chart-1 and Chart-2 shows the predicted probability distributions of actual label equals 0 and 1 respectively over the validation data split. Chart-3 shows the cut-off probability distribution post F_1 -Maximization, and, we observe that highest density of cut-off probability lies between 0.2 to 0.3. Table 1 presents the accuracy values post Modelling and F_1 -Maximization. It also has the average elasticity values along with weighted offer percent computed post optimization. From model performance perspective, it is observed that Grocery category has least BCELoss of 0.0283. Pharmaceutical and Meat categories followed Grocery with BCELoss of 0.0296 and 0.0299 respectively. Also, Grocery has the best F_1 score of 0.512 followed by Meat and Pharmaceutical scoring 0.511 and 0.509 respectively. Vegetables is the most elastic category with elasticity value of 1.53, whereas Packaged meat and Skin and Hair care are the least elastic categories with elasticity value of 0.62. From Figure 6, we can see the graphical representation of distribution of optimal offer calculated through optimization. We find Skin and Hair care along with Pharmaceutical to be left skewed, whereas Vegetables as well as Flowers and Plants to be right skewed.

Figure 6: Optimal Offers

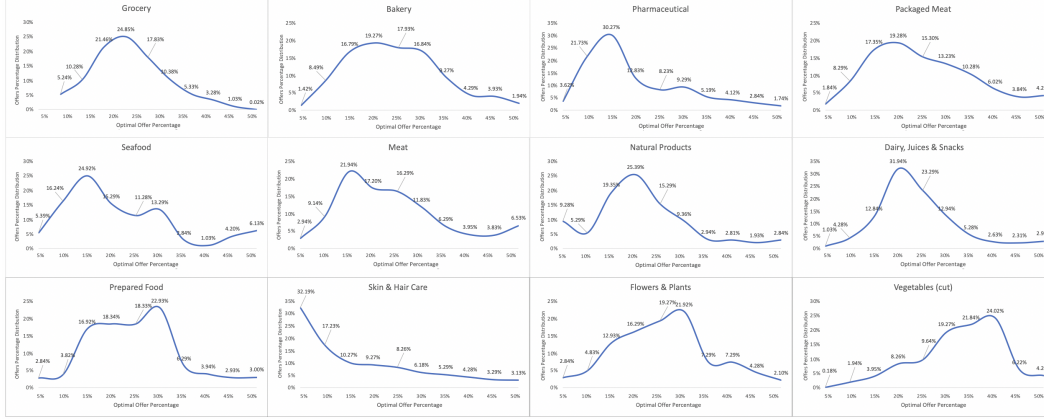


Table 1: Model Results and Elasticity

Category	Sample size	BCELoss	Precision	Recall	F ₁ -Score	Avg Elasticity	Weighted Offer Percent
Grocery	28,990	0.0283	0.524	0.501	0.512	1.13	23.37
Bakery	1,628	0.0415	0.346	0.391	0.367	1.06	22.15
Pharmaceutical	20,492	0.0296	0.538	0.483	0.509	0.73	17.89
Packaged Meat	1,473	0.0329	0.473	0.452	0.462	0.62	19.15
Seafood	539	0.0382	0.497	0.379	0.43	0.89	16.23
Natural Products	2,399	0.0319	0.451	0.524	0.485	0.95	21.78
Dairy, Juices, Snacks	2,060	0.0396	0.394	0.492	0.438	1.04	22.02
Prepared Food	1,407	0.0472	0.338	0.295	0.315	1.03	28.27
Skin, Hair Care	1,906	0.0391	0.429	0.453	0.441	0.62	7.93
Meat	1,767	0.0299	0.498	0.524	0.511	0.94	18.92
Flowers, Plants	491	0.0483	0.275	0.318	0.295	1.43	30.24
Vegetables (cut)	124	0.0469	0.364	0.267	0.308	1.53	37.92

4.3 INDUSTRIAL APPLICATIONS

Offer Personalization framework has multiple applications in the retail industry. Some of them include: **Personalized Marketing:** Optimal offer rollouts can be made at consumer-item granularity. **Inventory Planning:** Consumer preference model used to compute optimal offers can also be used in better short term inventory planning (2-4 weeks), which is largely dependant over what consumer is going to purchase in the near future.

5 CONCLUSION

We have presented our detailed methodology to solve the offer optimization problem at the intersection of consumer, item and time in retail setting. We have also presented the results of our models and optimization in the form of model accuracies and graphical representations at a category level. At the same time we understand that computation strategy is a key aspect in modelling millions of consumers, and we intend to further explore this aspect by building Transfer Learning framework Yosinski et al. (2014). We are also working to further improve our Sequence to Sequence neural network architectures to improve accuracy and decrease computation time.

REFERENCES

- Yoshua Bengio and MONTREAL CA. Rmsprop and equilibrated adaptive learning rates for non-convex optimization. *corr abs/1502.04390*, 2015.
- Pavel Izmailov, Dmitrii Podoprikin, Timur Garipov, Dmitry Vetrov, and Andrew Gordon Wilson. Averaging weights leads to wider optima and better generalization. *arXiv preprint arXiv:1803.05407*, 2018.
- Colin Lea, Rene Vidal, Austin Reiter, and Gregory D Hager. Temporal convolutional networks: A unified approach to action segmentation. In *European Conference on Computer Vision*, pp. 47–54. Springer, 2016.
- Zachary C Lipton, Charles Elkan, and Balakrishnan Naryanaswamy. Optimal thresholding of classifiers to maximize f1 measure. In *Joint European Conference on Machine Learning and Knowledge Discovery in Databases*, pp. 225–239. Springer, 2014.
- Leslie N Smith. Cyclical learning rates for training neural networks. In *2017 IEEE Winter Conference on Applications of Computer Vision (WACV)*, pp. 464–472. IEEE, 2017.
- Jason Yosinski, Jeff Clune, Yoshua Bengio, and Hod Lipson. How transferable are features in deep neural networks? In *Advances in neural information processing systems*, pp. 3320–3328, 2014.
- Manzil Zaheer, Sashank Reddi, Devendra Sachan, Satyen Kale, and Sanjiv Kumar. Adaptive methods for nonconvex optimization. In *Advances in neural information processing systems*, pp. 9793–9803, 2018.

A APPENDIX

Figure 7: Exploratory Data Analysis

