

Bertelsmann Tech Scholarship - Data Track

9.18 UNC

Introduction to Data Analysis & Programming

The median is the "middle" of the data \neq average;
half of the data values $<$ median $<$ half are greater.

9.22 Find Median with Outlier

- Get median between 2 medians by get average.
- Median = best measure of central tendency in highly skewed distribution

9.24 Order Measures of Center 1

9.25 Order Measures of Center 2

- Symmetrical, Normal distribution. mean = median = mode

9.27 Udacians' Facebook Friends - Mean

=average(B2:B28) --> Formula for the mean of dataset.

9.28 Udacians' Facebook Friends - find Median

- Menu > Data > Sort range

> Sort by Column B - A -> Z

9.29 Formula Location of Median -->

- Using symbol notation.

9.30 Wrap Up - Measures of Center

Here is a short doc outlining Mean,

Median, and Mode.

<http://tinyurl.com/measureOfCenter>

LESSON 10

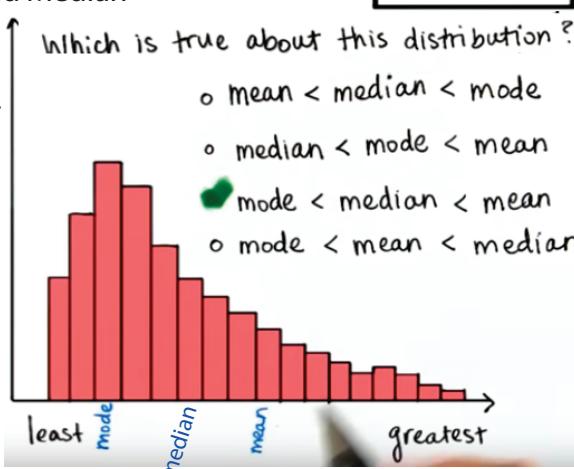
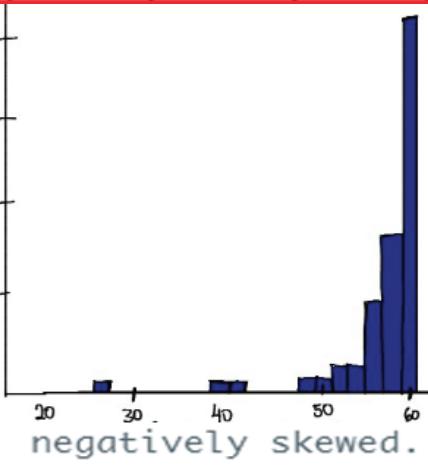
PS 3a: Central Tendency

10.4 Quiz 4. What Distribution?

Measures of Center

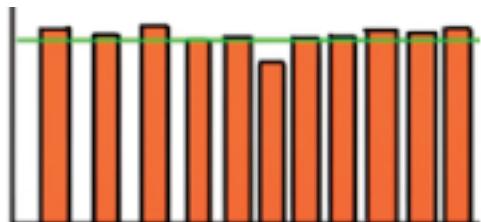
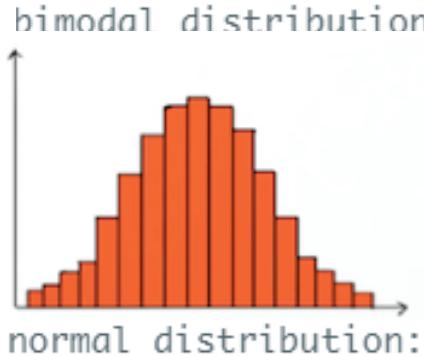
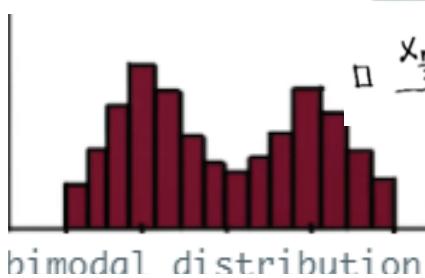
Has a simple equation
Will always change if any data value changes
Not affected by change in bin size
Not affected severely by outliers
Easy to find on a histogram

$\checkmark \frac{\sum x}{n}$	\checkmark	\checkmark		
		\checkmark	\checkmark	highest frequency
		\checkmark	\checkmark	

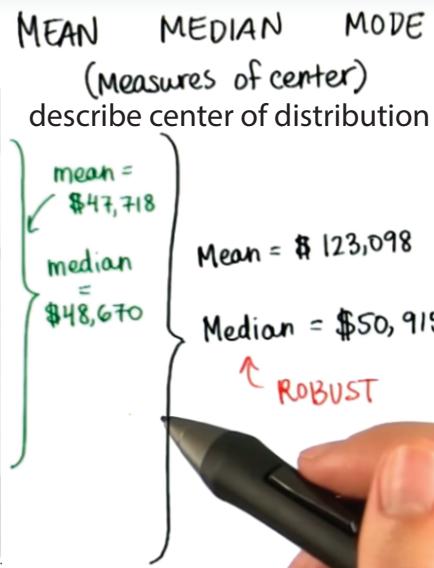


Rank	Value ($x_i - i^{\text{th}}$ value)
1	x_1
2	x_2
3	x_3
:	:
13	x_{13}
14	x_{14} (median)
15	x_{15}
:	:
27	x_{27}

n even $\boxed{\frac{x_{\frac{n}{2}} + x_{\frac{n}{2}+1}}{2}}$ n odd $\boxed{\frac{x_{\frac{n+1}{2}}}{2}}$



uniform distribution:
Each value has the same frequency



Bertelsmann Tech Scholarship - Data Track

LESSON 11

PS 3b: Additional Practice (Optional)

LESSON 12

Variability

12.1 Social Networkers' Salaries

12.2 What's the Difference?

12.6 Mark Zuckerberg the Outlier

12.9 IQR

12.13 Match Boxplots

12.14 Mean Within IQR?

- We can visualize data w/ histogram & Boxplots

12.15 Problem with IQR

12.18 Deviation from Mean

Sample

\$33,219
\$36,254
\$38,801
\$46,335
\$46,840
\$47,596
\$55,130
\$56,863
\$78,070
\$88,830

Deviation from Mean ($x_i - \bar{x}$)

-19,574.80
-16,539.80
-13,992.80
-6,458.80
-5953.80
-5197.80
2336.20
4069.20
25,276.20
36,036.20

Mean

$$\bar{x} = \frac{\sum x}{10} = \$52,793.80$$

12.20 Equation for Average Deviation

Average deviation =

○

$$\circledast \frac{\sum (x_i - \bar{x})}{10}$$

Avg. squared de

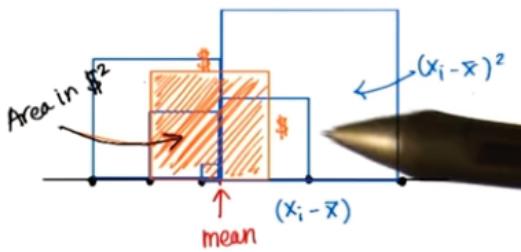
$$= \frac{\sum (x_i - \bar{x})^2}{10} = 291,622,740$$

$$\circledast \frac{\sum (x_i - \bar{x})}{10}$$

VARIANCE

12.27 Average Squared Deviation = Variance

12.29 One Dimension



$$SS = \sum (\text{area of each square}) = \sum (x_i - \bar{x})^2$$

$$\text{Avg. squared deviation} = \frac{\sum (x_i - \bar{x})^2}{n}$$

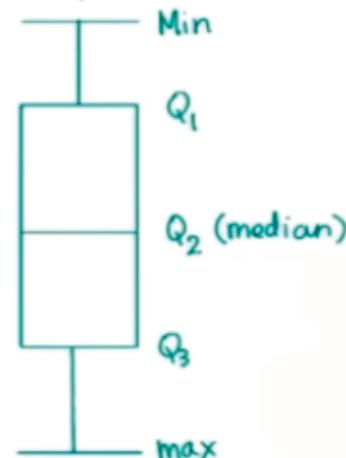
12.31 Calculate Standard Deviation
square root of VARIANCE

$$\sigma = \sqrt{\frac{\sum (x_i - \bar{x})^2}{10}} = 17,071$$

Sample

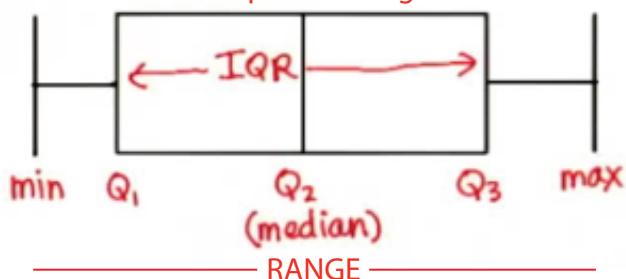
\$38,946
\$43,420
\$49,191
\$50,430
\$50,557
\$52,580
\$53,595
\$54,135
\$60,181
\$10,000,000

Boxplots



Outlier

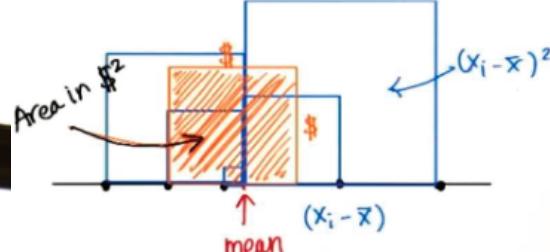
Interquartile Range



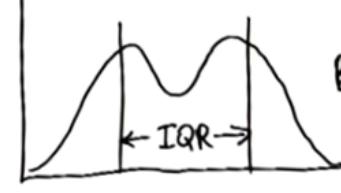
Normal

$$\circledast \frac{\sum (x_i - \bar{x})}{10}$$

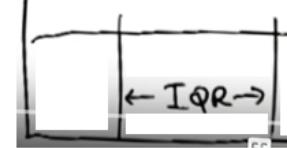
VARIANCE



Bi-modal



Uniform



How do we convert the dimensions of the average square back to one dimension (\$) from two (\$^2)?
② Take the square root

$$\text{Avg. squared de} = \frac{\sum (x_i - \bar{x})^2}{10}$$

VARIANCE

$$= \frac{\sum (x_i - \bar{x})^2}{10} = 291,622,740$$

square root of VARIANCE = σ (sigma)

mean
Standard deviation

Bertelsmann Tech Scholarship - Data Track

12.32 SD Social Networkers

	A	B	C
1	=A1-51511.1	=constant	=B1^2
2	38946	-12565.1	157881738.01
3	43420	-8091.1	65465899.21
4	49191	-2320.1	5382864.00999999
5	50430	-1081.1	1168777.21
6	50557	-954.099999999998	910306.8099999997
7	52580	1068.9	1142547.21
8	53595	2083.9	4342639.21000001
9	54135	2623.9	6884851.21000001
10	60181	8669.9	75167166.01
11	62076	10564.9	11161712.01
12	515111		variance =
13	51511.1	<- average	42996390.09
14	=sum(A1:A10)/10		standard deviation =
15	=average(c1:c10)=		=sqrt(c13) 6557.16326546777

12.33 SD in Words

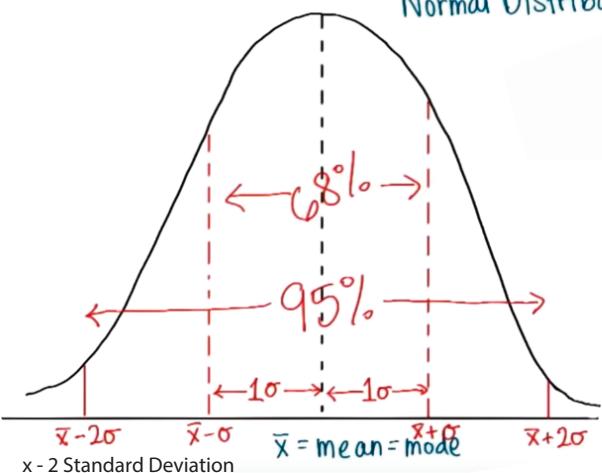
12.34 Spreadsheet SD

$$\sigma = \sqrt{\frac{\sum (x_i - \bar{x})^2}{n}}$$

12.35 Point of SD

What's so great about the standard deviation anyway?

Normal Distribution



What is a way to put the standard deviation in words?
12.33 SD in Words

- Square root of average squared deviation $\sqrt{\frac{\sum (x_i - \bar{x})^2}{n}}$
- (Average squared deviation) Squared $(\frac{\sum (x_i - \bar{x})^2}{n})^2$
- Sum of squared deviations $\sum (x_i - \bar{x})^2 = SS$
- Sum of (absolute deviations squared) = SS
- Square root of ((Sum of squared deviations) divided by n) $\sqrt{\frac{\sum (x_i - \bar{x})^2}{n}}$

12.38 Bessel's Correction

12.39 Clarifying Sample SD

12.38 Bessel's Correction

Population

$$\mu = 18.97$$

$$\sigma = 5.99$$

$$= 2.6$$

Sample
 $n = 9$

Bessel's Correction

$$\text{Standard deviation} = \sqrt{\frac{\sum (x_i - \bar{x})^2}{n-1}}$$

$$\text{Variance} = \frac{\sum (x_i - \bar{x})^2}{n-1}$$

What will this do to the original standard deviation and variance?
 make them bigger
 make them smaller

Sample standard deviation

$$S = \sqrt{\frac{\sum (x_i - \bar{x})^2}{n-1}} \approx \sigma = \sqrt{\frac{\sum (x_i - \bar{x})^2}{n}}$$

(n=5)	$\bar{x} = 3$
5	4
2	1
1	4
0	9
7	16

$$\sum (x_i - \bar{x})^2 = 34 \quad (\text{sum of squares})$$

$$\text{standard deviation of sample} = \sqrt{\frac{34}{5}}$$

sample standard dev.
(S)

$$\text{standard deviation of population} \approx \sqrt{\frac{34}{4}}$$

Bertelsmann Tech Scholarship - Data Track

LESSON 13

PS 4: Variability

L4-24 What Proportion? > L5-5 Range of Propo > L5-19 Prop over 60

13.7 Udacians' Facebook Friends (proportion)

- Proportion = $\text{SUM}(n1:n2)/\text{SUM}(A1:A \text{ last})$
last 2 numbers of 13.6

13.8 Udacians' Facebook Friends (sample sd)

LESSON 14

Standardizing

14.1 Chess

14.2 UCSF Distribution

- Propo data values

14.9 Continuous Distribution

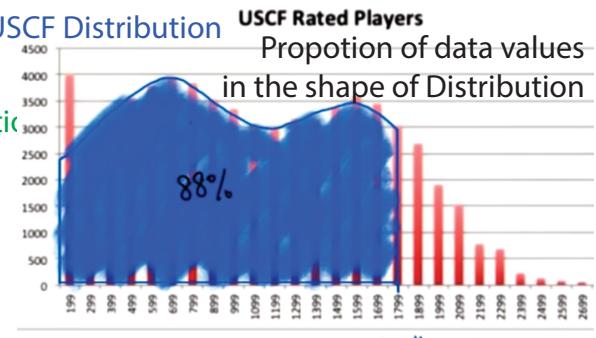
- Theoritically Continuous Distribution, this model use relative frequencies. This equation help to calculate the propo of any 2 values on x axis

$$s_v = \sqrt{\frac{s^2}{n-1}} > s_{sd} \quad 13.8 \text{ (sample sd)}$$

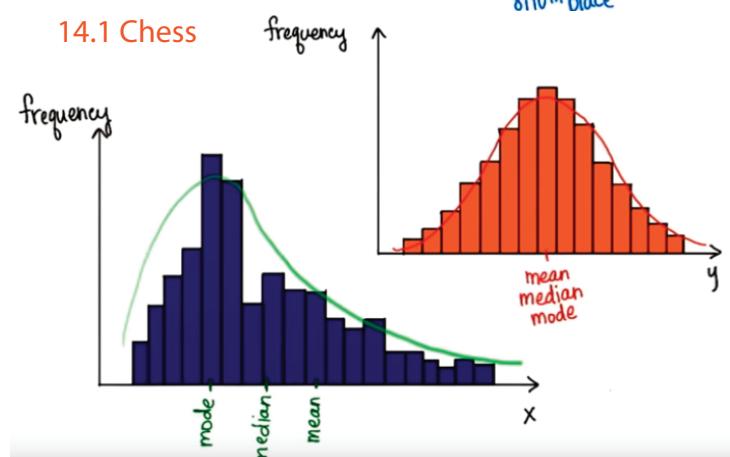
$$= \sqrt{1477.35} > 437.58$$

14.2 UCSF Distribution

Introduction



14.1 Chess

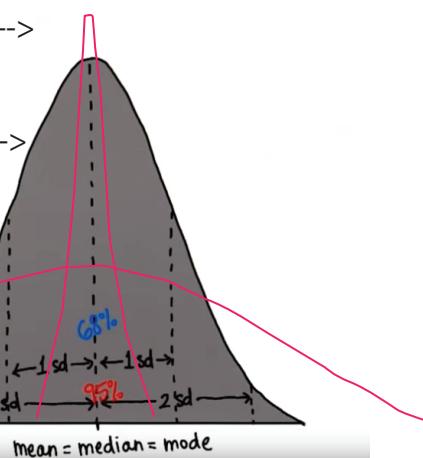


14.10 Theoretical Normal Distribution

Skinny distri. --->

Normal distri. -->

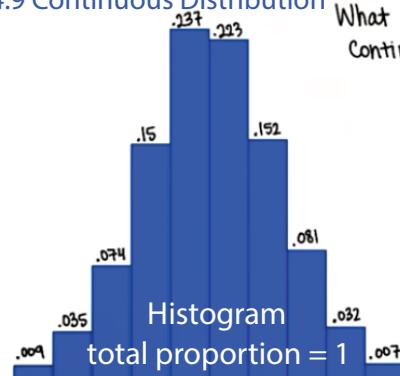
Stretched distri.



14.11 Z

- Location of value on x-axis = SD = standard deviation

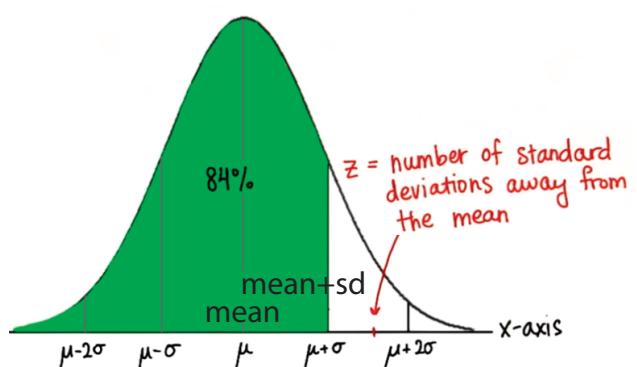
for find the location of data values
14.9 Continuous Distribution



What is the area under our theoretical
Continuous curve?

Proportion = 1

Theoretical
Continuous curve

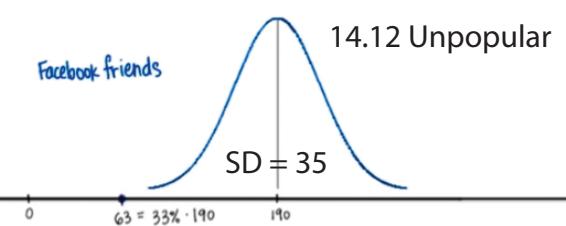
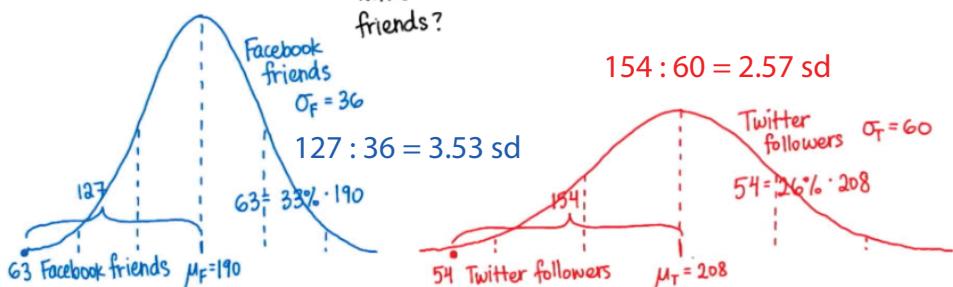


Bertelsmann Tech Scholarship - Data Track

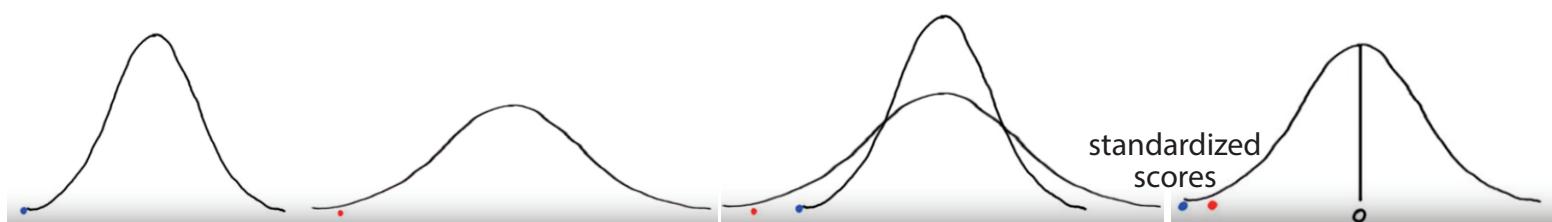
14.12 Unpopular

14.13 Katie - SDs Below

How many standard deviations is Andy's number of Twitter followers from the mean number of Facebook friends?



14.15 Who's More Unpopular?



14.16 Formula for Number of SDs

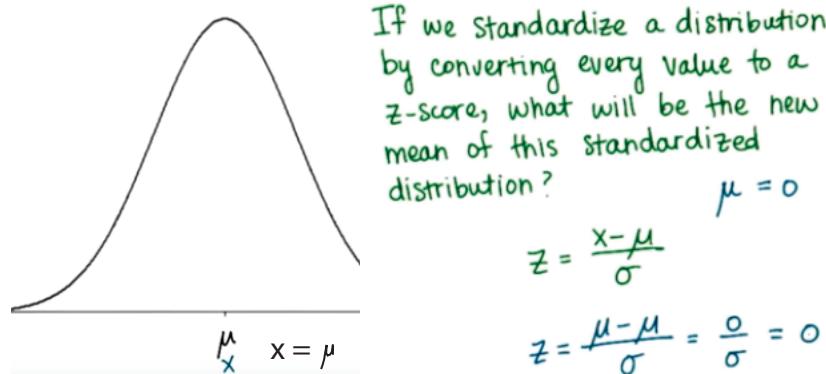
$$\frac{\mu - x}{\sigma}$$

$$Z = \frac{(x - \mu)}{\sigma}$$

14.17 Z-Score

14.19 Mean of Standardized Distribution

$$\mu = 0$$



If we standardize a distribution by converting every value to a z-score, what will be the new mean of this standardized distribution?

$$\mu = 0$$

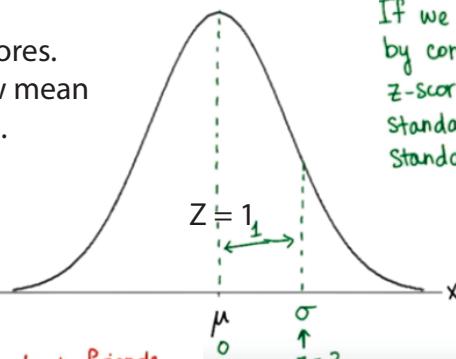
$$z = \frac{x - \mu}{\sigma}$$

$$z = \frac{\mu - \mu}{\sigma} = \frac{0}{\sigma} = 0$$

14.20 SD of Standardized Distribution = 1

- Standardized Distribution by converting values to Z scores.
- Calculate Z score by x subtract the mean to get 0, now mean = 0. Then divide SD we change the shape of distribution.

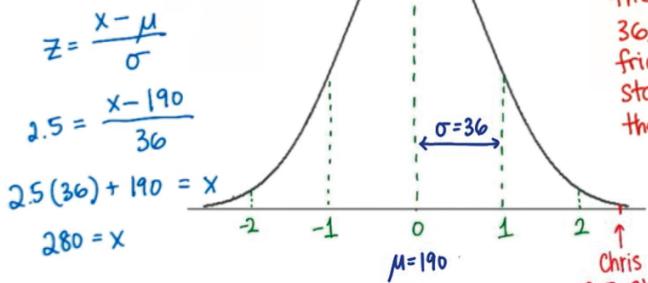
14.22 Popular Chris



$$z = \frac{x - \mu}{\sigma} = \text{sigma}$$

$$\frac{\sigma - 0}{\sigma} = \frac{\sigma}{\sigma} = 1$$

normal distribution
Standard Normal Distribution



How many Facebook friends does Chris have if the mean number of friends is 190, the standard deviation is 36, and the number of friends Chris has is 2.5 standard deviations above the mean?

$$2.5 \text{ std.dev.} = 36 \times 2.5 = 90$$

$$190 + 90 = 280$$

Chris
2.5 Standard deviations
above the mean

Bertelsmann Tech Scholarship - Data

14.24 Convert to Popularity Score

LESSON 15

PS 5a: Standardizing

LESSON 16

PS 5b: Additional Practice (Optional)

16.1 Quiz 7. Mean and SD

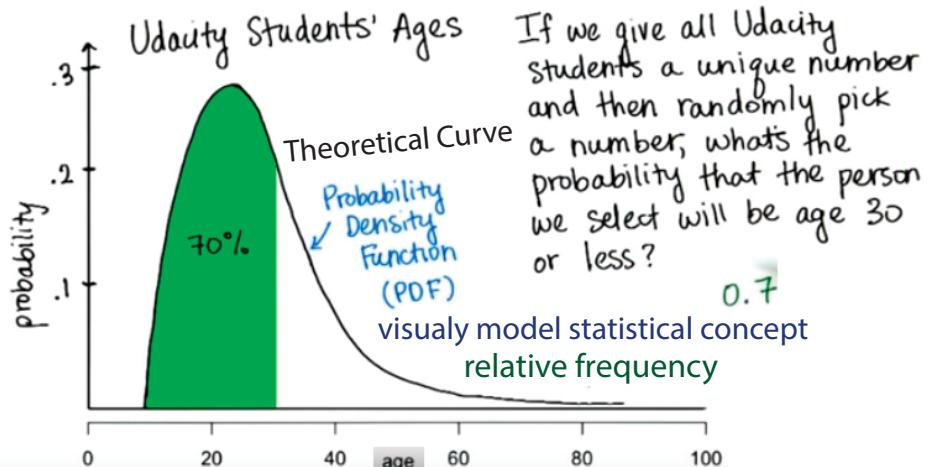
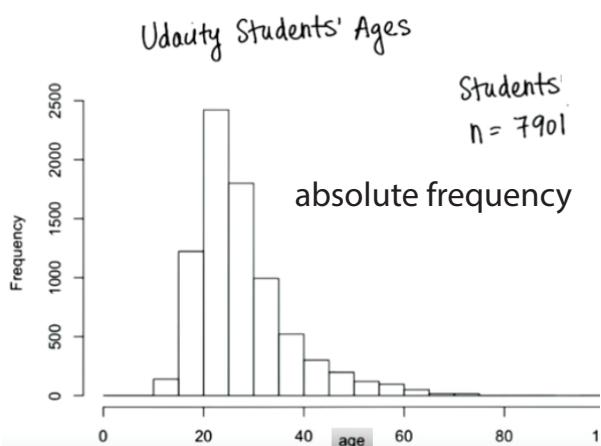
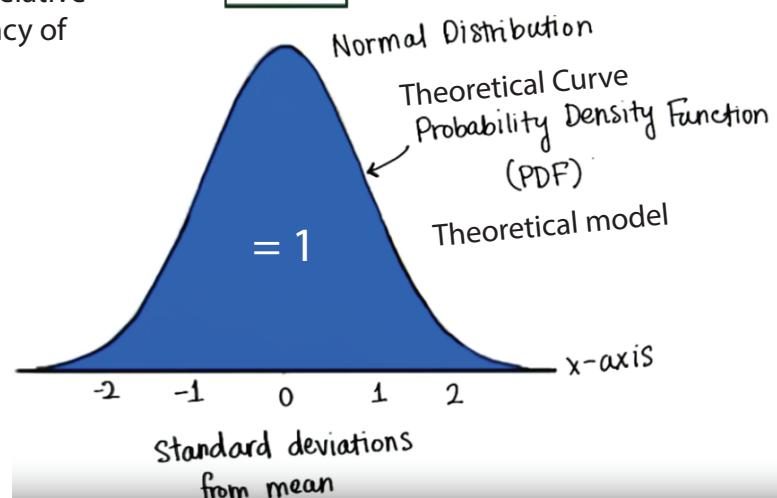
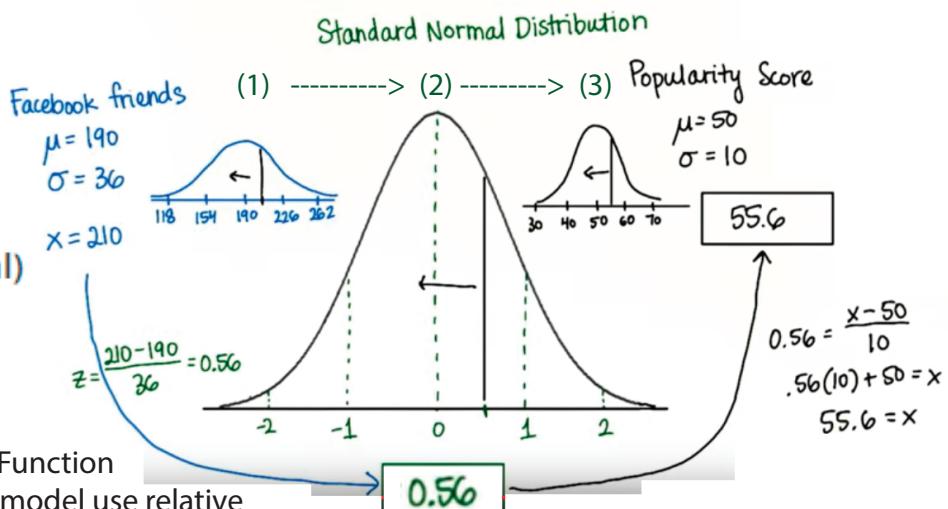
LESSON 17

Normal Distribution

17.1 Intro to the PDF = Probability Density Function

- Theoretically Continuous Distribution, this model use relative frequencies. The curve shape model w/ relative frequency of distribution of data in term of proportions.

17.2 Probability



17.3 Get to Know the PDF

