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## TNSL20 - basic logistic algorithms

### Homework Set 4, 2017

Solutions are due October 13, 2017.

**Question 1 (IMPLEMENTATION):** Implement the algorithm that tests if a given set of vertices  $I$  is an independent set for a given graph  $G = (V, E)$  using the adjacency matrix of the graph. The pseudocode of the algorithm is as follows:

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**Algorithm 1:** Test for independence

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**Input** : Adjacency matrix  $A$ , set of vertices  $I$

**Output:** Boolean value  $t$  (true if  $I$  is an independent set and false otherwise)

```
1 Function is_independent_set ( $A, I$ )
2    $t := \text{true};$ 
3   if  $\text{length}(I) > 1$  then
4     for  $v_{\text{index}} = 1$  TO  $\text{length}(I)-1$  do
5        $v := I[v_{\text{index}}];$ 
6       for  $w_{\text{index}} = v_{\text{index}} + 1$  TO  $\text{length}(I)$  do
7          $w := I[w_{\text{index}}];$ 
8         if  $A[v][w] == 1$  then
9            $t := \text{false};$ 
10        end
11      end
12    end
13  end
14  return  $t$ ;
15 end
```

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Test your code on the adjacency matrix obtained from Homework 2 Question 3 for the graph  $G_2$ .

**Question 2 (IMPLEMENTATION):** Combine the code from Homework 2 Question 3 and Homework 4 Question 1 in order to get a code that works with  $E$  and  $n$  as an input.

Please note that you must create Matlab functions `adjacency_matrix` and `is_independent_set` using the code from Homework 2 Question 3 and Homework 4 Question 1. Description of the input and output variables of the functions you can find in the corresponding files with pseudocode.

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**Algorithm 2:** Test for independence

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**Input** : Edges  $E$ , number of vertices  $n$ , set of vertices  $I$

**Output:** Boolean value  $t$  (true if  $I$  is an independent set and false otherwise)

```

1 Function is_independent_set_without_adjacency_matrix ( $E, n, I$ )
2    $A := \text{adjacency\_matrix}(E, n)$  ;           // algorithm from HW2 Q3
3    $t := \text{is\_independent\_set}(A, I)$  ;         // algorithm from HW4 Q1
4   return  $t$ ;
5 end

```

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