

Computer vision - Problem set 5

Nicolas Six

April 5, 2018

Contents

1	Gaussian and Laplacian Pyramids	1
1.1	Gaussian pyramids	1
1.2	Laplacian pyramid	2
2	Lucas Kanade optic flow	2
2.1	On small movement	2
2.2	On larger movement	3
2.3	Gaussian pyramid	3
3	Hierarchical LK optic flow	3
4	The Juggle Sequence	6

Question 1 Gaussian and Laplacian Pyramids

1.1 Gaussian pyramids

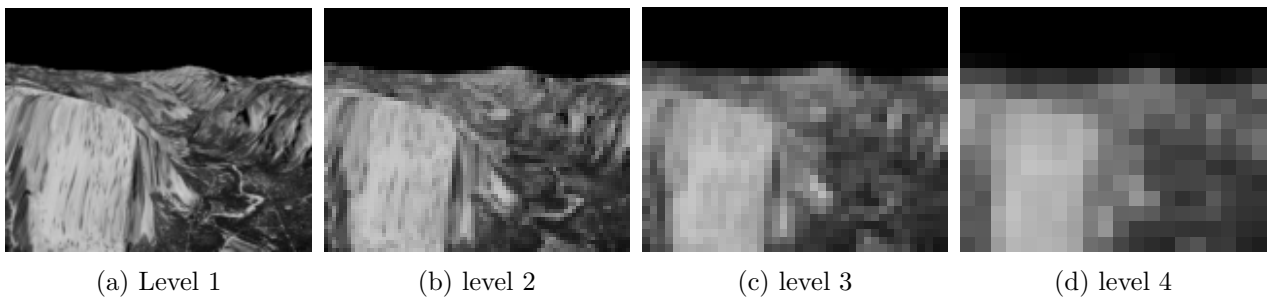


Figure 1: 4 levels Gaussian pyramid

```
1 def gaussian_reduce(im: np.ndarray):  
2     im = cv2.GaussianBlur(im, (3, 3), 0)  
3     im = cv2.resize(im, (0, 0), fx=0.5, fy=0.5,  
4         interpolation=cv2.INTER_NEAREST)  
5     return im
```

1.2 Laplacian pyramid

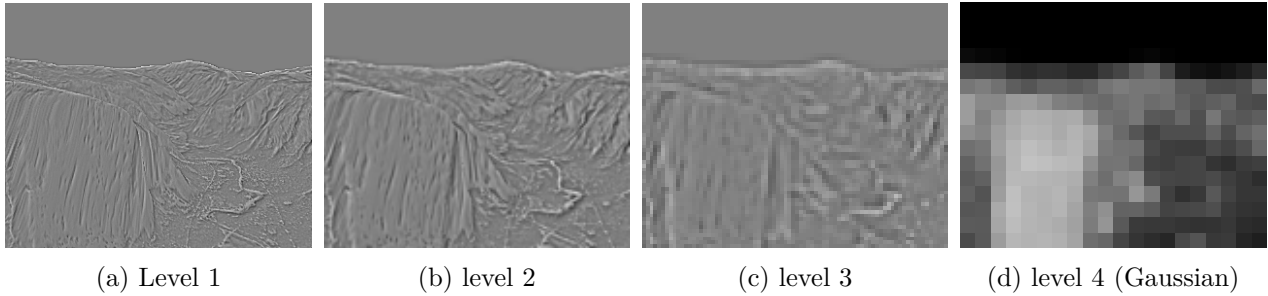


Figure 2: 4 levels Laplacian pyramid

```
1 def gaussian_expand(im: np.ndarray):
2     im = cv2.resize(im, (0, 0), fx=2.0, fy=2.0,
3                     interpolation=cv2.INTER_NEAREST)
4     im = cv2.GaussianBlur(im, (3, 3), 0)
5     return im
6
7 def laplacian_reduce(im: np.ndarray):
8     r = gaussian_reduce(im.copy())
9     e = gaussian_expand(r.copy())
10    im = cv2.resize(im, (e.shape[1], e.shape[0]))
11    return r, im.astype(np.int) - e.astype(np.int)
```

Question 2 Lucas Kanade optic flow

2.1 On small movement

```
1 def lucas_kanade_optic_flow(im1, im2, win_size, blur_size=None):
2     if blur_size is not None:
3         im1 = cv2.GaussianBlur(im1, (blur_size, blur_size), 1,
4                                 borderType=cv2.BORDER_REPLICATE)
5         im2 = cv2.GaussianBlur(im2, (blur_size, blur_size), 1,
6                                 borderType=cv2.BORDER_REPLICATE)
7
8     i_x = compute_gradient(im1, 'X')
9     i_y = compute_gradient(im1, 'Y')
10    i_t = im1.astype(np.int32) - im2.astype(np.int32)
11
12    win = cv2.getGaussianKernel(win_size, 1)
13
14    i_xx_sum = convolve2d(np.power(i_x, 2), win, 'same', boundary='symm')
15    i_yy_sum = convolve2d(np.power(i_y, 2), win, 'same', boundary='symm')
16    i_xy_sum = convolve2d(i_x * i_y, win, 'same', boundary='symm')
17    i_xt_sum = convolve2d(i_x * i_t, win, 'same', boundary='symm')
18    i_yt_sum = convolve2d(i_y * i_t, win, 'same', boundary='symm')
```

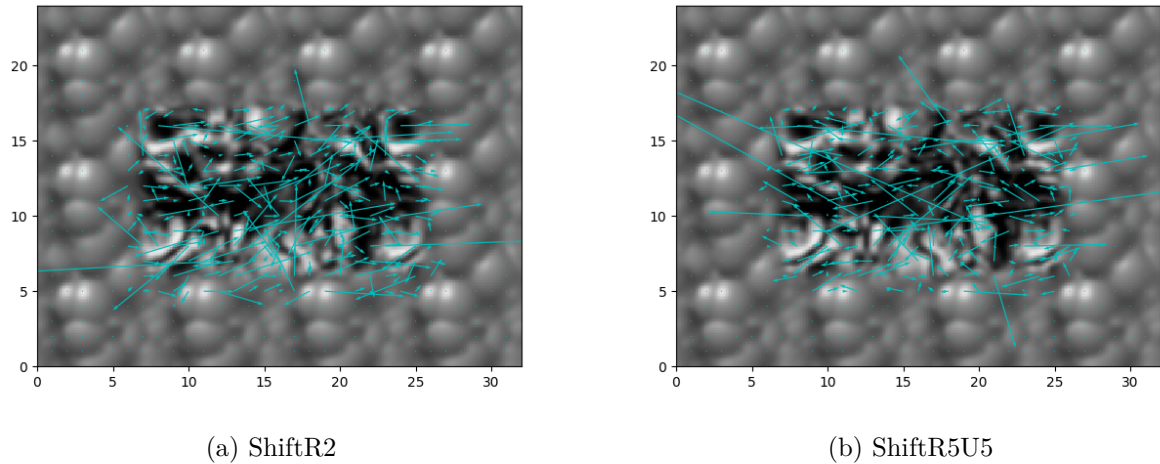


Figure 3: Lucas Kanade displacement arrows drawn over original image, computed after adding a 51px Gaussian blur

```

19     det = np.power(i_xx_sum * i_yy_sum - i_xy_sum**2, -1)
20
21     inds = np.where(np.isinf(det))
22     det[inds] = 0.0
23
24     vx = (-i_yy_sum * i_xt_sum + i_xy_sum * i_yt_sum) * det
25     vy = ( i_xy_sum * i_xt_sum - i_xx_sum * i_yt_sum) * det

```

2.2 On larger movement

We verify, here, that Lucas Kanade does not work well on big movement. If the general movement is still globally in the right direction, the bigger is the shift, the bigger is the noise.

2.3 Gaussian pyramid

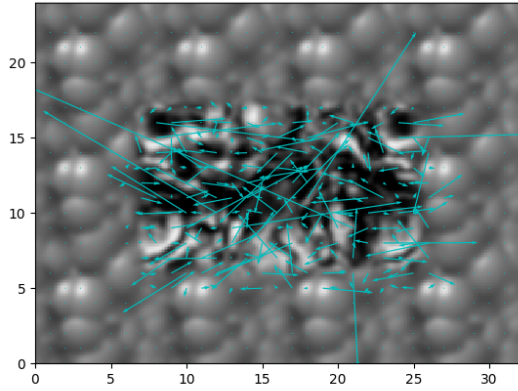
```

1 def wrap(im: np.ndarray, vx: np.ndarray, vy: np.ndarray):
2     map1 = vx + np.array(range(vx.shape[0])).reshape((vx.shape[0], 1))
3     map2 = vy + np.array(range(vy.shape[1])).reshape((1, vy.shape[1]))
4     im = im[:vx.shape[0], :vx.shape[1]]
5     ret = cv2.remap(im, map2.astype(np.float32), map1.astype(np.float32),
6                     cv2.INTER_NEAREST)
7     return ret

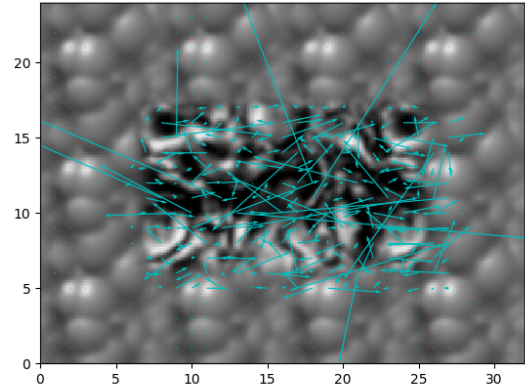
```

On Figure 6, you can see that the wrapped image does not allow to recover the destination image. We were expecting better results, but did not find how to get them.

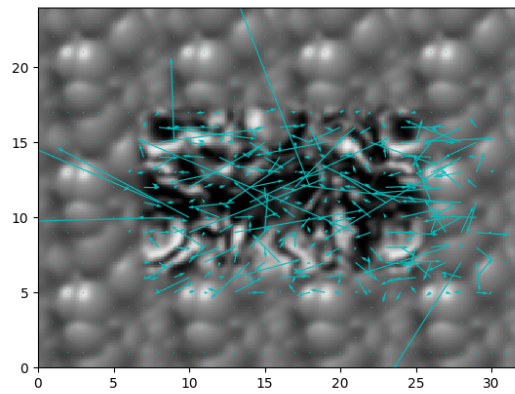
Question 3 Hierarchical LK optic flow



(a) ShiftR10



(b) ShiftR20



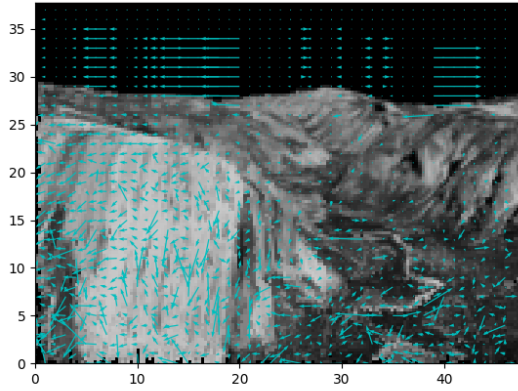
(c) ShiftR40

Figure 4: Lucas Kanade displacement arrows draw over original image, computed after adding a 51px Gaussian blur

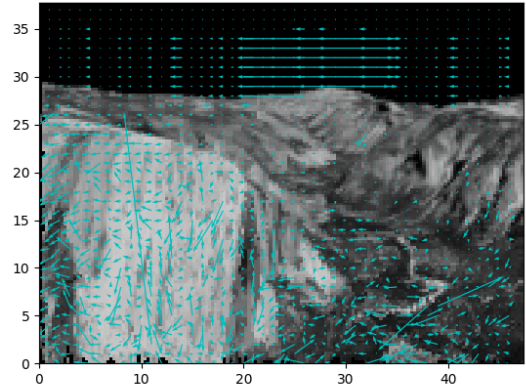
```

1 def hierarchical_lk(im1, im2, level, win_size=5, blur_size=None):
2     sr = []
3     imgs = (im1, im2)
4     sr.append(imgs)
5     for lvl in range(level):
6         imgs = gaussian_reduce(imgs[0]), gaussian_reduce(imgs[1])
7         sr.append(imgs)
8
9     vx = np.zeros(sr[-1][0].shape, dtype=np.float64)
10    vy = np.zeros(sr[-1][0].shape, dtype=np.float64)
11    for lvl in range(level, -1, -1):
12        w, h = sr[lvl][0].shape
13        vx = vx[:w, :h]
14        vy = vy[:w, :h]
15        im_l0 = wrap(sr[lvl][0], vx, vy)
16        new_vx, new_vy = lucas_kanade_optic_flow(im_l0, sr[lvl][1],
17                                                win_size, blur_size)

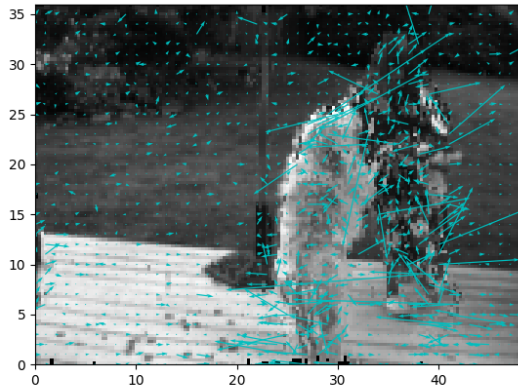
```



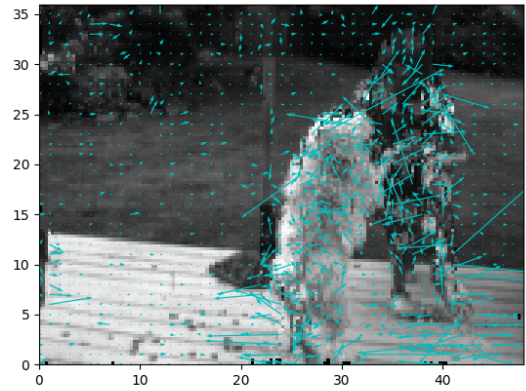
(a) Yosemite image 1



(b) Yosemite image 2

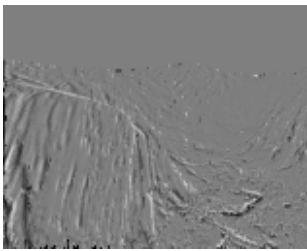


(c) Dog 0

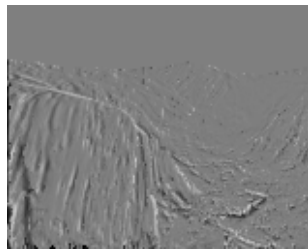


(d) Dog 1

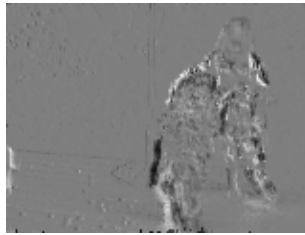
Figure 5: Lucas Kanade displacement arrows draw over original image



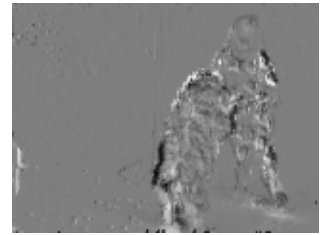
(a) Yosemite image 1



(b) Yosemite image 2



(c) Dog 0



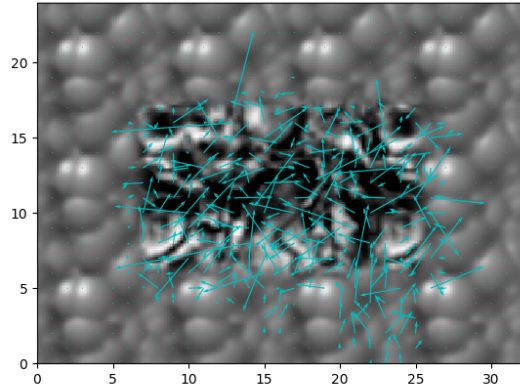
(d) Dog 1

Figure 6: Difference between the wrapped and destination image

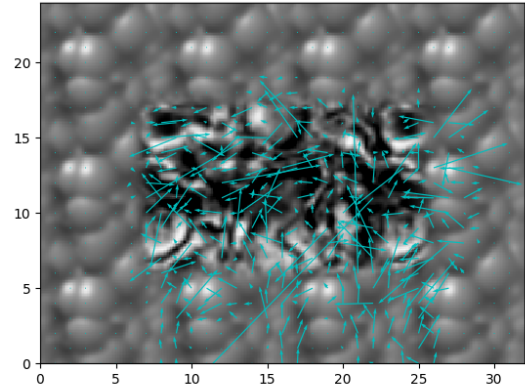
```

17     vx += new_vx
18     vy += new_vy
19     if lvl != 0:
20         vx, vy = gaussian_expnd(vx), gaussian_expnd(vy)
21
22     return vx, vy

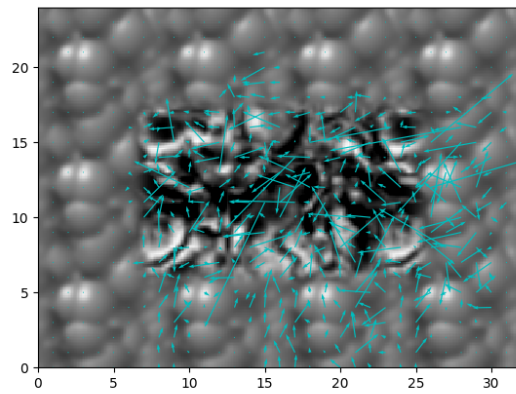
```



(a) shiftR10

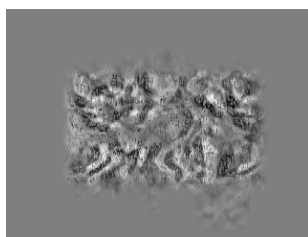


(b) shift20

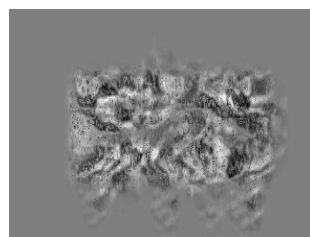


(c) shiftR40

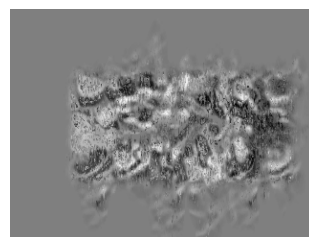
Figure 7: Lucas Kanade displacement arrows draw over original image



(a) shiftR10



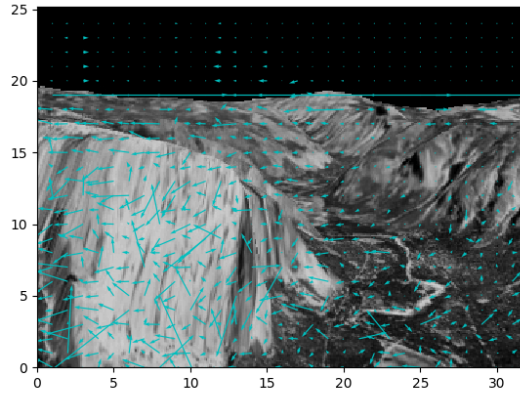
(b) shift20



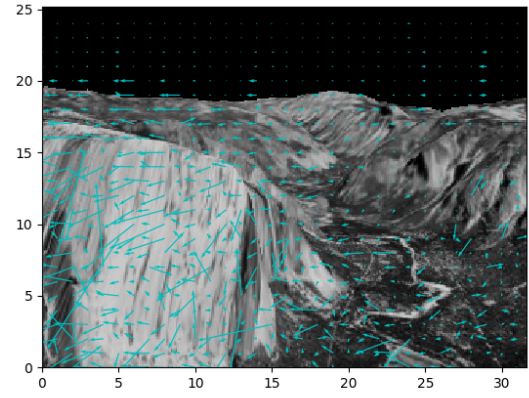
(c) shiftR40

Figure 8: Difference between the wrapped and destination image

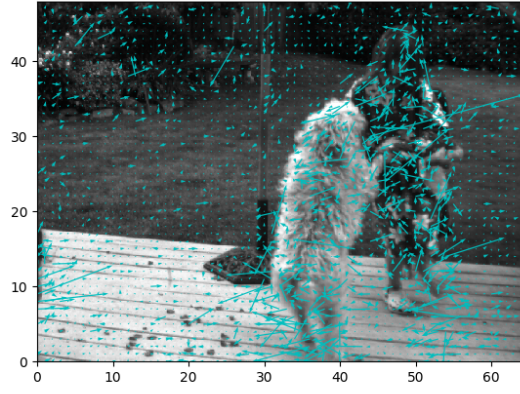
Question 4 The Juggle Sequence



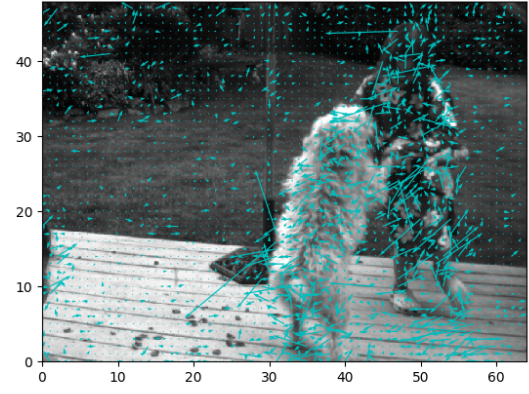
(a) Yosemite image 1



(b) Yosemite image 2

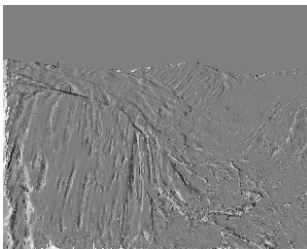


(c) Dog 0

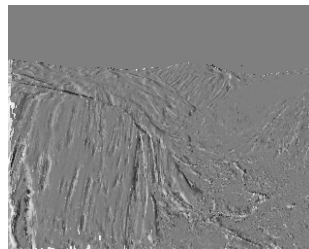


(d) Dog 1

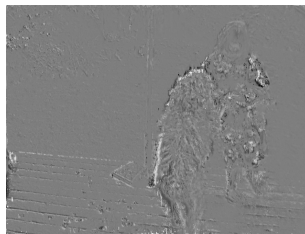
Figure 9: Lucas Kanade displacement arrows draw over original image



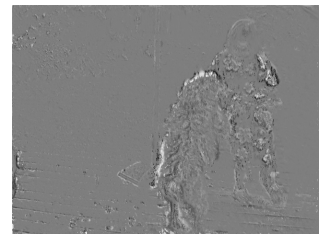
(a) Yosemite image 1



(b) Yosemite image 2

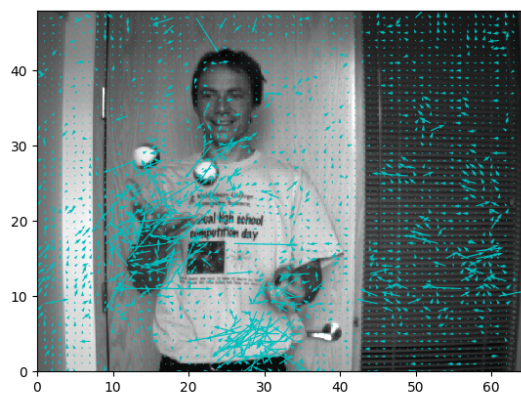


(c) Dog 0

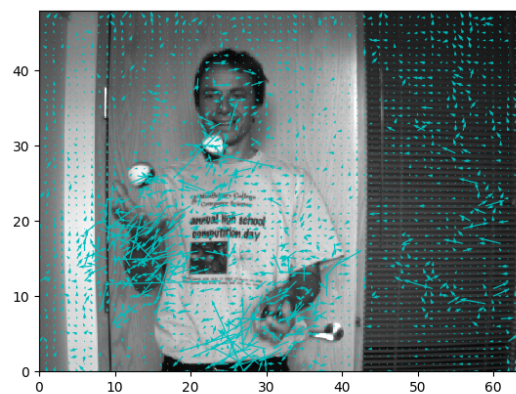


(d) Dog 1

Figure 10: Difference between the wrapped and destination image

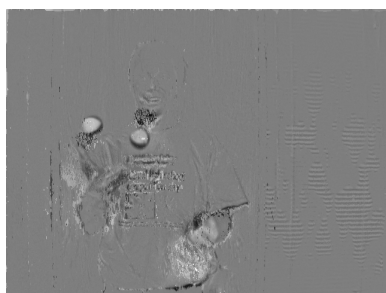


(a) Juggle 1

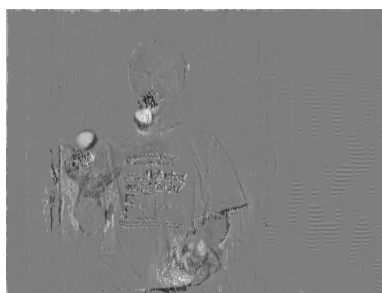


(b) Juggle 2

Figure 11: Lucas Kanade displacement arrows draw over original image



(a) Juggle 1



(b) Juggle 2

Figure 12: Difference between the wrapped and destination image