

NPRE 321 HW 1

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1.
 - i: $\lambda_D = \sqrt{\frac{\epsilon_0 k T}{n e^2}} = \sqrt{\frac{8.854 \times 10^{-12} \times 3 \times 11604 \times 1.38 \times 10^{-23}}{10^{17} \times (1.62 \times 10^{-19})^2}} = \boxed{4.071 \times 10^{-5} \text{ m}}$
 - ii: $\frac{4}{3} \pi \lambda_D^3 = \frac{4}{3} \times 3.1415 \times (4.071 \times 10^{-5})^3 = 2.826 \times 10^{-13} \text{ m}^3$
 $nV = 10^{17} \times 2.826 \times 10^{-13} = \boxed{28263.272}$
2.
 - i: setting $\begin{cases} \rho = 10^{20} \text{ m}^{-3} \\ T = 10^3 \text{ eV} \end{cases}$ As environment in magnetic fusion experiment, while setting it to hydrogen plasma.
 $\lambda_D = 7430 \sqrt{\frac{T}{n}} = 2.35 \times 10^{-5} \text{ m}$
 $\omega_e = \sqrt{\frac{n_e e^2}{\epsilon_0 m_e}} = 5.64 \times 10^{11}$
 $\omega_i = \sqrt{\frac{n_i e^2}{\epsilon_0 m_i}} = 1.31627 \times 10^{10}$
 - ii: setting $\begin{cases} \rho = 10^{25} \text{ m}^{-3} \\ T = 10^5 \text{ eV} \end{cases}$ As environment in magnetic fusion reactors, while setting it to hydrogen plasma.
 $\lambda_D = 7430 \sqrt{\frac{T}{n}} = 7.43 \times 10^{-7} \text{ m}$
 $\omega_e = \sqrt{\frac{n_e e^2}{\epsilon_0 m_e}} = 1.78 \times 10^{14}$
 $\omega_i = \sqrt{\frac{n_i e^2}{\epsilon_0 m_i}} = 4.1624 \times 10^{12}$
 - iii: setting $\begin{cases} \rho = 10^7 \text{ m}^{-3} \\ T = 10 \text{ eV} \end{cases}$ As environment in solar wind, while setting it to hydrogen plasma.
 $\lambda_D = 7430 \sqrt{\frac{T}{n}} = 7.43 \text{ m}$
 $\omega_e = \sqrt{\frac{n_e e^2}{\epsilon_0 m_e}} = 1.78 \times 10^5$
 $\omega_i = \sqrt{\frac{n_i e^2}{\epsilon_0 m_i}} = 4.16 \times 10^3$

3.

$$\oint B dl = \mu_0 \sum I$$

$$B \times 2\pi r = \mu_0 NI$$

$$B = \frac{\mu_0 NI}{2\pi r}$$

4. i: $1 \times 10^4 \times e \times 1 = \boxed{1.602 \times 10^{-15} \text{ J}}$

ii: $10^4 \times 11604 = \boxed{1.16 \times 10^8 \text{ K}}$

iii: $v = \sqrt{\frac{8KT}{\pi m}} = \boxed{6.69 \times 10^7 \text{ m/s}}$

5.

i: $v_i = \sqrt{\frac{8KT_i}{\pi m_i}} = \sqrt{\frac{8 \times 1.38 \times 10^{-23} \times 100 \times 11604}{1.008665 \times 1.673 \times 10^{-27}}} = \boxed{2.755 \times 10^5 \text{ m/s}}$

$v_e = \sqrt{\frac{8KT_e}{\pi m_e}} = \sqrt{\frac{8 \times 1.38 \times 10^{-23} \times 1000 \times 11604}{9.11 \times 10^{-31}}} = \boxed{3.74998 \times 10^7 \text{ m/s}}$

ii: $\omega_e = \sqrt{\frac{n_e e^2}{\epsilon_0 m_e}} = \sqrt{\frac{10^{17} \times (1.602 \times 10^{-19})^2}{8.854 \times 10^{-12} \times 9.11 \times 10^{-31}}} = \boxed{1.784 \times 10^{10}}$

$\omega_i = \sqrt{\frac{n_e e^2}{\epsilon_0 m_i}} = \sqrt{\frac{10^{17} \times (1.602 \times 10^{-19})^2}{8.854 \times 10^{-12} \times 1.673 \times 10^{-27}}} = \boxed{4.1624 \times 10^8}$

iii: $f_e = \frac{\omega_e}{2\pi} = 2.8397 \times 10^9 \text{ Hz} = 2839.7 \text{ MHz}$
 $f_i = \frac{\omega_i}{2\pi} = 6.6247 \times 10^7 \text{ Hz} = 66.247 \text{ MHz}$ Thus, it will be heating ions.

iv: $f = \frac{Bq}{2\pi m} = 7.6 \times 10^7 = \frac{B \times 1.602 \times 10^{-19}}{2\pi \times 1.673 \times 10^{-27}}$, Thus, $B = \boxed{4.98686 \text{ T}}$

v: $r_i = \frac{v_i}{\omega_i} = \frac{2.755 \times 10^5}{4.1624 \times 10^8} = \boxed{6.6187 \times 10^{-4} \text{ m}}$