

# Regression Analysis I

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```
library(GLMsData)
data(AIS)
library(dplyr)
AIS_f<-AIS%>%filter(Sex=='F')
```

This file is one of the regression analysis papers. Here you can find:

- Plots
- Correlations
- Identifying the best model
- Influence and leverage points
- Residuals examination
- Variance examination

Physical measurements and blood measurements from high performance athletes at the AIS, this dataset contain information about 98 athletes and it is a subset of the data(AIS) in the library GLMsData. The function `summary` was used to obtain the following result

```
library(readxl)
colnames(AIS_f)

## [1] "Sex" "Sport" "LBM" "Ht" "Wt" "BMI" "SSF" "RBC"
## [9] "WBC" "HCT" "HGB" "Ferr" "PBF"

atletas<-subset(AIS_f,select = c("LBM", "Ht", "Wt", "BMI", "SSF"))
```

The summary function is an excellent option to see a brief description of each variable, finding here all of the quantiles.

```
summary(atletas)
```

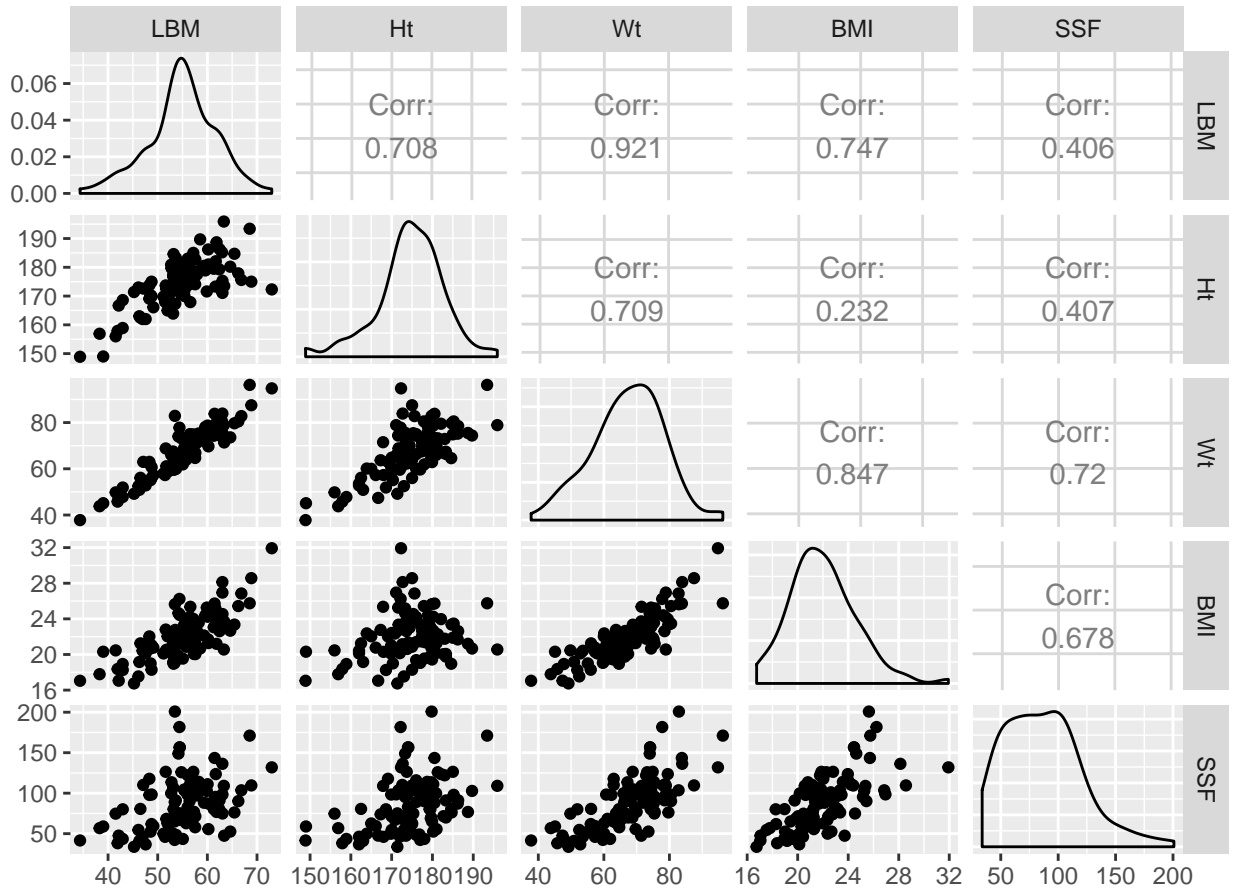
	LBM	Ht	Wt	BMI
## Min.	:34.36	Min. :148.9	Min. :37.80	Min. :16.75
## 1st Qu.	:51.93	1st Qu.:171.0	1st Qu.:60.08	1st Qu.:20.27
## Median	:54.92	Median :175.0	Median :68.05	Median :21.82
## Mean	:54.89	Mean :174.6	Mean :67.34	Mean :21.99
## 3rd Qu.	:59.40	3rd Qu.:179.7	3rd Qu.:74.42	3rd Qu.:23.39
## Max.	:72.98	Max. :195.9	Max. :96.30	Max. :31.93
##	SSF			
## Min.	: 33.80			
## 1st Qu.	: 59.27			
## Median	: 81.80			
## Mean	: 86.97			
## 3rd Qu.	:107.42			
## Max.	:200.80			

## Scatterplot matrix

Another good option is looking a matrix with all the scatterplots. For example we can see that Wt and BMI have a linear behavior with the response variable (LBM), and the other variables even when some of them

have an approximate linear behavior is easy to see that these ones are more dispersed, for example: Ht and SSF.

```
library(GGally)
ggpairs(atletas, columns = 1:ncol(atletas), title = "",
        axisLabels = "show", columnLabels = colnames(atletas))
```

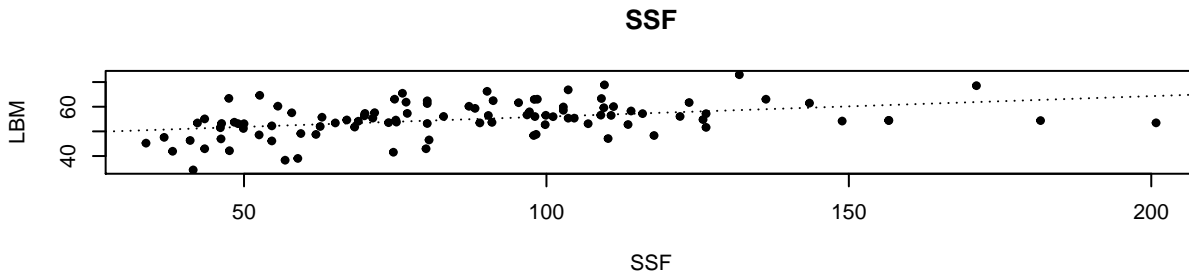
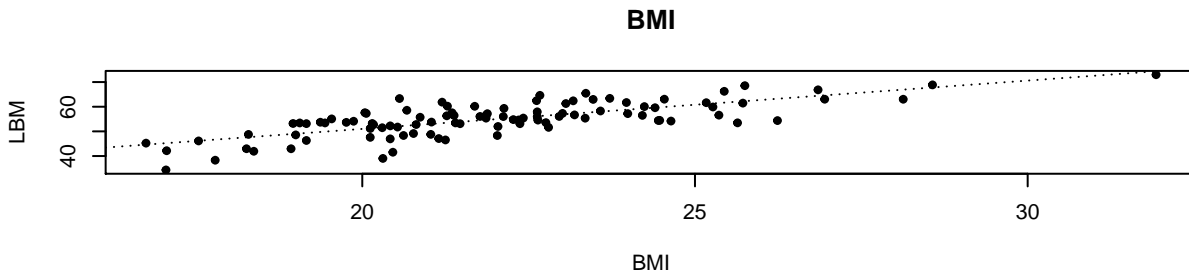
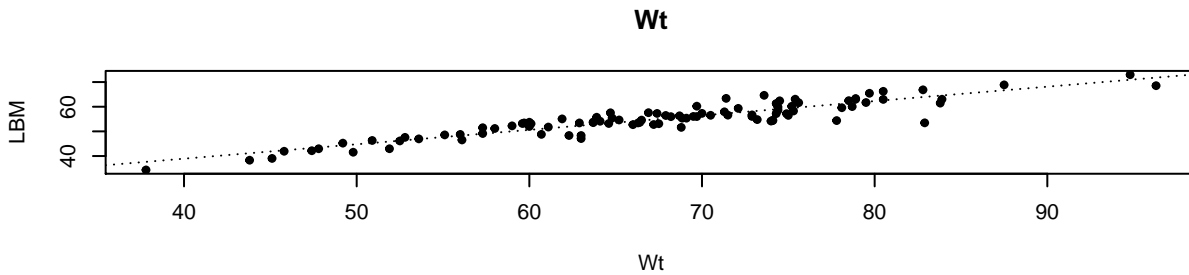
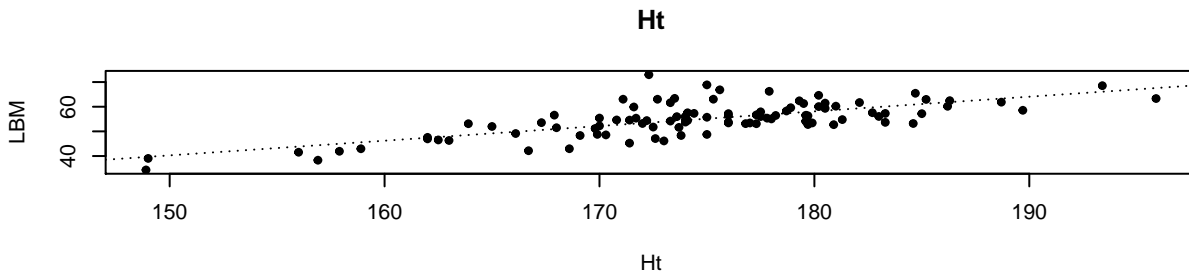


## Correlations

The simple correlation is a measure used to determine the strength and the direction of the relationship between two variables. In this example the independent variable is lbm and the other ones are the dependent variables.

The scatterplots show a strong lineal association between ht and lbm that is reflected for a correlation of 0.7082, the second scatterplots shows a strong relation between wt and lbm that is respalded for a correlation of 0.9207. Between the BMI and lbm there is a correlation of 0.7474 which represent a strong relation as well. Another imporant fact is the strong relation reflected for a correlation of 0.847 between the BMI and wt, that means that some of the information in the variable BMI are in wt and viceversa, furthermore the correlation between wt and ht is really hight (0.7087).

```
fit <- lm(LBM ~ 1+Ht+Wt+BMI+SSF, data=atletas) ##This model contain all of the variables
##It is used to determine the simple and partial correlations
```



,

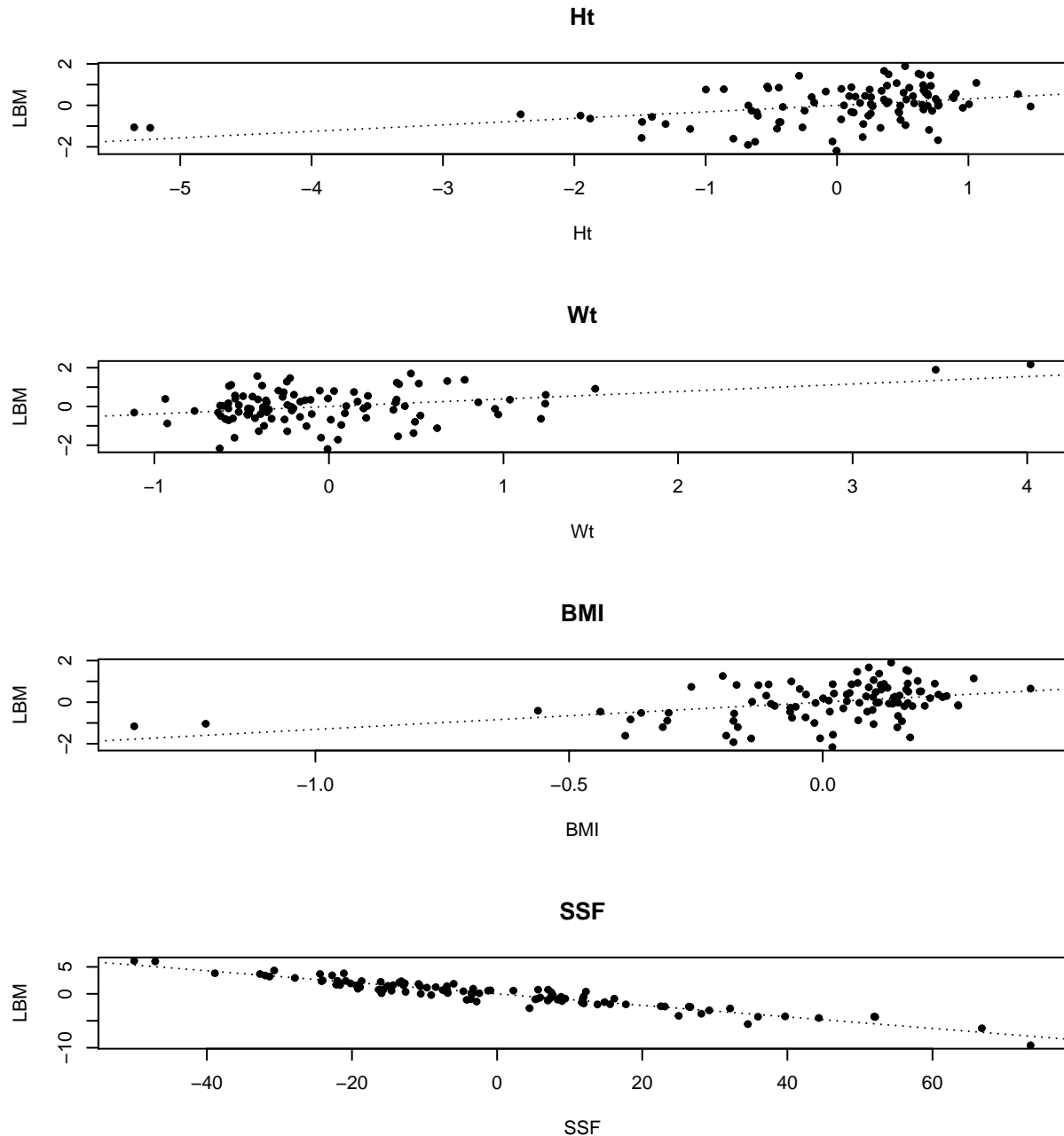
```
##          LBM          Ht          Wt          BMI          SSF
## LBM 1.0000000 0.7082934 0.9207976 0.7474915 0.4064912
## Ht  0.7082934 1.0000000 0.7087400 0.2316648 0.4065155
## Wt  0.9207976 0.7087400 1.0000000 0.8470335 0.7196649
## BMI 0.7474915 0.2316648 0.8470335 1.0000000 0.6784880
## SSF 0.4064912 0.4065155 0.7196649 0.6784880 1.0000000
```

## Partial correlation

The partial correlation for ht and lbm is shorter than the obtained in the plot of simple correlation, that means that part of the information of the ht variable over the response variable is also contained in the other

dependent variables . The same result appears when the simple correlation coefficient is compared 0.7082 with 0.377. This situations occurs in the same way with Wt having 0.9207 vs 0.338. Finally, rcc has a partial correlation coefficient of 0.195. This correlations describe the information that has every variable and there is not contained in aother one.

```
Correlaciones.parcial(fit,4,1,1,"")
```



```
##      [,1]      [,2]
## [1,] "Variables" "Respuesta"
## [2,] "Ht"       "0.377"
## [3,] "Wt"       "0.338"
## [4,] "BMI"      "0.382"
```

```
## [5,] "SSF"          "-0.949"
```

```
library(MASS)
library(zoo)
library(lmtest)
```

## Possible models

Models with one, two and 3 parameters are examined using the quality measures: SCRes, R2, R2 ajust and AIC. Maximum R2 and Shorter AIC

```
ajuste.normal(fit,1)
```

```
##      [,1]      [,2] [,3]      [,4]      [,5]      [,6]
## [1,] "Modelo"      ""      "SCRes" "R2"      "R2 Ajust" "AIC"
## [2,] "(Intercept)" "Ht"    "2363.9" "0.502" "0.497"    "606.1"
## [3,] "(Intercept)" "Wt"    "721.7" "0.848" "0.846"    "487.4"
## [4,] "(Intercept)" "BMI"   "2093.2" "0.559" "0.554"    "593.9"
## [5,] "(Intercept)" "SSF"   "3959.9" "0.165" "0.157"    "657.7"
```

```
ajuste.normal(fit,2)
```

```
##      [,1]      [,2] [,3]      [,4]      [,5]      [,6]      [,7]
## [1,] "Modelo"      ""      ""      "SCRes" "R2"      "R2 Ajust" "AIC"
## [2,] "(Intercept)" "Ht"    "Wt"    "692.1" "0.854" "0.851"    "485.2"
## [3,] "(Intercept)" "Ht"    "BMI"   "657.8" "0.861" "0.858"    "480.2"
## [4,] "(Intercept)" "Ht"    "SSF"   "2284"  "0.519" "0.509"    "604.6"
## [5,] "(Intercept)" "Wt"    "BMI"   "704"   "0.852" "0.849"    "486.9"
## [6,] "(Intercept)" "Wt"    "SSF"   "75.9"  "0.984" "0.984"    "264.2"
## [7,] "(Intercept)" "BMI"   "SSF"   "2004.1" "0.578" "0.569"    "591.6"
```

```
ajuste.normal(fit,3)
```

```
##      [,1]      [,2] [,3]      [,4]      [,5]      [,6]      [,7]      [,8]
## [1,] "Modelo"      ""      ""      ""      "SCRes" "R2"      "R2 Ajust" "AIC"
## [2,] "(Intercept)" "Ht"    "Wt"    "BMI"   "653.3" "0.862" "0.858"    "481.5"
## [3,] "(Intercept)" "Ht"    "Wt"    "SSF"   "75.9"  "0.984" "0.983"    "266.2"
## [4,] "(Intercept)" "Ht"    "BMI"   "SSF"   "73.2"  "0.985" "0.984"    "262.6"
## [5,] "(Intercept)" "Wt"    "BMI"   "SSF"   "75.6"  "0.984" "0.984"    "265.8"
```

```
ajuste.normal(fit,4)
```

```
##      [,1]      [,2] [,3]      [,4]      [,5]      [,6]      [,7]      [,8]
## [1,] "Modelo"      ""      ""      ""      ""      "SCRes" "R2"      "R2 Ajust"
## [2,] "(Intercept)" "Ht"    "Wt"    "BMI"   "SSF"   "64.9"  "0.986" "0.986"
##      [,9]
## [1,] "AIC"
## [2,] "252.5"
```

Over this results the best model will be that which contain all of the variables, however the model which contains just Wt and BMI has almost the same R2, furthermore, notice that the variable SSF seems with non homogenize variance, after running some models the best results were obtained applying log over there.

```
fit <- lm(LBM ~ 1+Wt+log(SSF), data=atletas)
summary(fit)
```

```
##
## Call:
```

```
## lm(formula = LBM ~ 1 + Wt + log(SSF), data = atletas)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -6.0308 -0.5960  0.0031  0.8787  2.4240
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 39.07183    1.51368   25.81  <2e-16 ***
## Wt          0.83149    0.01795   46.31  <2e-16 ***
## log(SSF)    -9.14915    0.49798  -18.37  <2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.289 on 97 degrees of freedom
## Multiple R-squared:  0.966, Adjusted R-squared:  0.9653
## F-statistic: 1380 on 2 and 97 DF,  p-value: < 2.2e-16
```

```
AIC(fit)
```

```
## [1] 339.4675
```

Now, see this model without intercept

```
fit2 <- lm(LBM ~ -1+Wt+log(SSF), data=atletas)
summary(fit2)
```

```
##
## Call:
## lm(formula = LBM ~ -1 + Wt + log(SSF), data = atletas)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -13.5921  -1.5619   0.5926   2.8043   6.8489
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## Wt          0.69927    0.04802  14.561  <2e-16 ***
## log(SSF)    1.71290    0.74312   2.305   0.0233 *
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 3.596 on 98 degrees of freedom
## Multiple R-squared:  0.9959, Adjusted R-squared:  0.9958
## F-statistic: 1.178e+04 on 2 and 98 DF,  p-value: < 2.2e-16
```

```
AIC(fit2)
```

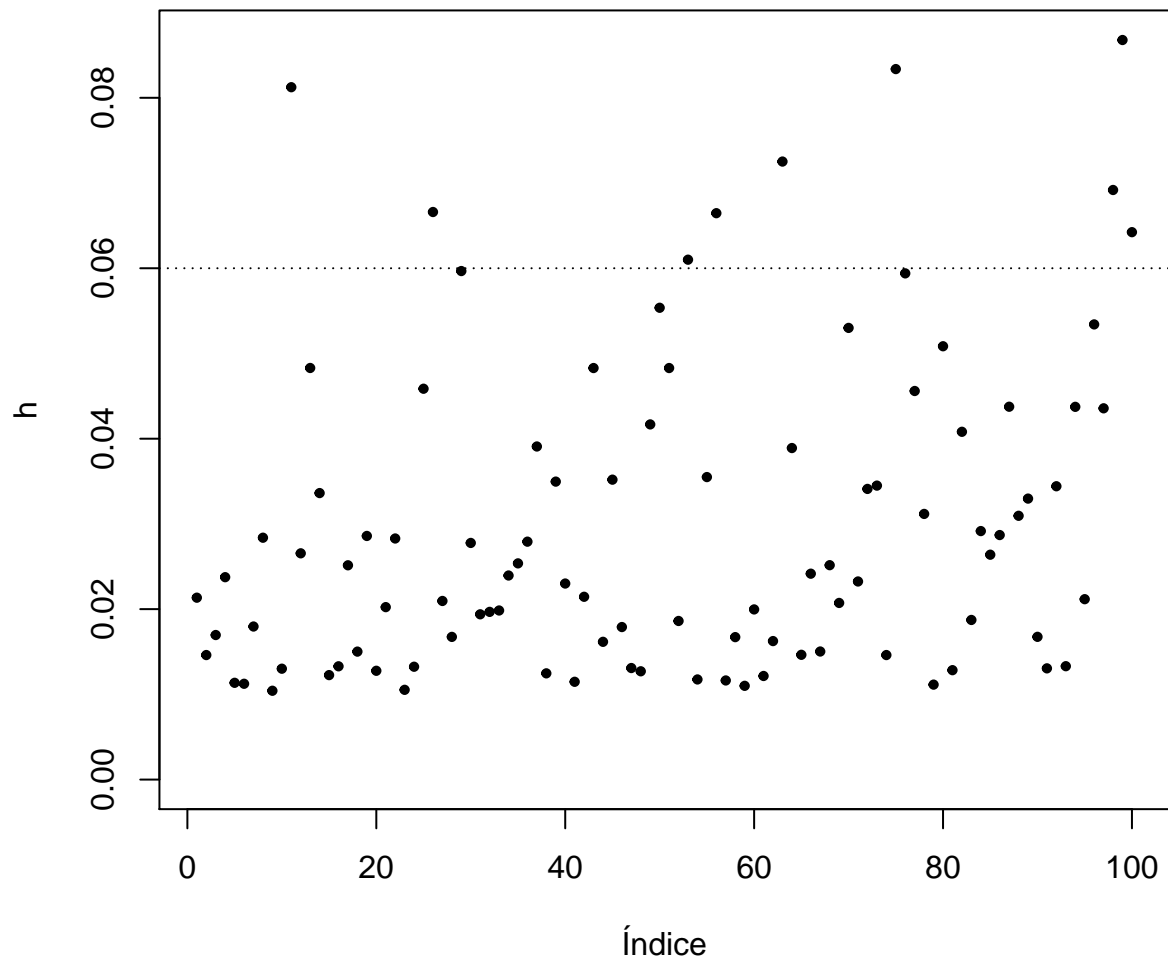
```
## [1] 543.7588
```

The R2 definition changes depends on the presence/absence of the intercept, for that reason the R2 ajust there are not comparable between the two final that differs in intercept. To decide about the best model the AIC help us, we can see that the model I has shorter AIC than the model II, furthermore all of these parameter are significant, that is the reason to choose this model over the first one.

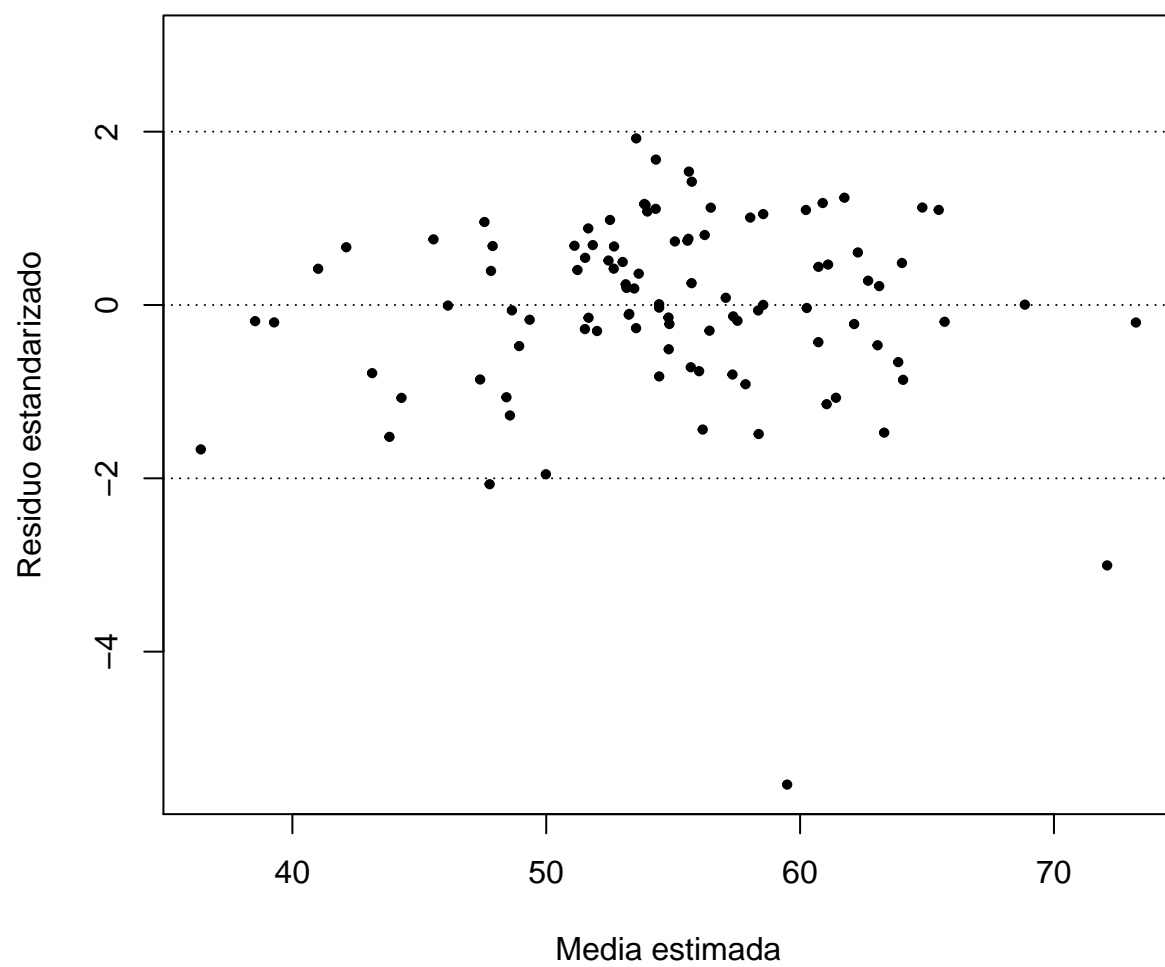
## Residuals examination

It is necessary to examine the residuals distribution, points of leverage and influence.

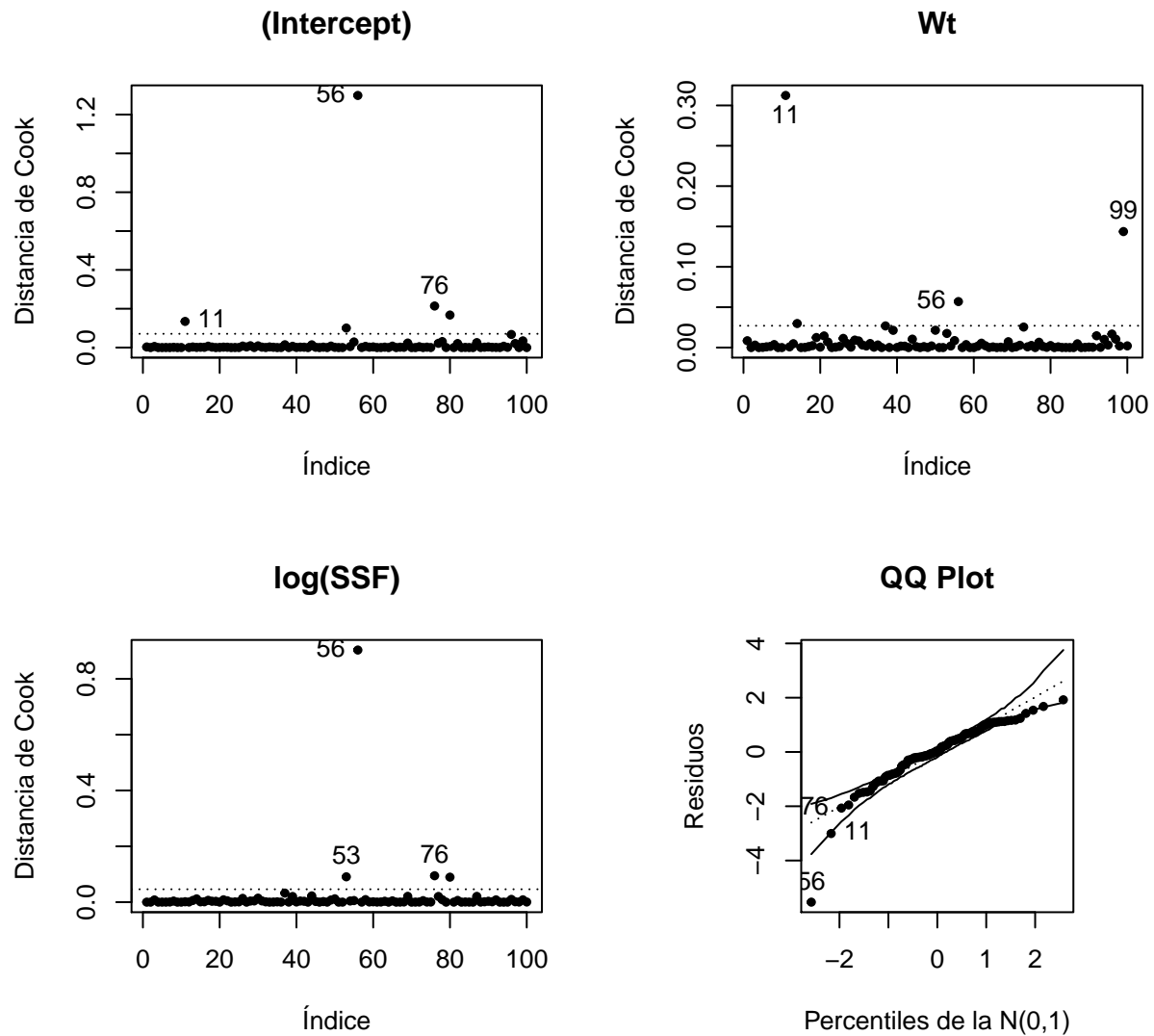
## Puntos de alto Leverage



### Observaciones extremas en la respuesta







```
## [1] 11 56 76
```

Well, the points 56,71 and 76 are the outliers, it is necessary talking with the expert to decide if it is necessary removing this points of the sample.

### Variance examination

```
##### Evaluando homogeneidad de la varianza #####
library(lmtest)
##### Test de Breusch-pagan #####
bptest(fit)

##
## studentized Breusch-Pagan test
##
## data: fit
## BP = 5.1186, df = 2, p-value = 0.07736
```

The Breusch-pagan's test to examine the homogeneity in the variance is not rejected with a significant level of 5%

```
##### Evaluando NO correlaci3n de los errores #####
##### Test de Durbin-Watson #####
```

```
dwtest(fit)
```

```
##
## Durbin-Watson test
##
## data: fit
## DW = 1.7363, p-value = 0.07647
## alternative hypothesis: true autocorrelation is greater than 0
```

The autocorrelation between residuals is rejected at significant level of 5%

## Removing outliers

For this example, we are going to suppose that the best option is deleting the outliers 11 and 56 of out sample. Let see how the model behaviour without this points.

```
atletas2<-atletas[-c(11,56),]
```

```
fit3<- lm(LBM ~ 1+Wt+log(SSF), data=atletas2)
summary(fit3)
```

```
##
## Call:
## lm(formula = LBM ~ 1 + Wt + log(SSF), data = atletas2)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -2.34120 -0.74054  0.03627  0.82504  2.20410
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  36.68876    1.28526   28.55  <2e-16 ***
## Wt           0.83796     0.01499   55.90  <2e-16 ***
## log(SSF)     -8.68087     0.41566  -20.88  <2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.056 on 95 degrees of freedom
## Multiple R-squared:  0.9768, Adjusted R-squared:  0.9763
## F-statistic: 1996 on 2 and 95 DF, p-value: < 2.2e-16
```

```
AIC(fit3)
```

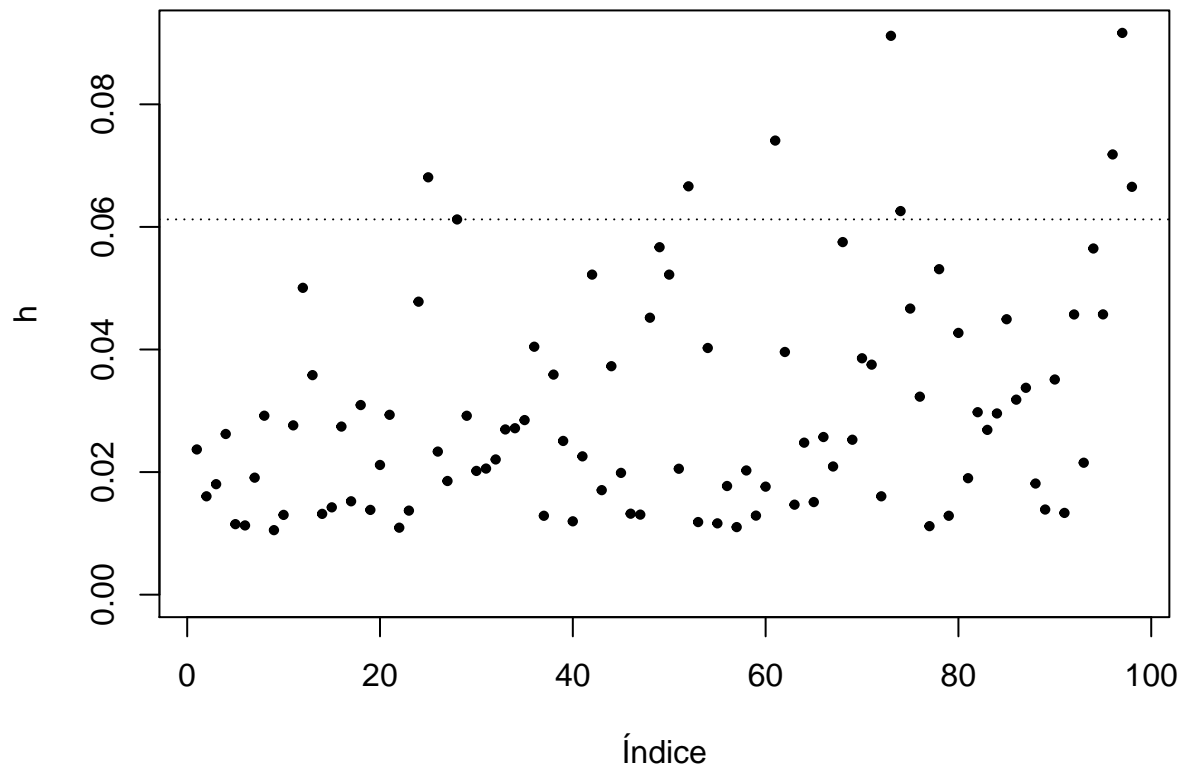
```
## [1] 293.6598
```

Well, the model seems good. Let's go to see the residuals examination

```
##### Leverage #####
```

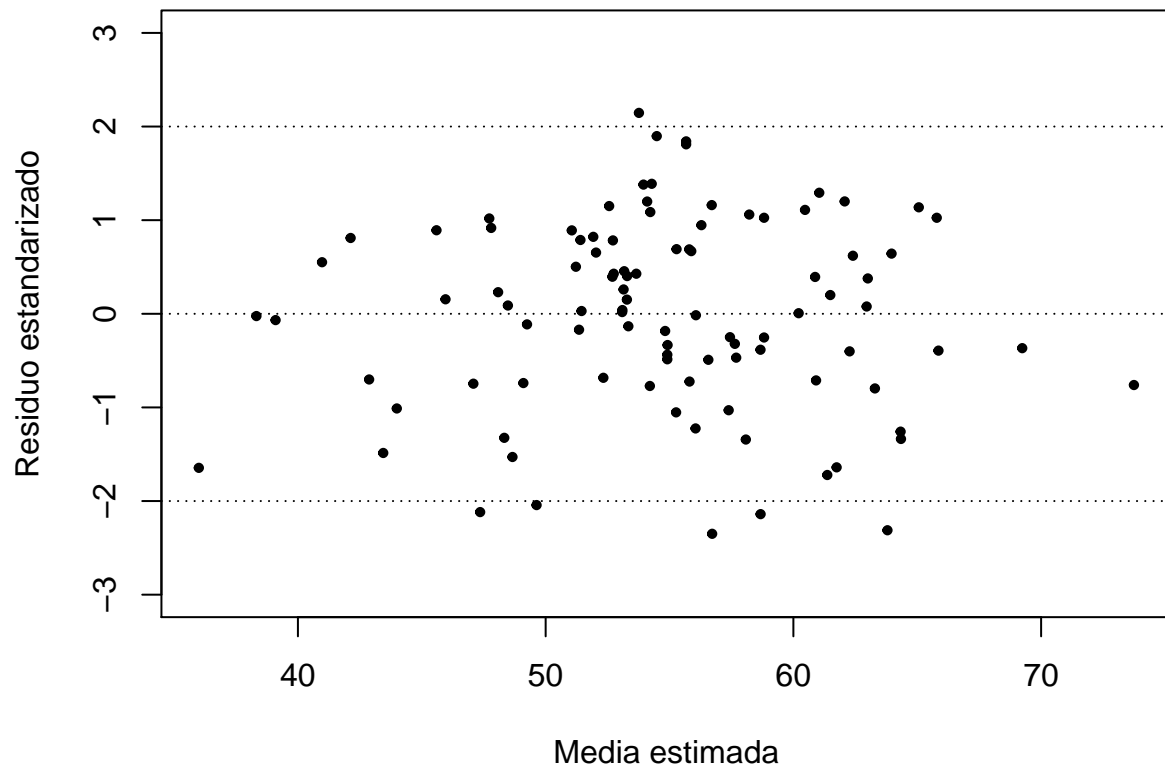
```
#par(mfrow=c(6,1))
Leverage <- Leverage.normal(fit3,3,"")
```

## Puntos de alto Leverage

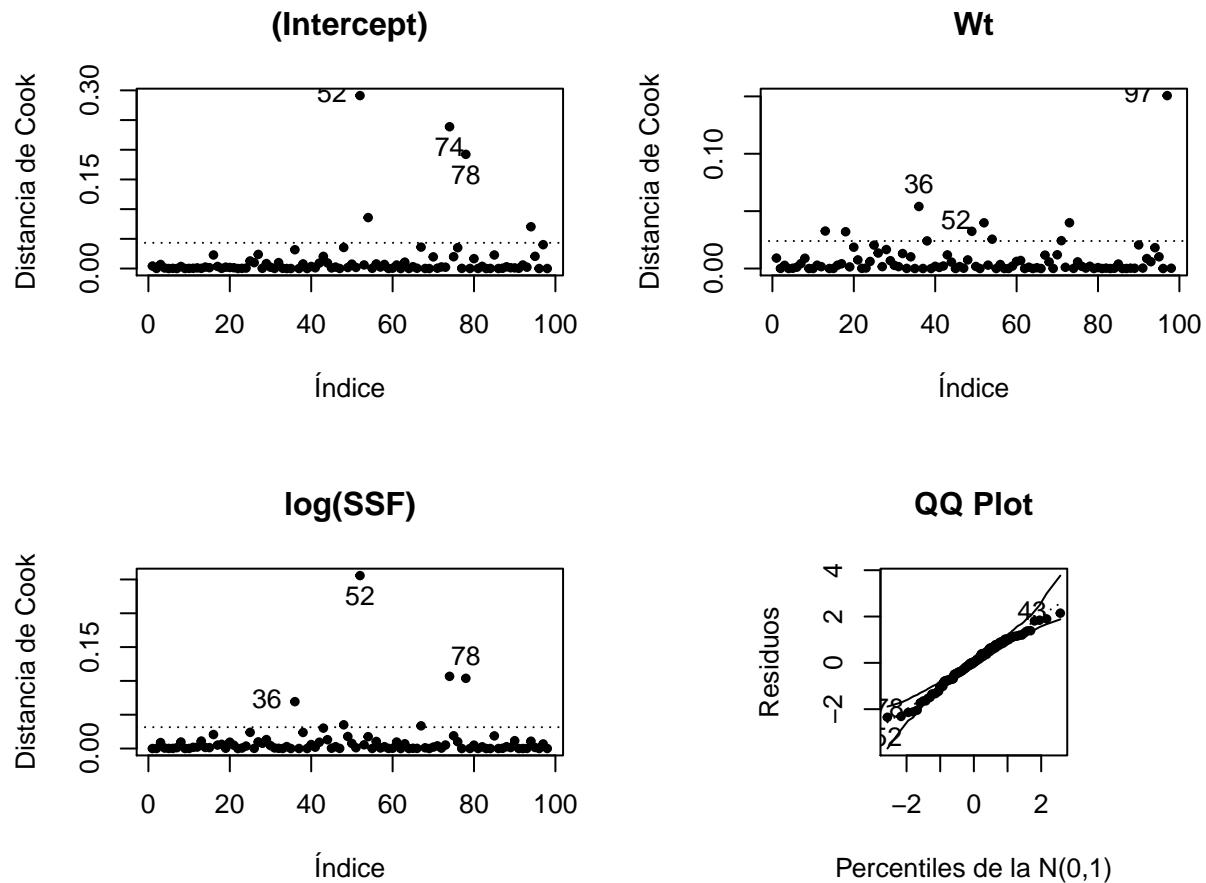


```
##### Residuos #####  
residuos <- Residuos.normal(fit3,3,"")
```

## Observaciones extremas en la respuesta



```
##### Influencia #####  
influence <- Influence.normal(fit3,2,2,3,"")  
  
##### QQ Plot y sus bandas de confianza #####  
qqplot.normal(fit3,500,0.01,3,"")
```



```
## [1] 43 52 78
##### Evaluando homogeneidad de la varianza #####
library(lmtest)
##### Test de Breusch-pagan #####
bptest(fit3)

##
## studentized Breusch-Pagan test
##
## data: fit3
## BP = 1.0013, df = 2, p-value = 0.6061
##### Evaluando NO correlaci3n de los errores #####
##### Test de Durbin-Watson #####
dwtest(fit3)

##
## Durbin-Watson test
##
## data: fit3
## DW = 1.9963, p-value = 0.4375
## alternative hypothesis: true autocorrelation is greater than 0
```

We can see that the model fits good the data and the residuals examination were good. Then our model is finished.

## Moldel interpretation

The final model is:  $LBM = B_0 + B_1Wt + B_2\log(SSF)$ , now, it is the time to interpretate its parameters. From the summary function we can identify just the coefficients.

```
summary(fit3)$coef
```

##	Estimate	Std. Error	t value	Pr(> t )
## (Intercept)	36.6887553	1.2852625	28.54573	2.118217e-48
## Wt	0.8379619	0.0149899	55.90176	1.725750e-74
## log(SSF)	-8.6808703	0.4156628	-20.88440	2.802111e-37

- $B_0$  for a person who has 0 in Wt and  $\log(SSF)$  the LBM should be in average 36.6887
- $B_1$  for each adicional unit of the Wt the LBM should increase in average 0.8379 units
- $B_2$  for each adicional unit of  $\log(SSF)$  the LBM should decrease in average -8.68087 units

## References

- Peter K. Dunn and Gordon K. Smyth (2018). GLMsData: Generalized Linear Model Data Sets. R package version 1.0.0. <https://CRAN.R-project.org/package=GLMsData>
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- Hadley Wickham and Jennifer Bryan (2019). readxl: Read Excel Files. R package version 1.3.1. <https://CRAN.R-project.org/package=readxl>
- Barret Schloerke, Jason Crowley, Di Cook, Francois Briatte, Moritz Marbach, Edwin Thoen, Amos Elberg and Joseph Larmarange (2018). GGally: Extension to 'ggplot2'. R package version 1.4.0. <https://CRAN.R-project.org/package=GGally>
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- Achim Zeileis, Torsten Hothorn (2002). Diagnostic Checking in Regression Relationships. R News 2(3), 7-10. URL <https://CRAN.R-project.org/doc/Rnews/>