

Merge Sort

Before understanding merge sort, first we should know about merging

Merging means merge two sorted array into a single array, so merging is done by need of extra array.

ex: ~~XXXXXXXXXX~~

a =

2	10	18	20	23
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b =

4	9	19	25
---	---	----	----

we will merge this two array.

let 'i' points on array a.

& j points on array b.

Let the array in which merge array would store be c[];

no. of elements in c be (m+n)

where m = elements in array a.

n = elements in array b.

we will use this concept:

if (a[i] > b[j]) (i < m & j < n)

c[k++] = a[i++];

else

c[k++] = b[j++];

If still elements in array remains then we can use

for (; i < m ; i++)

c[k++] = a[i++];

for (; j < n ; j++)

c[k++] = b[j++];

from above step we get array c as.

$c[] = [2, 4, 9, 10, 18, 19, 20, 23, 25];$

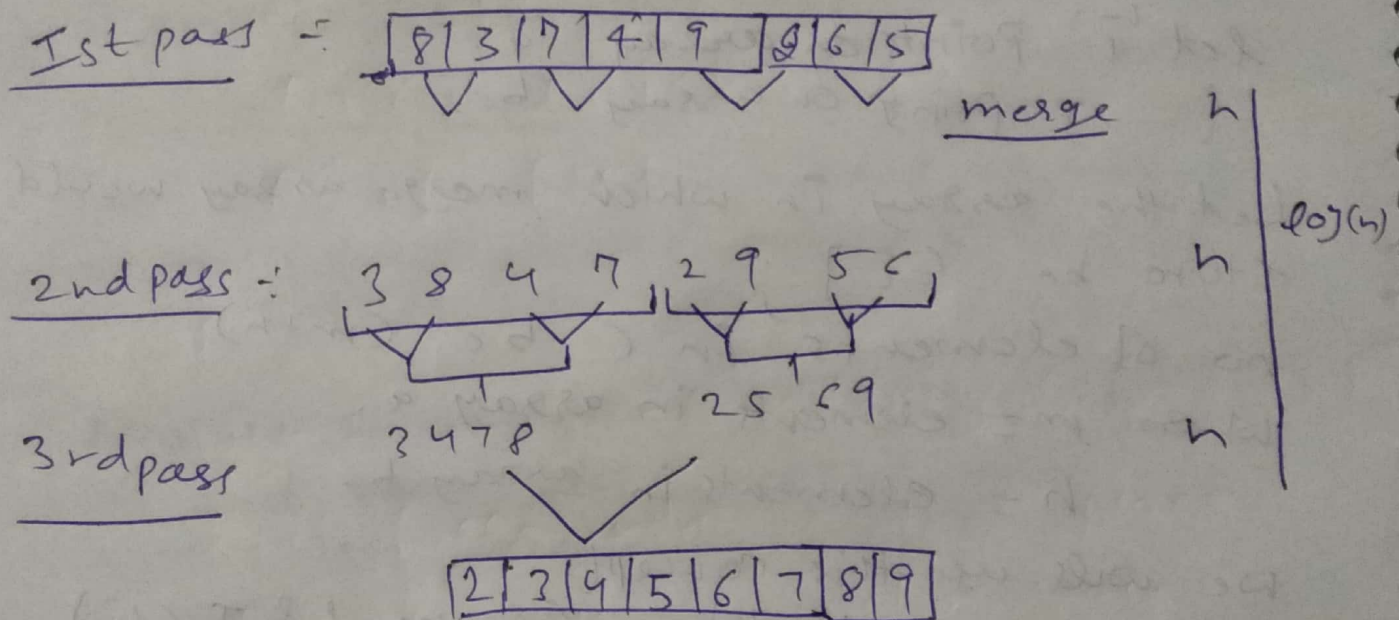
Now, Algorithm for merge sort :-

2-way merging + can be implemented iteratively or recursively

ex: A

8	3	7	4	9	2	6	5
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While implementing merge sort, assume each element of array is a separate list & apply merge sort.



$h = \text{no. of elements}$

So, we conclude time complexity of merge sort is $O(n \log n)$

/* iterative algorithm */

void mergesort (int A[], int n)

{
 for ($i = 0; i + p - 1 \leq n; i = i + p$)
 {
 $l = i;$

$h = i + p - 1;$

$mid = \frac{l+h}{2};$

$merge(A, l, mid, h);$

}

}

if ($p/2 < n$)

$merge(A, 0, \frac{p}{2}-1, n-1);$

}

/* Recursive */

void RmergeSort(int A[], int l, int h)

{

int mid;

if ($l < h$)

{

RmergeSort(A, l, mid);

RmergeSort(A, mid+1, h);

merge(A, l, mid, h);

}

}

/* Program for merging */

void merge(int A[], int l, int mid, int h)

{

int i, j, k;

$i = l; j = mid+1; k = l;$

while ($i \leq mid$ & $j \leq h$)

{

if ($A[i] \leq A[j]$)

$B[k++] = A[i++]$;

else

$B[k++] = A[j++]$

}

for (; i <= mid ; i++)

$B[k++] = A[i]$;

for (; j <= h ; j++)

$B[k++] = A[j]$

/ copy elements of B to A again */*

for (i = 1 ; i <= h ; i++)

$A[i] = B[i]$;

}

Now it's Time complexity $O(n \log 4)$

& it falls under out of place algorithm as an extra array is needed.