## Department of Mathematics MTH 372 (Statistical Inference) Assignment Sheet

Instructions

- Use statistical software R for your codes and only basic in-built functions are allowed.
- The due date is April 20, 2024 (11.59 p.m.). No late assignments will be accepted.
- Submit all of your work which include the report, codes, results and graphs.
- Provide detailed explanations in the reports to obtain full marks.
- Follow the given labelling method for your files (rollnumber-name).
- If not mentioned, then use  $\alpha = 0.05$ , assume the sample is a simple random sample and the sample comes from a normally distributed population.
- Plagiarism in the codes will lead to zero marks in the assignment.
- The data is given in attached (csv) file.
- 1. Find the distribution that best fits the data.

(3 marks)

- 2. List at least two estimators of the parameter(s) involved in the underlying distribution.
- (2 marks)
- 3. a. Classify the estimators in (1) into the unbiased, consistent or efficient estimators. b. Find the estimates from the data.
- (1 marks) (1 marks)

4. Find two parameters of the distribution using Method of Moments.

- (2 marks)
- 5. Find the Uniformly Minimum Variance Unbiased Estimator (UMVUE) of the parameter's and find its estimate from the data.

(2 marks)

- 6. Find the interval estimator of any one parameter of the population distribution with confidence  $\alpha = 0.01$ ; 0.05; 0.1. (3 marks)
- 7. Test the hypothesis that the mean  $\mu$  is equal to  $\mu_0$  (Take any value which is nearer to the mean of data). (2 mark)
- 8. Test the hypothesis that the variance  $\sigma^2$  is equal  $\sigma_0^2$  (Take any value which is nearer to the variance of data).
- 9. Perform goodness of fit to test the hypothesis that the distribution of the collected data is same as the distribution you fitted in Qustion 1.

(2 marks)