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5. DIVIDE AND CONQUER I

quickselect demo

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Quickselect demo

3-way partition array so that:

- Pivot element *p* is in place.
- Smaller elements in left subarray L.
- Equal elements in middle subarray M.
- Larger elements in right subarray R.

Recur in one subarray—the one containing the k^{th} smallest element.

select the $k = 8^{th}$ smallest

1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
65	28	59	33	21	56	22	95	50	12	90	53	28	77	39

 $k = 8^{th}$ smallest

2

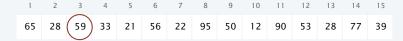
Quickselect demo

3-way partition array so that:

- Pivot element *p* is in place.
- Smaller elements in left subarray L.
- Equal elements in middle subarray $\it M$.
- Larger elements in right subarray R.

Recur in one subarray—the one containing the kth smallest element.

choose a pivot element at random and partition



 $k = 8^{th}$ smallest

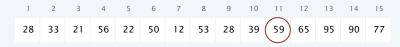
Quickselect demo

3-way partition array so that:

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- Equal elements in middle subarray M.
- Larger elements in right subarray R.

Recur in one subarray—the one containing the k^{th} smallest element.

partitioned array



 $k = 8^{th}$ smallest

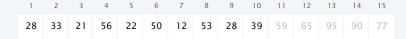
Quickselect demo

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- Larger elements in right subarray R.

Recur in one subarray—the one containing the k^{th} smallest element.

recursively select 8th smallest element in left subarray



 $k = 8^{th}$ smallest

5

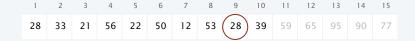
Quickselect demo

3-way partition array so that:

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- Larger elements in right subarray R.

Recur in one subarray—the one containing the k^{th} smallest element.

choose a pivot element at random and partition



 $k = 8^{th}$ smallest

6

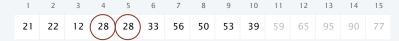
Quickselect demo

3-way partition array so that:

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- Smaller elements in left subarray L.
- Equal elements in middle subarray M.
- Larger elements in right subarray R.

Recur in one subarray—the one containing the k^{th} smallest element.

partitioned array



 $k = 8^{th}$ smallest

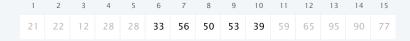
Quickselect demo

3-way partition array so that:

- Pivot element p is in place.
- Smaller elements in left subarray $\it L$.
- Equal elements in middle subarray M.
- Larger elements in right subarray R.

Recur in one subarray—the one containing the kth smallest element.

recursively select the 3rd smallest element in right subarray



 $k = 3^{rd}$ smallest

7

8

Quickselect demo

3-way partition array so that:

- Pivot element *p* is in place.
- Smaller elements in left subarray L.
- Equal elements in middle subarray M.
- Larger elements in right subarray R.

Recur in one subarray—the one containing the kth smallest element.

choose a pivot element at random and partition



 $k = 3^{rd}$ smallest

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Quickselect demo

3-way partition array so that:

- Pivot element *p* is in place.
- Smaller elements in left subarray L.
- Equal elements in middle subarray M.
- Larger elements in right subarray R.

Recur in one subarray—the one containing the kth smallest element.

stop: desired element is in middle subarray



Quickselect demo

3-way partition array so that:

- Pivot element *p* is in place.
- Smaller elements in left subarray L.
- Equal elements in middle subarray M.
- Larger elements in right subarray R.

Recur in one subarray—the one containing the k^{th} smallest element.

partitioned array

1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
21	22	12	28	28	33	39	50	53	56	59	65	95	90	77

 $k = 3^{rd}$ smallest

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