

Fall 2013

SCHEMA REFINEMENT AND NORMAL FORMS

[CH 19]

Database Design: The Story so Far

- Requirements Analysis
 - Data stored, operations, apps, ...
- Conceptual Database Design
 - Model high-level description of the data, constraints, ER model
- Logical Database Design
 - Choose a DBMS and design a database schema
- Schema Refinement
 - Normalize relations, avoid redundancy, anomalies ...
- Physical Database Design
 - Examine physical database structures like indices, restructure ...
- Security Design

Normalization

What is a good relational schema? How can we improve it?

- e.g.: Suppliers (name, item, desc, addr, price)

Redundancy Problems:

1. A supplier supplies two items: **Redundant Storage**
2. Change address of a supplier: **Update Anomaly**
3. Insert a supplier: **Insertion Anomaly**
 - What if the supplier does not supply any items (nulls?)
 - Record desc for an item that is not supplied by any supplier
4. Delete the only supplier tuple: **Delete Anomaly**
 - Use nulls?
 - Delete the last item tuple. Can't make name null. Why?

Alternative:

Dealing with Redundancy

- Identify “bad” schemas
 - functional dependencies
- Main refinement technique: decomposition
 - replacing larger relation with smaller ones
- Decomposition should be used judiciously:
 - Is there a reason to decompose a relation?
 - Normal forms: guarantees against (some) redundancy
 - Does decomposition cause any problems?
 - Lossless join
 - Dependency preservation
 - Performance (must join decomposed relations)

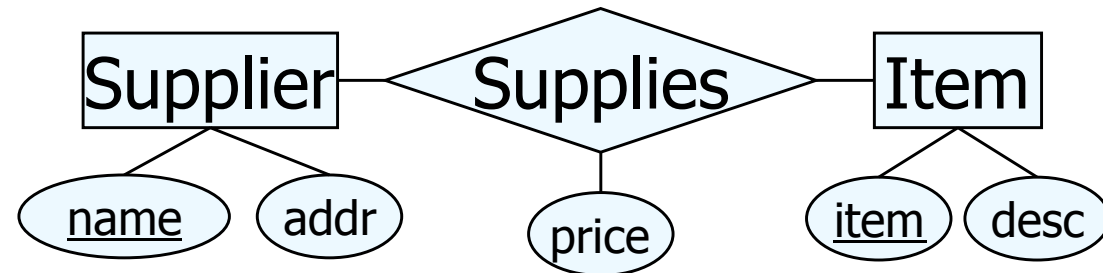
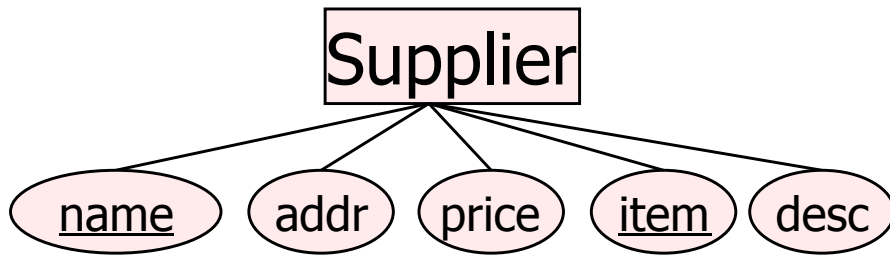
Functional Dependencies (FDs)

- A form of IC
- D: $X \rightarrow Y$ X and Y subsets of relation R 's attributes
 $t1 \in r, t2 \in r, \Pi_X(t1) = \Pi_X(t2) \Rightarrow \Pi_Y(t1) = \Pi_Y(t2)$
- An FD is a statement about all allowable relations.
 - Based only on application semantics, can't deduce from instances
 - Can simply check if an instance violates FD (and other ICs)
- Consider, $(X,Y) \rightarrow Z$. Does this imply (X,Y) is a key?

X	Y	Z	K
1	1	11	A
1	2	12	A
2	2	22	A
2	2	22	B

Primary Key IC is a special case of FD

Example: Constraints on Entity Set



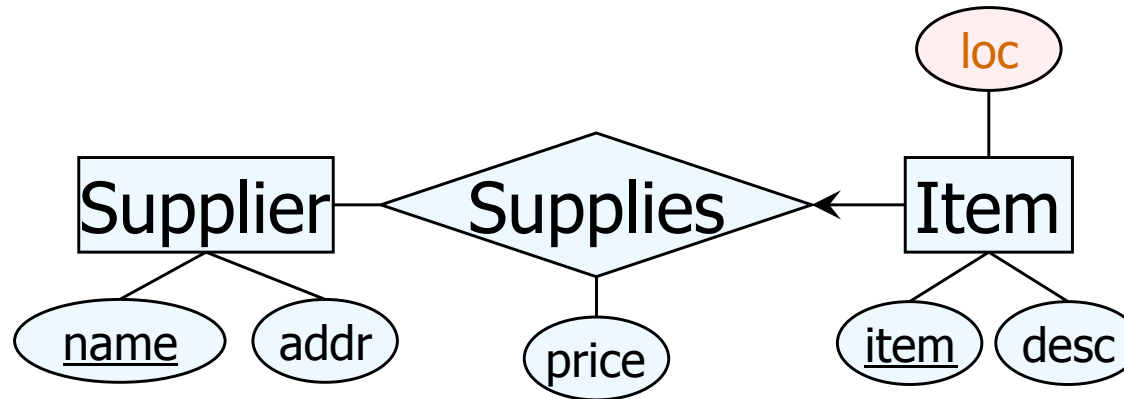
- $S(\underline{\text{name}}, \underline{\text{item}}, \text{desc}, \text{addr}, \text{price})$
- FD: $\{n, i\} \rightarrow \{n, i, d, a, p\}$
- FD: $\{n\} \rightarrow \{a\}$
- FD: $\{i\} \rightarrow \{d\}$
- Decompose to: $\underline{\text{NA}}, \underline{\text{ID}}, \underline{\text{INP}}$

- $\text{Spl}(\underline{\text{name}}, \underline{\text{item}}, \text{price})$
 - FD: $\{n, i\} \rightarrow \{n, i, p\}$
- $\text{Sup}(\text{name}, \text{addr})$
 - FD: $\{n\} \rightarrow \{n, a\}$
- $\text{Item}(\underline{\text{item}}, \text{desc})$
 - FD: $\{i\} \rightarrow \{i, d\}$

ER design is subjective and can have many E + Rs
FDs: sanity checks + deeper understanding of schema

Same situation could happen with a relationship set

Refining an ER Diagram



- IS (item, name, desc, loc, price)
S (name, addr)
- A supplier keeps all items in the same location
FD: name \rightarrow loc
- Solution:

Inferring FD

- $\text{ename} \rightarrow \text{ejob}, \text{ejob} \rightarrow \text{esal}; \Rightarrow \text{ename} \rightarrow \text{esal}$
- Armstrong's Axioms (X, Y, Z are sets of attributes):
 - **Reflexivity**: If $Y \subseteq X$, then $X \rightarrow Y$
 - **Augmentation**: If $X \rightarrow Y$, then $XZ \rightarrow YZ$ for any Z
 - **Transitivity**: If $X \rightarrow Y$ and $Y \rightarrow Z$, then $X \rightarrow Z$
- Additional rules (derivable):
 - **Union**: If $X \rightarrow Y$ and $X \rightarrow Z$, then $X \rightarrow YZ$
 - **Decomposition**: If $X \rightarrow YZ$, then $X \rightarrow Y$ and $X \rightarrow Z$
- Set of all FD = closure of F , denoted as F^+
- AA sound: only generates FD in F^+
- AA complete: repeated application generates all FD in F^+

Decomposition

- Replace a relation with two or more relations
- Problems with decomposition
 1. Some queries become more expensive. (more joins)
 2. **Lossless Join**: Can we reconstruct the original relation from instances of the decomposed relations?
 3. **Dependency Preservation**: Checking some dependencies may require joining the instances of the decomposed relations.

Lossless Join Decompositions

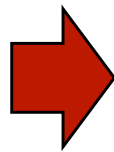
- Relation R, FDs F: Decomposed to X, Y

- Lossless-Join decomposition if:

$$\Pi_X(r) \bowtie \Pi_Y(r) = r \quad \text{for every instance } r \text{ of } R$$

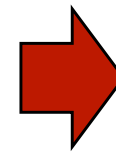
- Note, $r \subseteq \Pi_X(r) \bowtie \Pi_Y(r)$ is always true, not vice versa, unless the join is lossless
- Can generalize to three more relations

A	B	C
1	2	3
4	5	6
7	2	8



A	B
1	2
4	5
7	2

B	C
2	3
5	6
2	8



A	B	C
1	2	3
4	5	6
7	2	8
1	2	8
7	2	3

Lossless Join ...

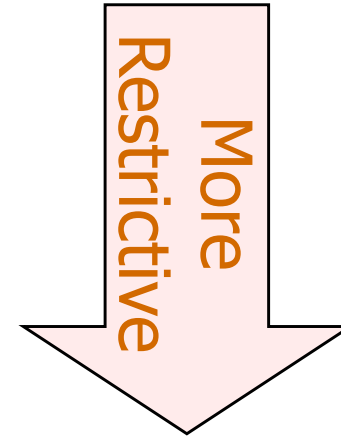
- Relation R , FDs F : Decomposed to X, Y
 - Test: lossless-join w.r.t. F if and only if the closure of F contains:
 - $X \cap Y \rightarrow X$, or
 - $X \cap Y \rightarrow Y$
 - i.e. attributes common to X and Y contain a key for either X or Y
 - Also, given FD: $X \rightarrow Y$ and $X \cap Y = \emptyset$, the decomposition into $R-X$ and XY is lossless
 - **X is a key in XY , and appears in both**

Dependency Preserving Decomposition

- $R(\text{sailor, boat, date}) \quad \{D \rightarrow S, D \rightarrow B\}$
 $\rightarrow X(\text{sailor, boat})$
 $Y(\text{boat, date}) \quad \{D \rightarrow B\}$
- To check $D \rightarrow S$ need to join R_1 and R_2 (expensive)
- Dependency preserving:
 - $R \rightarrow X, Y \quad F^+ = (F_x \cup F_y)^+$
 - Note: F not necessarily $= F_x \cup F_y$

Normal Forms

- Is any refinement is needed!
- Normal Forms: guarantees that certain kinds of problems won't occur
 - 1 NF : Atomic values
 - 2 NF : Historical
 - 3 NF : ...
 - BCNF : Boyce-Codd Normal Form



- Role of FDs in detecting redundancy:
 - Relation R with 3 attributes, ABC.
 - No ICs (FDs) hold \Rightarrow no redundancy.
 - $A \rightarrow B \Rightarrow$ 2 or more tuples with the same A value, redundantly have the same B value!

Boyce-Codd Normal Form (BCNF)

- Reln R with FDs F is in BCNF if, for all $X \rightarrow A$ in F^+
 - $A \in X$ (trivial FD), or
 - X is a super key

i.e. all non-trivial FDs over R are key constraints.

- **No redundancy in R** (at least none that FDs detect)
- Most desirable normal form

- Consider a relation in BCNF and FD: $X \rightarrow A$, two tuples have the same X value
 - Can the A values be the same (i.e. redundant)?
 - **NO!** X is a key, $\Rightarrow y1 = y2$. Not a set!

X	Y	A
x	y1	a
x	y2	?

3NF

- Relation R with FDs F is in 3NF if, for all $X \rightarrow A$ in F^+
 - $A \in X$ or
 - X is a super key or
 - A is part of some key for R (prime attribute)
 - Minimality of a key (not superkey) is crucial!
- BCNF implies 3NF
- e.g.: Sailor (Sailor, Boat, Date, CreditCrd)
 - SBD \rightarrow SBDC, S \rightarrow C (not 3NF)
 - If C \rightarrow S, then CBD \rightarrow SBDC (i.e. CBD is also a key). Now in 3NF!
 - Note redundancy in (S, C); 3NF permits this
 - Compromise used when BCNF not achievable, or perf. Consideration
- Lossless-join, dependency-preserving decomposition of R into a collection of 3NF relations always possible.