

École polytechnique de Louvain

LMAPR2451 Atomistic and nanoscopic simulations

Study of FeS₂ and its optical properties

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This report aims to investigate the optical properties of FeS_2 . To do so, *ab initio* computations are performed on a 6-atoms orthorhombic unit cell. The convergence with respect to several structural parameters is also studied. The optical properties are then analyzed in the light of the obtained results. Finally, a comparison is made with the published research, and a discussion about the quality of the simulation is made.

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1 Introduction

1.1 Motivation

Pyrite (FeS_2) is an interesting semiconducting material. Indeed, it can be used in numerous domains, from mechanical applications, where it is appreciated for its toughness and abrasiveness, to optical applications, where it can be used as an high-energy light absorber [1]. As pyrite is very abundant, it can become a material of choice in the industry if correct and valuable uses of the latter could be elaborated. It is depicted on Figure 1a.





(b) Marcassite, the orthrhombic polymorph of pyrite

Figure 1: FeS_2 ores

One of the promising potential application of pyrite is its integration into solar panels. Indeed, pyrite thin films could be good alternatives to the conventional silicon based solar cells, since the latter are more economically and ecologically costly [2, 3]. However, the performances of the material must be similar to or better than materials already used for solar cells, in order to make it truly competitive.

The concept of solar cell dates all the way back to 1883 [4]. However, it is interesting to recall some of the main features of such a device. A solar cell consists of photoelectric components able to convert the energy of the (solar) light into electricity though the *photovoltaic effect*. More precisely, it is composed of a *pn*-junction diode, usually made of silicon. When the depletion region of the junction is hit by solar photons, an electron is delivered in the *n*-layer and a hole is delivered in the *p*-layer (Figure 2). By doing so on a large scale, the *pn*-junction is able to generate a voltage of about 0.5 V, if the *n*-doped layer is sufficiently thin (to make the photons reach the depletion region as easily as possible). A solar panel is composed of several solar cells in series, in order to add up the voltage generated by each cell. The best materials for solar cells-related applications are the materials showing:

- a semiconducting behavior
- a high optical absorption coefficient
- a high electrical conductivity
- an abundant presence in the Earth's crust.[5]

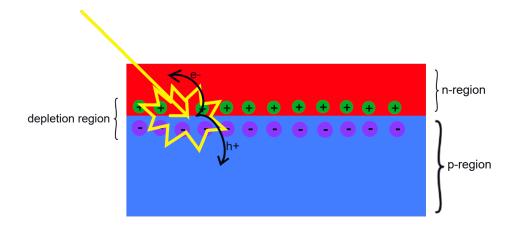


Figure 2: Simplified view of the photovoltaic effect at the pn-junction of a solar cell. The green and purple dots are the charges resulting from the recombination of charge carriers in the depletion region. When a photon hits an atom in the depletion region, an electron is released in the n-region and a hole is released in the p-region, creating a voltage when repeated multiple times.

Even if bulk pyrite shows a n-type behavior, pyrite thin-films show a p-type behavior. Only the deposition of a thin layer of n-type semiconductor on the pyrite film is needed to form a pn-heterojunction. Furthermore, the pyrite has a strong absorption coefficient. It thus allows to decrease the thickness of the pyrite film, which is helpful to improve the performances of the pn-junction, and hence, of the solar cell [6]. Furthermore, it is earth-abundant. Pyrite thus seems to be a material of choice for photovoltaic applications.

However, serious limitations prevent pyrite to be highly performant in this framework. Indeed, a very poor solar energy conversion efficiency is observed when assessing the performances of pyrite solar cells. That low efficiency is presumably due to a low photovoltage generation. The origin of that low photovoltage is highly debated among the scientific community. Several possible sources have been proposed over the years: detrimental S vacancies (although stoichimetric pyrite shows the same low photovoltage), detrimental impurities or even lattice defects [7]. No consensus has been found so far. But as pyrite could be a game-changer in the solar cell industry if its efficiency were improved, it is worth to look a little closer to the optical properties of the material.

In the following report, the properties of the FeS_2 in the Pnnm space group will be studied using the Abinit package [8]. As the unit cell of pyrite, which contains 12 atoms, is close to the computational limits of Abinit, the computations will be performed on a 6-atoms orthorhombic polymorph, depicted on Figure 1b. The results will be used as a starting point for the reflection concerning the actual pyrite. First, the unit cell and its structural parameters will be described, based on the Materials Project documentation¹. Then, the representation of the crystal in Abinit will be presented. Secondly, the pseudopotential and the approximation used in the first place will be discussed. Then, the convergence of the total energy per atom and the lattice scale parameters, with respect to the energy cut-off (ecut) and the number of k-points (ngkpt) will be studied. After that, Abinit computations will be performed using the converged values and the optical properties will be studied. To conclude, the obtained results will be compared with the published research.

¹https://materialsproject.org/materials/mp-1522/

1.2 FeS_2 : Overview and Abinit representation

The orthorhombic FeS_2 primitive cell contains 2 Fe atoms and 4 S atoms (Figure 3). The space group is Pnnm[58] in the Hermann-Mauguin notation.

Furthermore, it is a semiconductor. The energy of the indirect bandgap is about 0.978 eV[9]. Finally, the primitive cell will be represented as follow in Abinit input files:

```
acell
        3.390 4.438 5.411 Angstr
                                 # the lattice vectors scaling
                                   there are two types of atoms in the
ntypat
                                       primitive cell: Fe and S
znucl
        26 16
                                  # Fe has 26 electrons and S has 16
natom
        6
                                  # there are 6 atoms in the primitive cell
        1 1 2 2 2 2
                                  # 2 Fe atoms and 4 S atoms
typat
xred
               0
                      0
                                  # position of the first Fe atom in reduced coordinates
        0.5
               0.5
                      0.5
                                  # position of the second Fe atom
               0.206 0.3753
                                  # position of the first S atom
               0.794
                      0.6247
                                  # position of the second S atom
        0.5
               0.294
                      0.8753
                                  # position of the third S atom
        0.5
               0.706
                      0.1247
                                  # position of the fourth S atom
```

The data also comes from the Materials Project [9].

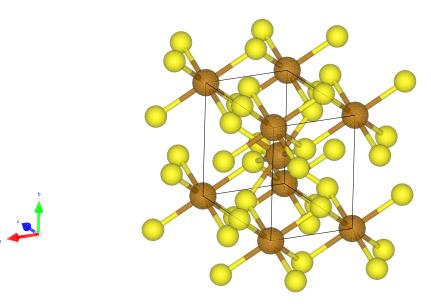


Figure 3: Primitive cell of orthorhombic FeS₂. Materials Project (mp-1522), Vesta

2 Convergence studies and pseudopotentials

In DFT computations, convergence studies are very important. They are meant to ensure that the chosen input parameters, like the cut-off energy (\mathtt{ecut}) or the number of k-points in the cell (determined by the sampling of the Brillouin zone \mathtt{ngkpt}), allow accurate results while limiting the computational time as much. To perform such an analysis, the same computations are repeated using datasets with various values of the parameter of interest, with an increasing accuracy of the environment. The evolution of some calculated variables, like the total energy of the unit cell (\mathtt{etotal}), indicates when the parameters of interest guarantee a sufficiently accurate simulation.

In the following subsections, the convergence of the total energy per atom and of the lattice scale parameters will be studied with respect to ecut and ngkpt.

2.1 Additional parameters

To begin, we will use the Local Density Approximation (LDA) functional. The pseudopotentials that will be used are retrieved from the PseudoDojo [10]. Two pseudopotentials are used: the NC SR (ONCVPSP v0.4.1) LDA standard pseudopotential relative to Fe, and the same one but relative to S (both in psp8 format). The pseudopotentials respectively consider 16 electrons $(3s^23p^64s^23d^6)$ for Fe) and 6 electrons $(3s^23p^4)$ for S) so that the unit cell contains 56 electrons.

It is also important to properly define the parameters ruling the SCF procedure. The most important one is nstep, defining the number of allowed SCF cycles to reach convergence. It is set to 100 in the first place. toldfe, the difference of total energy between two SCF cycles defining the moment when convergence is reached, is set to 1.0d-10 Ha. toldfe is chosen as the structural relaxation is not performed yet (in that case, toldff or tolrff is preferably used). Although it is not mandatory, the SCF procedure can be preconditioned by specifying the macroscopic dielectric constant (diemac). It is used to speed up the SCF procedure. A value of 24 is chosen, accordingly to the Materials Project [9].

Finally, the parameters of the k-points grid must be specified. kptopt is set to 1 in order to take advantage of the symmetry of the unit cell. By setting prtkpt to 1, Abinit will generate a set of k-point grids, that will be helpful to optimize further computations and convergence studies.

```
pseudos
         "pdj_nc_sr_041_lda_standard_psp8/Fe.psp8, pdj_nc_sr_041_lda_standard_psp8/S.psp8"
# parameters of the SCF procedure :
                  # maximal number of SCF cycles
nstep
         100
toldfe
         1.0d-10
                  # SCF procedure will stop when the difference of total energy
                        between two iterations will be lower than toldfe Hartree
diemac
         24.0
                  # preconditioning of the SCF procedure.
# parameters of the k-points grid :
kptopt
         1
prtkpt
```

2.2 Convergence of the total energy per atom as a function of the cut-off energy (ecut)

In the next computations, the default Monkhorst-Pack grids will be used. 4 k-points will be sampled along the longest lattice direction ([0 0 1]). To keep a constant density of k-points

along each axis, 3 k-points will be sampled along directions [1 0 0] and [0 1 0]. The input lattice parameters are thus :

ngkpt 3 3 4 nshiftk 1 shiftk 0.5 0.5 0.5

The study of the convergence of the simulation was performed by running Abinit with the input file 1522_3_ecutConv.abi (Appendix A). The total energy per atom of the unit cell is then plotted versus ecut (which spans from 10 [Ha] to 59 [Ha]) (Figure 4). Upper and lower bounds of ± 0.5 [mHa] are set around the last obtained value. It allows to determine the first ecut for which the convergence is reasonable. In the present case, ecut = 40 [Ha].

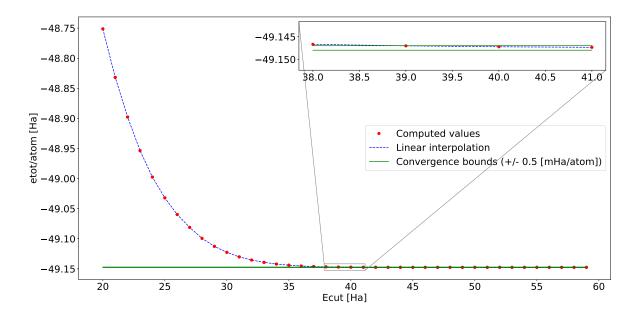


Figure 4: Total energy per atom as a function of the cut-off energy. The ecut range is truncated for visual reasons. Linear interpolations are shown as a guide for the eyes.

2.3 Convergence of the total energy per atom as a function of the number of k-points (ngkpt)

Alternatively, the same kind of study is performed with respect to the number of k-points in the Brillouin zone. Abinit is run with the input file 1522_4_nkpConv.abi (Appendix B). The energy per atom can be plotted versus the ngkpt parameter (Figure 5). However, as the biggest and the smallest lattice scale parameters differs from 60% in size, additional values of ngkpt keeping a similar k-sampling density along each axis are also tested.

The first converged ngkpt value is [3 3 3].

Concerning the convergence of the total energy per atom, the couple of values (ecut,ngkpt) that will be used in the further computations is thus (40 [Ha],[3 3 3]).

2.4 Convergence of acell as a function of the cut-off energy

The convergence of the length scales of the unit cell was performed using a dataset of ecut values between 20 [Ha] and 50 [Ha], $ngkpt = [3 \ 3]$ and ecutsm = 0.5 [Ha]. The input file

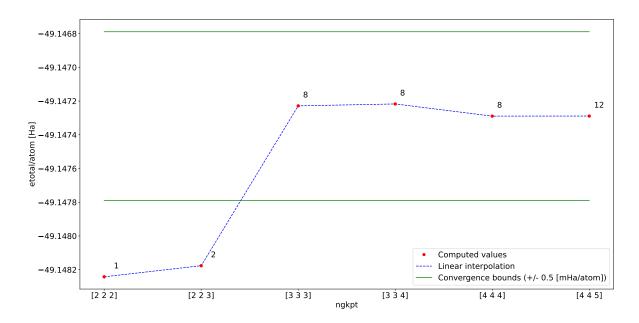


Figure 5: Total energy per atom as a function of the number of k-points in the k-points grid. The number near each dot represents the corresponding number of k-points.

used is 1522_6_acellEcutConv.abi (Appendix C). The results are displayed on Figure 6. The first converged value is 30 [Ha].

2.5 Convergence of acell as a function of the number of k-points

The convergence of the length scales of the unit cell was analyzed with ecut = 40 [Ha] and ecutsm = 0.5 [Ha]. Additional values of ngkpt accounting for the conservation of a similar k-sampling density along the axis of the unit cell are also tested. The input file used is 1522_3_acellNgkptConv.abi (Appendix D). The results are displayed on Figure 7. It can be seen that [2 2 2] is already in the limits of 0.2% of the length. Therefore, the value [2 2 2] is considered as the first converged value.

2.6 Summary

	ecut [Ha]	ngkpt
Convergence of etotal/atom	40	[3 3 3]
Convergence of acell	30	[2 2 2]

Furthermore, the most accurate value for acell and xred, obtained with $ngkpt = [4 \ 4 \ 5]$ (nkpt = 12) and ecut = 40 [Ha], is

acell(1)	6.2645 Bohr
acell(2)	8.2011 Bohr
acell(3)	9.9992 Bohr

or

acell(1)	3.315 Angstroms
acel1(2)	4.3398 Angstroms
acel1(3)	5.2913 Angstroms

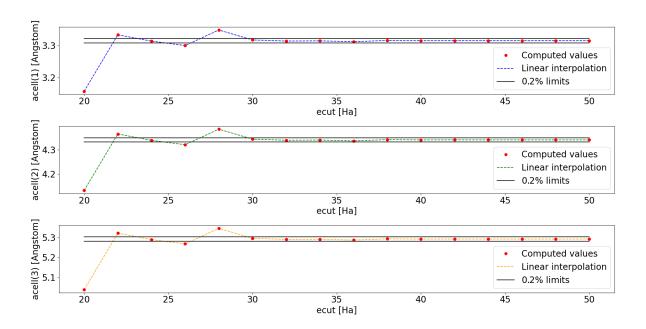


Figure 6: Convergence of the length scales acell as a function of the cut-off energy ecut.

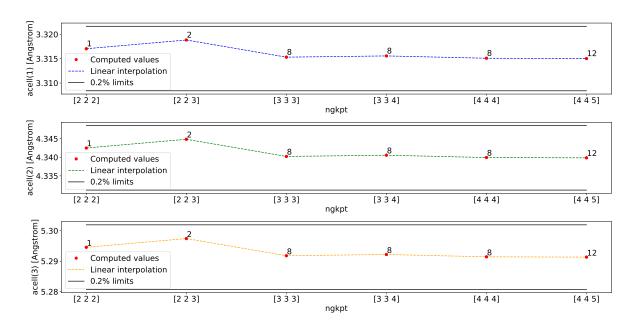


Figure 7: Convergence of the length scales acell as a function of the number of k-points in the k-points grid. The number near each dot represents the corresponding number of k-points.

and

	xred(1)	xred(2)	xred(3)
Fe #1	0	0	0
Fe #2	0.5	0.5	0.5
S #1	0	2.0809E-01	3.7374E-01
S #2	0	7.9191E-01	6.2626E-01
S #3	0.5	2.9191E-01	8.7374E-01
S #4	0.5	7.0809E-01	1.2626E-01

3 Optical properties

3.1 Electronic band structure

The band structure of the material was computed as follows. First, an optimal k-path is generated in the Brillouin zone of a simple orthorhombic lattice Figure 8 using the Abistruct module of Abipy (Appendix E).

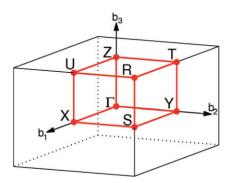


Figure 8: Brillouin zone for a simple orthorhombic lattice [11]

To obtain the band structure of the material, a SCF computation of the electronic density is run in the first place. Then, the band structure is computed using a non-SCF computation based on the previously generated electronic density file. The structural parameters of the unit cell are the ones provided by Absitruct. ecut and ngkpt are chosen accordingly to the previous convergence studies.

For the SCF computation, prtden is set to 1, in order to generate the DEN files.

For the band structure computation, iscf is set to -2 and getden is set to -1 to read the electronic densities from the previously generated DEN file. As the pseudopotentials used only consider 56 electrons in the whole unit cell, 27 electronic bands are completely filled. The 28th band is thus the valence band. To obtain a clear representation of the band gap of the material, 35 electronic bands are defined. kptopt is set to -15 accrodingly to the k-path provided by Abistruct. ndivsm is set to 30, and nbdbuf is set to -2 to place the last 2% bands of highest energy in a buffer, preventing Abinit to spent too much time trying to converge them.

The input file 1522_14_bs.abi is available in Appendix F.

The band structure is represented on Figure 9. The Fermi energy and the energy of the bandgap were also retrieved from the computed data. It is compared below with the data from the Materials Project [9]. The band structure provided by the Materials Project, which can be found in Appendix G, is compared with the computed one on Figure 10.

Besides a difference of 2.45 eV concerning the Fermi energies, the results of the computation seems consistent regarding the data of the Materials Project. That difference can be explained

	Computed	Materials Project
Fermi energy [eV]	10.13183	7.6763
Band gap energy [eV]	0.8674	0.8807

Table 1: Comparison between the computed results and the data provided by the Materials Project

by a difference in the value of the parameters ruling the computation.

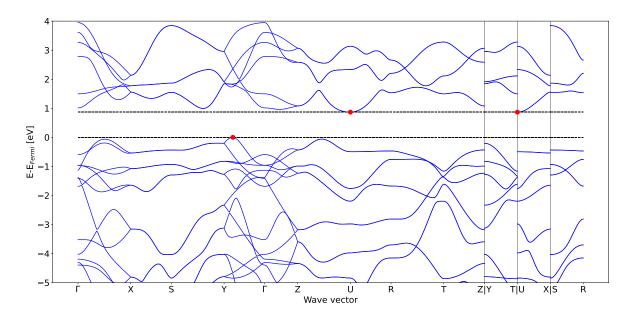


Figure 9: Band structure of FeS₂. The red dots represent the valence band minimums and the conduction band maximum.

3.2 Electronic density of states (DOS)

The electronic density of states was obtained by first running a SCF computation to generate a density file as for the computation of the bandstructure. In that case, **shiftk** was set to [0 0 0] as recommended in the Abinit documentation [12].

Then, the DOS was computed using the tetrahedron methode with prtdos = 2 and dosdeltae = 5.0d-5 Ha. ngkpt was set to [8 8 8] to ensure a good resolution in the DOS plot. The input file used is available in Appendix H. Several plots were obtained when trying to display the density of states of the material. Each of the plot presents a different level of smearing. The smearing is controlled by the k-sampling of the Brillouin zone and the step of energy that was chosen during the computation of the density of states. Indeed, the k-sampling and the energy step have both an influence on the resolution of the plot, as the DOS plot is obtained with the sum of Gaussian spreads localized on the eingenvalues composing each band, and for each k-point. Therefore, the smaller the energy step, the more detailed (and as it will be seen, the rougher) the pattern of density of states, as long as the k-sampling is sufficiently high (if the number of k-points or the energy step is too small, there will be undesired gaps in the DOS plot).

By default, Abipy smears the the plot of the DOS, no matter what step of energy was chosen fort the computation. It will thus be compared to the DOS pattern provided by the Materials

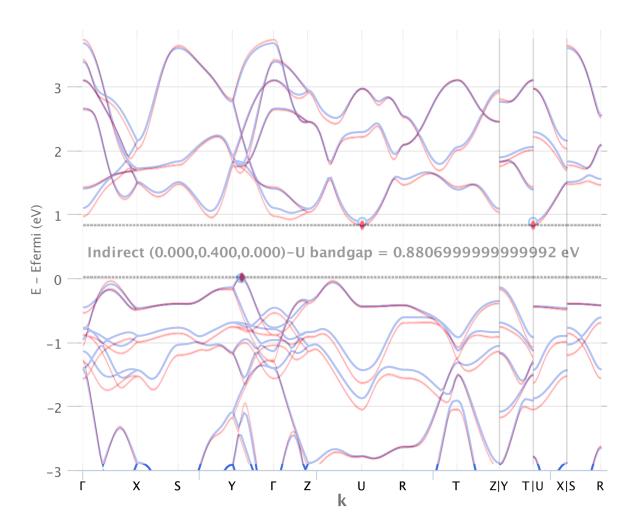
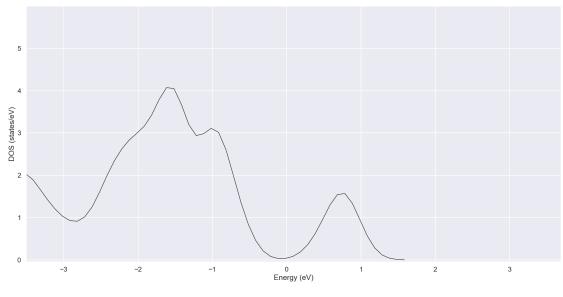


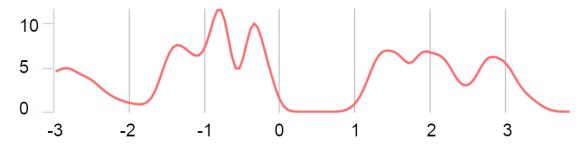
Figure 10: Blue : Band structure provided by the Materials Project. Red : Computed band structure.

Project, as the smearing is of the same order of magnitude there. The comparison is displayed on Figure 11. It can be seen that the two plots present the same features: a drop of the DOS at E=0 eV representing the bandgap, and similar peaks around the bandgap. However, substantial differences subsist:

- First, the plot displayed by Abipy (Figure 11a) isn't as wide as the one provided by the Materials Project (Figure 11b). This is due to the fact that only the first conduction band was computed with Abinit in the first case, while additional conduction bands were considered on the Materials Project.
- Secondly, the amplitude of the peaks isn't the same for the two graphs. Once again, it is presumably due to smearing reasons. The main drawback of these two sources (Abipy and the Materials Project) is that the smearing (or the energy step and the sampling of the Brillouin zone) is a black box. However, it can also be due to the method that was used to generate the data (but as it is not specified on the Materials Project, it's difficult to be sure).
- Lastly, it can be seen that the peaks on the plot provided by the Mateirals Project are higher in terms of DOS than on the plot calculated by Abinit and displayed by Abipy. That difference can be explained by a difference between the smearing level and the k-points lattice that has been chosen to run the computation. However, the most worthwhile comparison concerns the density of valence states.



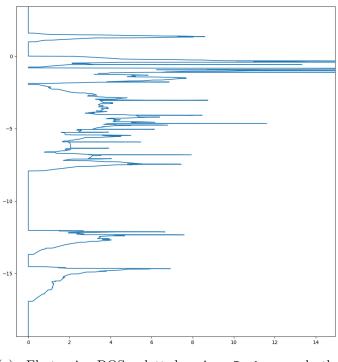
(a) Electronic DOS (displayed using Abipy)

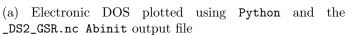


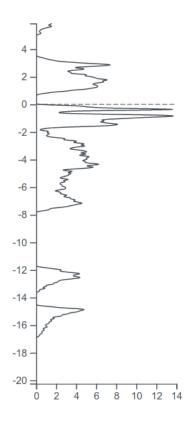
(b) Electronic DOS provided by the Materials Project (https://materialsproject.org/materials/mp-1522/)

Figure 11: Comparison of the most smeared DOS patterns

Then, the plot of the electronic DOS was displayed using a handmade Python script, using the _DS2_GSR.nc output file generated by Abinit (here DS2 is explained by the fact that the DOS was computed in the second dataset of the run, the first one being the SCF density computation). It was then compared with a plot of the DOS whose smearing seems to be significantly lower than for the two previous examples. The latter plot was obtained on the Topological Materials Database [13, 14, 15, 16, 17]. The two plots are compared on Figure 12. The goal here is to make the comparison between two less smeared plots.







(b) Electronic DOS provided by the Topological Materials Database

Figure 12: Comparison of less smeared DOS patterns

One can see here that the plots also show the same features. Some differences can however be mentioned :

- On the plot obtained using Abinit and Python (Figure 12a), the peaks above the bandgap are not as developed as on the plot provided by the Topological Materials Database (Figure 12b). This is due to the same reason as previously: only the first conduction band has been considered during the Abinit computation, while it is clearly not the case for the other plot.
- On the plot obtained with Python, peaks of high amplitude can be seen at several energies (for example just below the bandgap). After further investigation, the peaks span until a DOS of ~ 65 states/eV, implying that the amplitude of those peaks is probably a computational artefact. Such peaks are not visible on the other plot, because it has been smeared a little, demonstrating the utility of the smearing of the plot of the electronic DOS.

3.3 Phonon dispersion

The phonon dispersion of the material was computed as follows. First, a list of convenient q-points has to be generated. This is done by generating a list of k-points. To do so, we run a standard SCF computation. However in this case the SCF procedure is dummy. Indeed, nstep and nline are set to 1, preventing Abinit to run more than one iteration during the computation, as explained in [18]. The input file is available in Appendix I. Note that shiftk

was set to $[0\ 0\ 0]$ and not $[0.5\ 0.5\ 0.5]$ as in the previous computations. This is done to force Abinit to include the Γ point in the list to be generated.

Once the list of k-points is generated, we use it as a list of q-points for the further computations. The next step is to compute the phonon spectrum over the obtained q-points. A few datasets are used :

- The first one is a ground-state self-consistency computation that will be used for all the other datasets.
- The second dataset is used to compute the response function of the ground-state wavefunctions with respect to k ($\frac{d}{dk}$ calculation).
- The third one is used to compute the response function at Γ of an electric field perturbation.
- The other datasets are used to compute the phonon response at the other q-points. As only one q-point can be considered at a time, we need as many additional datasets as q-points.

After the run, several databases are generated, corresponding to the specified datasets. The input file is available in Appendix J. Those databases are merged and analyzed using the MRGDDB and ANADDB utilities. During the latter analysis, ANADDB computes different physical properties based on the databases containing the derivatives of the total energy (merged using MRGDDB). The properties to be computed are specified by a series of flags. For example:

- ifcflag is used to compute the interatomic force constants, which will be used to interpolate the phonon spectrum used in the band structure.
- dipdip is used to handle the dipole-dipole interactions separately from the interatomic forces, leading to more accurate results.
- eivec is used to generate an output file containing the frequencies for the different q-points, allowing to plot the phonon dispersion (referred to as the _B2EPS.freq file).
- prtdos allows to output a file containing the phonon density of states (see Figure 15).

The input file must also contain two specific lists of q-points. The first one is the q-path along which the phonon dipsersion will be computed. A previous list of k-points used to plot the electronic band structure was used. The second list of q-points contains actually one single q-point: Γ . Indeed, a discontinuity can be seen in the phonon band structure at this specific point. The frequencies computed at this point will be hardcoded in the _B2EPS.freq file to get a proper plot².

Then, using the generated _B2EPS.freq file containing the frequencies for all the q-points of the specified q-path, it is possible to produce a final file containing the band structure. It was plotted using Abipy (Figure 13) and was compared with the phonon dispersion plot provided by the Materials Project (Figure 14).

3.4 Phonon density of states

By setting prtdos = 2, it is possible to compute the phonon DOS using the tetrahedron method. The plot is obtained with Abipy, and is compared in Figure 15 with the phonon DOS plot provided on the Materials Project. It can be seen that the results are in good agreement, as the plots show the same features, and only differ by the smearing level of the plot.

²Note that the discontinuity at Γ is still there on Figure 13 and Figure 14. Indeed, no package was able to open the hacked .eps file properly.

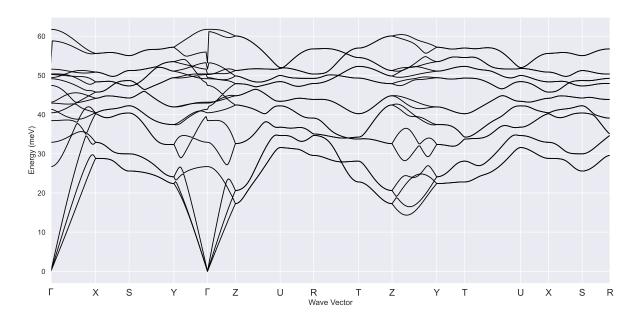


Figure 13: Computed phonon dispersion plotted with Abipy

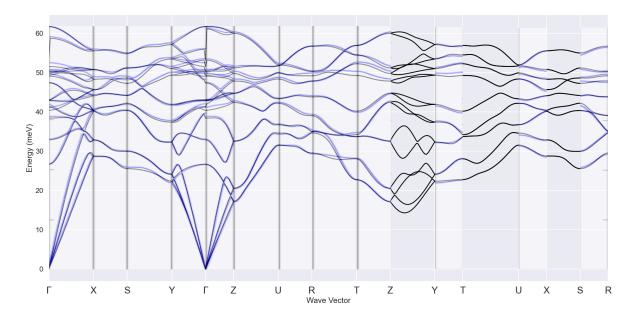
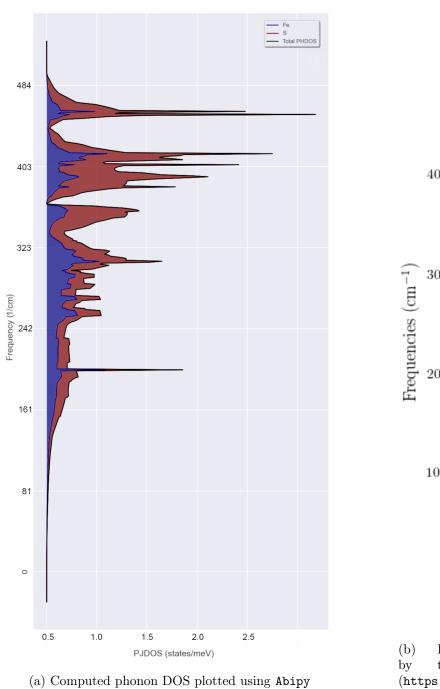
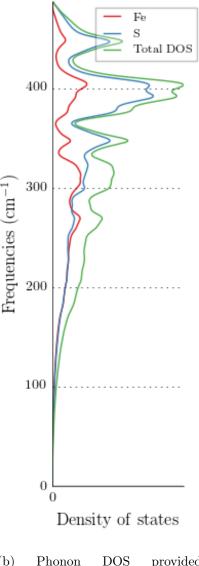


Figure 14: Comparison between the computed phonon dispersion (in black) and the phonon dispersion obtained on the Materials Project (in blue, https://materialsproject.org/materials/mp-1522/). The superposition of the plots is not complete as the plot provided by the Materials Project is truncated at some q-points.





(b) Phonon DOS provided by the Materials Project (https://materialsproject. org/materials/mp-1522/)

Figure 15: Comparison of the phonon DOS

3.5 Dielectric tensor

To compute the dielectric tensor of the material, a DFPT computation is performed using Abinit. In the input file (Appendix L) three datasets are created:

- The first one is used to generate the ground-state properties of the material, and the ground-state wavefunctions that will be used in the further computations.
- The second dataset is used to compute the derivatives of the wavefunctions with respect to k ($\frac{d}{dk}$ calculation).
- The third and last dataset is used to compute the response function under perturbations due to the electric field.

The obtained dielectric tensor is a diagonal 3×3 tensor:

$$\underline{\underline{\varepsilon}} = \begin{pmatrix} 20.2021 & 0 & 0\\ 0 & 20.9923 & 0\\ 0 & 0 & 20.8858 \end{pmatrix} \tag{1}$$

4 Results and macroscopic implications

4.1 Dielectric tensor

From Equation 1, the dielectric constant (relative permittivity) ε_r of FeS₂ can be computed :

$$\varepsilon_r = \frac{20.2021 + 20.9923 + 20.8858}{3} = 20.6934 \tag{2}$$

For comparison, the value provided by the Materials Project is $\varepsilon_r = 21.1311$.

The value of the electric susceptibility naturally follows Equation 2:

$$\chi = \varepsilon_r - 1 = 19.693 \tag{3}$$

4.2 Band structure and band gap

As seen in subsection 3.1, the band gap is indirect as the initial wavevector is (0,0.4,0) and the final wavevector is (0,0,0). The change of wavevector is represented on Figure 16. The computed energy of the band gap is 0.8674 eV (Table 1). In a semiconducting material, the electrons of the last valence band are able to jump in the first conduction band by interacting with an incident photon and absorbing its energy. The energy of the interacting photons must be equal to that one of the bandgap in order to be absorbed by the electrons. It is thus possible to know the frequency of the absorbed light:

$$E = h\nu = \hbar\omega \tag{4}$$

with h the Planck's constant and ν the frequency of the interacting photons. We get

$$\nu = \frac{0.8674 \times 1.60218 \times 10^{-19}}{6.62607 \times 10^{-34}} \text{ Hz}$$
 (5)

$$= 2.09737 \times 10^{14} \text{ Hz} \tag{6}$$

$$=209.737 \text{ THz}$$
 (7)

It corresponds to IR-B photons [19].

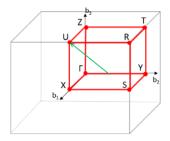


Figure 16: Brillouin zone for a simple orthorhombic lattice. The change of wavevector through the band gap is represented by the green arrow.

Although the material studied here is not candidate for future photovoltaic applications, its cubic polymorph, pyrite, is. The band gap of the latter material is also indirect [20]. It means that in order to generate a free electron-hole pair, one electron of the last valence band will have to interact with an incident photon and a phonon of the crystal lattice. This is why the phonon dipsersion and density of states can be interesting. Furthermore, it can be used to assess the thermal management of the material when exposed to light. In general, that kind of event (interaction with a photon and a phonon at the same time) is far more uncommon than for a direct bandgap, and the photons will penetrate deeper in the material before being absorbed. So in order to absorbed as much light as possible, the layer of material will have to be sufficiently thick [21].

4.3 Optics

When designing a photovoltaic cell, the material is wanted to have a maximum absorption and a minimum reflectivity, in order to mobilize as much incident light as possible. It implies that the refractive index must be as low as possible. Moreover, the photons have to be absorbed near the pn-junction to generate carriers. It is thus interesting to investigate the frequency dependent properties of the material, as for example the complex frequency dependent dielectric tensor $\tilde{\varepsilon}_r(\omega)$. Those quantities can then bu used to know the frequency dependent refractive index $n(\omega)$, and extinction coefficient $\kappa(\omega)$ as

$$\tilde{\varepsilon}_r(\omega) = \tilde{n}^2(\omega) \tag{8}$$

$$= (n(\omega) + j\kappa(\omega))^2 \tag{9}$$

This can be done using the Optic module of Abinit. However, as those kind of computations can be very time-consuming, it should be done with the material of interest, *pyrite* in this case. The absorption of the material in the visible range of light can be analyzed, and the effect of various modifications of the material can be studied (for example doping).

5 Conclusion

Marcassite is an orthorhombic polymorph of pyrite, of chemical formula FeS_2 . Several computations have been performed using Abinit to assess (part of) its optical properties: DFT calculations to get the electronic bandstructure and density of state, and response function calculations to get data about the phonons in the material (phonon dispersion and density of stats) and its dielectric tensor. The results have been compared with the Materials Project and good

agreement between the two sources has been showed in general. The similarities between marcassite and pyrite allows to expect some of properties of the latter crystal, and predict some of the properties to take into account to make efficient pyrite-based solar cells.

No need to say that this report could have been far more complete, even if some of the obtained results are satisfactory. Indeed, more convergence studies have to be done in order to ensure that the parameters ruling the different computations allow reliable results, even if they were chosen as wisely as possible during the writing of these lines. Furthermore, more optical properties of the crystal could be computed, using the <code>Optic</code> module. However, the convergence studies and the SCF calculations needed to run the <code>Optic</code> computations are very time-consuming.

This project allowed me to grasp all of the potential of the Abinit package and its working principle. Besides using the theoretical concepts seen during the classes, I could understand the specificities of intensive computing at a larger scale. I would like to thank Bogdan and Alexandre for their support during the project, their advices and the help they provided during the semester.

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A Convergence of the total energy per atom as a function of ecut

Name of the input file: 1522_3_ecutConv.abi

```
acell
         3.390 4.438 5.411 Angstr
ntypat
        26 16
znucl
{\tt natom}
         6
typat
        1 1 2 2 2 2
xred
         0
              0
                      0
         0.5 0.5
                      0.5
               0.206 0.3753
         0
         0
               0.794 0.6247
         0.5
               0.294 0.8753
         0.5
               0.706 0.1247
pseudos "Fe.psp8,S.psp8"
# parameters of the SCF procedure :
nstep
         100
                                 # maximal number of SCF cycles
toldfe
         1.0d-10
                                 # SCF procedure will stop when the difference of total
                                      energy between two iterations will be lower than
                                      toldfe Hartree
        24.0
                                 # preconditioning of the SCF procedure.
diemac
# parameters for generating the k-points grids :
kptopt
         3 3 4
ngkpt
nshiftk 1
shiftk
        0.5 0.5 0.5
ndtset
        50
ecut:
        10
ecut+
        1
```

B Convergence of the total energy per atom as a function of ngkpt

Name of the input file: 1522_4_nkpConv.abi

```
acell
         3.390 4.438 5.411 Angstr
ntypat
         26 16
znucl
{\tt natom}
         6
typat
        1 1 2 2 2 2
xred
         0
               0
                      0
         0.5
               0.5
                      0.5
               0.206 0.3753
         0
               0.794 0.6247
         0
         0.5
               0.294 0.8753
         0.5
               0.706 0.1247
                                 # the converged value for ecut
ecut
         40
pseudos "/Fe.psp8,S.psp8"
# parameters of the SCF procedure :
nstep
         100
                                  # maximal number of SCF cycles
                                 \# SCF procedure will stop when the difference of total
toldfe
         1.0d-10
                                       energy between two iterations will be lower than
                                 #
                                       toldfe Hartree
diemac
         24.0
                                 # preconditioning of the SCF procedure.
# parameters for generating the k-points grids :
getwfk
         -1
kptopt
        1
ndtset
        6
ngkpt1 2 2 2
ngkpt2 2 2 3
ngkpt3 3 3 3
ngkpt4 3 3 4
ngkpt5 4 4 4
        4 4 5
ngkpt6
nshiftk 1
shiftk 0.5 0.5 0.5
```

C Convergence of the lattice scale parameters as a function of ecut

Name of the input file: 1522_6_acellEcutConv.abi

```
acell
         3.390 4.438 5.411 Angstr
ntypat
         26 16
znucl
{\tt natom}
         6
typat
        1 1 2 2 2 2
xred
         0
               0
                      0
         0.5
               0.5
                      0.5
               0.206 0.3753
         0
         0
               0.794 0.6247
         0.5
               0.294 0.8753
         0.5 0.706 0.1247
ndtset
        16
        20
ecut:
ecut+
         2
pseudos "/Fe.psp8,S.psp8"
# parameters of the SCF procedure :
                                 # maximal number of SCF cycles
nstep
         100
toldff
         1.0d-6
                                 # SCF procedure will stop when the difference of total
                                      energy between two iterations will be lower than
                                      toldfe Hartree
                                 # preconditioning of the SCF procedure.
diemac
        24.0
ionmov
        2
optcell 1
dilatmx 1.05
ecutsm
        0.5
kptopt
        1
ngkpt
        3 3 3
nshiftk 1
shiftk 0.5 0.5 0.5
getwfk
        -1
```

D Convergence of the lattice scale parameters as a function of ngkpt

Name of the input file: 1522_3_acellNgkptConv.abi

```
acell
         3.390 4.438 5.411 Angstr
ntypat
znucl
         26 16
{\tt natom}
         6
typat
        1 1 2 2 2 2
xred
         0
               0
                       0
         0.5
               0.5
                       0.5
                0.206 0.3753
         0
         0
                0.794 0.6247
         0.5
               0.294 0.8753
         0.5
               0.706 0.1247
ndtset
         6
       2 2 2
ngkpt1
ngkpt2 2 2 3
        3 3 3
ngkpt3
ngkpt4
        3 3 4
ngkpt5
        4 4 4
        4 4 5
ngkpt6
ecut
         40
pseudos "/Fe.psp8,S.psp8"
# parameters of the SCF procedure :
nstep
         100
                                  # maximal number of SCF cycles
toldff
         1.0d-6
                                  # SCF procedure will stop when the difference of total
                                       energy between two iterations will be lower than
                                       toldfe Hartree
                                  \mbox{\tt\#} preconditioning of the SCF procedure.
diemac
         24.0
ionmov
         2
optcell 1
dilatmx 1.05
ecutsm
         0.5
nshiftk 1
shiftk
        0.5 0.5 0.5
getwfk -1
```

E Band structure : k-path generation using Absitruct (Abipy)

Command used: abistruct.py kpath input.abi

```
Input file: input.abi:
         3.315\ 4.3398\ 5.2913\ {\tt Angstr}\ \ \#\ {\tt the\ converged\ values}
 acell
 ntypat
 znucl
        26 16
 natom
          6
         1 1 2 2 2 2
 typat
                                     # the converged values
 xred
          0 0
                     0
          0.5 0.5
                     0.5
          0 0.20809 0.37374
          0 0.79191 0.62626
          0.5 0.29191 0.87374
          0.5 0.70809 0.12626
 pseudos "/Fe.psp8,S.psp8"
          100
 nstep
 toldfe 1.0d-10
 diemac 24.0
 kptopt 1
       3 3 3
 ngkpt
 nshiftk 1
 shiftk 0.5 0.5 0.5
 getwfk -1
```

```
Output:
# Abinit structure
          6
natom
ntypat
          2
           1 1 2 2 2 2
typat
znucl
          26 16
xred
                                                  # the converged values
          0 0
                      0
          0.5 0.5
                      0.5
             0.20809 0.37374
              0.79191 0.62626
           0.5 0.29191 0.87374
           0.5 0.70809 0.12626
acell
           1.0 1.0 1.0
rprim
          6.2644421031 0.0000000000 0.0000000000
           0.000000000 8.2010334357 0.0000000000
           # tolwfr 1e-20 iscf -2 # NSCF run
# To read previous DEN file, use: getden -1 or specify filename via getden_path "out_DEN"
# K-PATH IN REDUCED COORDINATES:
ndivsm
           10
kptopt
           -15
kptbounds
                                                  # $\Gamma$
           +0.00000 +0.00000 +0.00000
                                                  # X
          +0.50000 +0.00000 +0.00000
           +0.50000 +0.50000 +0.00000
                                                  # S
                                                  # Y
           +0.00000 +0.50000 +0.00000
           +0.00000 +0.00000 +0.00000
                                                  # $\Gamma$
                                                  # Z
           +0.00000 +0.00000 +0.50000
                                                  # U
          +0.50000 +0.00000 +0.50000
                                                  # R
           +0.50000 +0.50000 +0.50000
           +0.00000 +0.50000 +0.50000
                                                  # T
                                                  # Z
           +0.00000 +0.00000 +0.50000
           +0.00000 +0.50000 +0.00000
                                                  # Y
                                                  # T
          +0.00000 +0.50000 +0.50000
                                                  # U
           +0.50000 +0.00000 +0.50000
                                                  # X
           +0.50000 +0.00000 +0.00000
           +0.50000 +0.50000 +0.00000
                                                  # S
                                                  # R
           +0.50000 +0.50000 +0.50000
```

F Band structure computation

```
2
ndtset
natom
typas
           1 1 2 2 2 2
xred
           0.000000000 0.000000000 0.0000000000
           0.500000000 0.500000000 0.5000000000
           0.000000000 0.2080900000 0.3737400000
           0.000000000 0.7919100000 0.6262600000
           0.500000000 0.2919100000 0.8737400000
           0.5000000000 0.7080900000 0.1262600000
                                                    # converged value
ecut
# definition of the SCF procedure
nstep
           100
           24.0
diemac
# first dataset : SCF density computation
kptopt1
           1
nshiftk1
           1
shiftk1
           0.5 0.5 0.5
           3 3 3
                                                    # converged value
ngkpt1
prtden1
           1
toldfe1
           1.0d-10
# second dataset : band structure computation
iscf2
           -2
getden2
           -1
kptopt2
           -15
                                                    # number of k-segments
           35
                                                    # numbe rof bands
nband2
nbdbuf
           -2
ndivsm2
           30
kptbounds
           +0.00000 +0.00000 +0.00000
                                                    # $\Gamma$
                                                    # X
           +0.50000 +0.00000 +0.00000
           +0.50000 +0.50000 +0.00000
                                                    # S
           +0.00000 +0.50000 +0.00000
                                                    # Y
           +0.00000 +0.00000 +0.00000
                                                    # $\Gamma$
                                                    # Z
           +0.00000 +0.00000 +0.50000
                                                    # U
           +0.50000 +0.00000 +0.50000
           +0.50000 +0.50000 +0.50000
                                                    # R
           +0.00000 +0.50000 +0.50000
                                                    # T
                                                    # Z
           +0.00000 +0.00000 +0.50000
           +0.00000 +0.50000 +0.00000
                                                    # Y
                                                    # T
           +0.00000 +0.50000 +0.50000
                                                    # U
           +0.50000 +0.00000 +0.50000
           +0.50000 +0.00000 +0.00000
                                                    # X
           +0.50000 +0.50000 +0.00000
                                                    # S
           +0.50000 +0.50000 +0.50000
                                                    # R.
tolwfr2
           1.0d-12
enunit2
           1
                                                    # to get the energies in eV
```

${\bf G}\quad {\bf Band\ structure:\ Materials\ Project}$

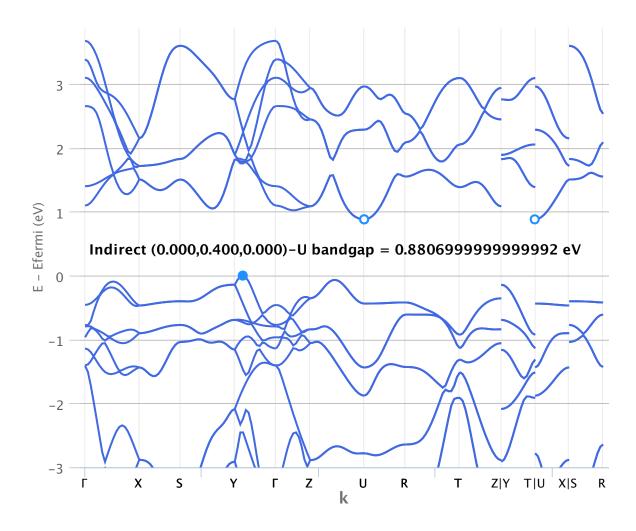


Figure 17: Band structure of orthorhombic FeS_2 provided by the Materials Project

H Electronic density of states

```
# computation of the electronic DOS
ndtset
# definition of the unit cell
           1.0 1.0 1.0
acell
rprim
            6.2644421031 0.0000000000 0.0000000000
            0.000000000 8.2010334357 0.0000000000
            0.000000000000000000000000000009.9991078432
# definition of the atoms types
            2
ntypat
znucl
            26 16
pseudos
          "Fe.psp8,S.psp8"
# definition of the atoms
natom
            1 1 2 2 2 2
typat
xred
            0.000000000 0.000000000 0.0000000000
            0.5000000000 \ 0.5000000000 \ 0.5000000000
            0.000000000 0.2080900000 0.3737400000
            0.000000000 0.7919100000 0.6262600000
            0.5000000000 \ 0.2919100000 \ 0.8737400000
            0.5000000000 \ 0.7080900000 \ 0.1262600000
ecut
            40.0
                                                     # converged value
# first dataset : SCF density computation
# definition of the SCF procedure
toldfe1 1.0d-10
            100
nstep
           24.0
diemac
# Brillouin zone sampling
kptopt1
           1
nshiftk1
shiftk1 0 0 0
                                                     # use of a non-shifted k-grid
            8 8 8
                                                     # higher than the converged value to
ngkpt1
                                                     # obtain a good resolution in the
                                                     # DOS plot
prtden1
            1
# second dataset : DOS computation
                                                     # computing the DOS using the
prtdos2
                                                     # wtetrahedron method
getden2
            -1
iscf2
            -3
tolwfr2
           1.0d-12
dosdeltae2 5.0d-5
```

I Phonons: Generation of a list of q-points

```
# Pnnm [58] FeS2 : computation of the q points
ngkpt
        3 3 3
nshiftk 1
shiftk
        0 0 0
# dummy SCF procedure
nstep
        1
nline
        1
        24.0
diemac
# common input variables
acell
        1.0 1.0 1.0
rprim
        6.2644421031 0.0000000000 0.0000000000
        0.000000000 8.2010334357 0.0000000000
        0.000000000 0.000000000 9.9991078432
ntypat
znucl
        26 16
pseudos
        "Fe.psp8,S.psp8"
natom
        1 1 2 2 2 2
typat
xred
        0.500000000 0.500000000 0.5000000000
        0.000000000 0.2080900000 0.3737400000
        0.000000000 0.7919100000 0.6262600000
        0.500000000 0.2919100000 0.8737400000
        0.500000000 0.7080900000 0.1262600000
        40.0
ecut
                                              # converged value
nband
        35
        1.0d-18
                                               # dummy variable as there is only one
tolvrs
                                               # step in the SCF procedure
```

J Phonons: Generation of the derivative databases

```
ndtset
            10
# dataset 1 : GS self-consistent computation
getwfk1 0
kptopt1 1
nqpt1
tolvrs1 1.0d-18
rfphon1 0
# Q vectors for all datasets
nqpt

      qpt2
      0.00000000E+00
      0.00000000E+00
      0.0000000E+00

      qpt3
      0.00000000E+00
      0.0000000E+00
      0.0000000E+00

      qpt4
      3.3333333E-01
      0.0000000E+00
      0.0000000E+00

      qpt5
      0.00000000E+00
      3.3333333E-01
      0.00000000E+00

            3.3333333E-01 3.3333333E-01 0.0000000E+00
qpt6
qpt7
            0.0000000E+00 0.0000000E+00 3.3333333E-01
            3.3333333E-01 0.00000000E+00 3.3333333E-01
qpt8
            0.0000000E+00 3.3333333E-01 3.3333333E-01
qpt9
qpt10
            3.3333333E-01 3.3333333E-01 3.3333333E-01
# dataset 2 :
                    response function calculation of d/dk wave function
iscf2
            -3
kptopt2 2
rfphon2 0
rfelfd2 2
tolwfr2 1.0d-22
# dataset 3: response function calculation at Q=O phonons and electric field perturbation
getddk3 2
kptopt3 2
rfelfd3 3
```

```
\# datasets 4-10 : finite-wave-vector phonon calculations (default for all datasets)
getwfk
        1
kptopt
        3
rfphon 1
rfatpol 16
rfdir
        1 1 1
tolvrs 1.0d-18
ntypat 2
znucl
        26 16
        "Fe.psp8,S.psp8"
pseudo
natom
        1 1 2 2 2 2
typat
         0.000000000 0.000000000 0.0000000000
xred
         0.5000000000 \ 0.5000000000 \ 0.5000000000
         0.0000000000 \ 0.2080900000 \ 0.3737400000
         0.000000000 0.7919100000 0.6262600000
         0.5000000000 0.2919100000 0.8737400000
         0.5000000000 \ 0.7080900000 \ 0.1262600000
         40.0
ecut
nband
         35
diemac
        24.0
ngkpt
        3 3 3
nshiftk 1
        0.5 0.5 0.5
shiftk
```

K Phonons : Computation of the band structure

```
ifcflag 1
ifcout 0
brav
          1
ngqpt 3 3 3
nqshift 1
q1shift 0.0 0.0 0.0
dipdip
eivec
          4
prtdos
          2
nph11
          401
\# the q-path is not written for visual reasons
 \label{eq:comma-Z-U-R-T-Z-Y-T-U-X-S-R} \\ \mbox{\# $\backslash$ Gamma-X-S-Y-\Gamma-Z-U-R-T-Z-Y-T-U-X-S-R$} 
# retrieved from the electronic bandstructure computation
nph21
qph2l
          1.0 1.0 1.0
ng2qpt
          3 3 3
```

L Dielectric tensor computation

```
ndtset
          3
kptopt
          1
          1.0d-19
tolvrs
rfelfd2
          2
rfdir
          1 1 1
nqpt2
          1
          0.0 0.0 0.0
qpt2
getwfk2
          -1
kptopt2
          2
iscf2
          -3
          1.0d-22
tolwfr2
rfphon3
          1
rfatpol3
         1 6
rfelfd3
          3
rfdir3
          1 1 1
nqpt3
          1
          0.0 0.0 0.0
qpt3
getwfk3
          -2
getddk3
          -1
kptopt3
          2
tolvrs3
          1.0d-12
          1.0 1.0 1.0
acell
rprim
          6.2644421031 0.0000000000 0.0000000000
          0.000000000 8.2010334357 0.0000000000
          0.000000000000000000000000000009.9991078432
          2
ntypat
          26 16
znucl
pseudos
          "Fe.psp8,S.psp8"
natom
          1 1 2 2 2 2
typat
xred
          0.000000000 0.000000000 0.0000000000
          0.500000000 0.500000000 0.5000000000
          0.000000000 0.2080900000 0.3737400000
          0.000000000 0.7919100000 0.6262600000
          0.5000000000 \ 0.2919100000 \ 0.8737400000
          0.5000000000 \ 0.7080900000 \ 0.1262600000
nband
          35
          40.0
ecut
ngkpt
          3 3 3
nshiftk
          1
          0.5 0.5 0.5
shiftk
          100
nstep
diemac
          24.0
```