

MATH 116: EXAM 01

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Answer the questions in the spaces provided on the question sheets and turn them in at the end of the class period. Unless otherwise stated, all supporting work is required. You may *not* use any calculators.

Name: _____

1. DEFINITIONS

1 (6 Points). *Let a, b be non-zero real numbers and m, n rational numbers. Fill in the blanks*

(i) $a^0 = \underline{\hspace{2cm}},$

(ii) $\left(\frac{a}{b}\right)^{-n} = \underline{\hspace{2cm}}.$

(iii) $a^m \cdot a^n = \underline{\hspace{2cm}}$

(iv) $\frac{a^m}{a^n} = \underline{\hspace{2cm}}$

(v) $(a \cdot b)^n = \underline{\hspace{2cm}}$

(vi) $\left(\frac{a}{b}\right)^n = \underline{\hspace{2cm}}$

2 (1 Points). *State the Quadratic Formula.*

3 (1 Points). *Fill in the blanks:*

To make $x^2 + bx$ a perfect square, add and subtract \square . This gives

$$x^2 + bx + \square - \square = (x + \square)^2 - \square.$$

4 (2 Points). (a) *State the Point-Slope form of a line passing through the point (x_0, y_0) with slope m .*

(b) *State the Slope-Intercept form of a line with slope m and y -intercept b .*

2. EXERCISES

5 (18 Points). *In the following problems, use the given information to find the equation of the line in slope-intercept form and then graph the lines.*

(a) *The line passing through the point $(-3, 3)$ and parallel to the line $3y - 9x = 27$.*

(b) *The line passing through the origin (that is, the point $(0, 0)$) and perpendicular to the line $3y - 9x = 27$.*

6 (18 Points). *Find the roots of the equation*

$$x^2 - 4x + 5 = 0.$$

7 (18 Points). (a) *Complete the square for the function $f(x) = 2x^2 - 12x + 12$.*

(b) *Solve $f(x) = 0$.*

(c) *Use the information from parts (a) and (b) to sketch a graph of $f(x)$. Label the y -intercept, any x -intercept(s), and the vertex.*

8 (18 Points). *Find all the roots, both real and complex, of the equation*

$$x^4 - 18x^2 + 81 = 0.$$

9 (18 Points). *Find the simultaneous solutions to the following system*

$$\begin{cases} y &= x^2 + 7x + 11, \\ y &= x + 2. \end{cases}$$