

**Table A1:** Language Sea: Persisting to Hard-Quit

Covariate	Hazard Ratio	95% CI
1 Seq error vs. No error	1.812	[ 1.626 , 2.019 ]
2 Seq errors vs. No error	1.907	[ 1.676 , 2.170 ]
3 Seq errors vs. No error	1.517	[ 1.279 , 1.798 ]
> 3 Seq errors vs. No error	1.956	[ 1.620 , 2.361 ]
Fast error vs. No error	1.937	[ 1.730 , 2.169 ]
Slow error vs. No error	1.183	[ 1.061 , 1.319 ]
During school vs. Outside school	3.231	[ 2.790 , 3.741 ]
High diff vs. Medium diff	1.216	[ 1.112 , 1.330 ]
High diff vs. Low diff	1.028	[ 0.927 , 1.140 ]
Higer grades vs. Lower grades	1.348	[ 1.250 , 1.453 ]
Girls vs. Boys	0.919	[ 0.853 , 0.991 ]

**Table A2:** Language Sea: Persisting to Soft-Quit

Covariate	Hazard Ratio	95% CI
1 Seq error vs. No error	2.962	[ 2.736 , 3.207 ]
2 Seq errors vs. No error	4.699	[ 4.318 , 5.115 ]
3 Seq errors vs. No error	10.221	[ 9.410 , 11.101 ]
> 3 Seq errors vs. No error	6.52	[ 5.888 , 7.220 ]
Fast error vs. No error	3.387	[ 3.160 , 3.631 ]
Slow error vs. No error	1.014	[ 0.941 , 1.092 ]
During school vs. Outside school	1.372	[ 1.283 , 1.467 ]
High diff vs. Medium diff	1.195	[ 1.127 , 1.266 ]
High diff vs. Low diff	1.123	[ 1.052 , 1.199 ]
Higer grades vs. Lower grades	1.288	[ 1.228 , 1.350 ]
Girls vs. Boys	0.98	[ 0.935 , 1.027 ]

**Table A3:** Math Garden: Persisting to Hard-Quit

Covariate	Hazard Ratio	95% CI
1 Seq error vs. No error	2.493	[ 2.345 , 2.649 ]
2 Seq errors vs. No error	2.699	[ 2.501 , 2.913 ]
3 Seq errors vs. No error	2.038	[ 1.829 , 2.271 ]
> 3 Seq errors vs. No error	1.989	[ 1.748 , 2.265 ]
Fast error vs. No error	2.064	[ 1.932 , 2.205 ]
Slow error vs. No error	1.013	[ 0.951 , 1.078 ]
During school vs. Outside school	2.584	[ 2.344 , 2.848 ]
High diff vs. Medium diff	1.032	[ 0.971 , 1.097 ]
High diff vs. Low diff	1.082	[ 1.019 , 1.149 ]
Higer grades vs. Lower grades	1.252	[ 1.197 , 1.309 ]
Girls vs. Boys	0.893	[ 0.854 , 0.934 ]

**Table A4:** Math Garden: Persisting to Soft-Quit

Covariate	Hazard Ratio	95% CI
1 Seq error vs. No error	4.666	[ 4.455 , 4.887 ]
2 Seq errors vs. No error	7.768	[ 7.386 , 8.171 ]
3 Seq errors vs. No error	13.341	[ 12.652 , 14.068 ]
> 3 Seq errors vs. No error	8.462	[ 7.923 , 9.039 ]
Fast error vs. No error	3.092	[ 2.969 , 3.220 ]
Slow error vs. No error	0.846	[ 0.811 , 0.882 ]
During school vs. Outside school	1.39	[ 1.321 , 1.462 ]
High diff vs. Medium diff	1.093	[ 1.049 , 1.138 ]
High diff vs. Low diff	1.215	[ 1.167 , 1.265 ]
Higer grades vs. Lower grades	1.324	[ 1.285 , 1.364 ]
Girls vs. Boys	1.021	[ 0.990 , 1.052 ]

## B Supplementary Material: 2-State Markov Model

**Table B1:** Main effects

	Training Data		Testing Data	
	HR	95% CI	HR	95% CI
1 vs. 0 Sequential Errors	7.36	[7.09 ; 7.65]	8.20	[7.89 ; 8.53]
2 vs. 0 Sequential Errors	22.93	[22.02 ; 23.87]	23.39	[22.44 ; 24.38]
3 vs. 0 Sequential Errors	17.61	[16.50 ; 18.79]	19.99	[18.71 ; 21.36]
>3 vs. 0 Sequential Errors	17.65	[16.26 ; 19.17]	17.92	[16.43 ; 19.54]
Fast vs. Slow Response Time	0.95	[0.94 ; 0.97]	0.93	[0.92 ; 0.94]
During vs. Outside School Hours	1.60	[1.56 ; 1.64]	1.61	[1.57 ; 1.65]
Grade 5-6 vs. Grade 7-8	1.13	[1.11 ; 1.15]	1.26	[1.23 ; 1.28]
Grade 3-4 vs. Grade 7-8	1.44	[1.42 ; 1.47]	1.55	[1.52 ; 1.58]
Easy vs. Medium Difficulty Level	1.05	[1.03 ; 1.07]	1.02	[1.00 ; 1.04]
Difficult vs. Medium Difficulty Level	1.08	[1.07 ; 1.10]	1.10	[1.08 ; 1.12]

*Note.* 95% confidence intervals are computed using normal approximation methods, assuming normality of the log effect. HR = Hazard Ratio.

**Table B2:** Interaction Effects

	Training Data		Testing Data	
	HR	95% CI	HR	95% CI
1 SE * Fast RT	0.95	[0.93 ; 0.97]	0.97	[0.95 ; 0.98]
2 SE * Fast RT	1.52	[1.49 ; 1.55]	1.52	[1.49 ; 1.55]
3 SE * Fast RT	1.51	[1.46 ; 1.55]	1.48	[1.44 ; 1.52]
>3 SE * Fast RT	1.35	[1.30 ; 1.40]	1.36	[1.31 ; 1.42]
1 SE * Easy Level	1.02	[0.99 ; 1.04]	1.01	[0.99 ; 1.03]
2 SE * Easy Level	1.14	[1.11 ; 1.17]	1.20	[1.17 ; 1.24]
3 SE * Easy Level	1.15	[1.10 ; 1.21]	1.21	[1.15 ; 1.27]
>3 SE * Easy Level	1.12	[1.05 ; 1.20]	1.23	[1.15 ; 1.31]
1 SE* Difficult Level	0.82	[0.81 ; 0.84]	0.81	[0.79 ; 0.82]
2 SE * Difficult Level	0.95	[0.93 ; 0.97]	0.91	[0.89 ; 0.93]
3 SE * Difficult Level	0.88	[0.85 ; 0.91]	0.89	[0.86 ; 0.92]
>3 SE * Difficult Level	0.90	[0.86 ; 0.93]	0.93	[0.89 ; 0.97]
1 SE* Grade 3-4	1.31	[1.28 ; 1.34]	1.21	[1.18 ; 1.24]
2 SE * Grade 3-4	0.78	[0.76 ; 0.80]	0.71	[0.70 ; 0.73]
3 SE * Grade 3-4	0.91	[0.87 ; 0.95]	0.82	[0.79 ; 0.85]
>3 SE * Grade 3-4	0.98	[0.94 ; 1.04]	0.87	[0.82 ; 0.91]
1 SE * Grade 5-6	1.13	[1.10 ; 1.16]	1.03	[1.00 ; 1.06]
2 SE * Grade 5-6	0.89	[0.86 ; 0.91]	0.80	[0.77 ; 0.82]
3 SE * Grade 5-6	0.97	[0.92 ; 1.01]	0.85	[0.81 ; 0.89]
>3 SE * Grade 5-6	1.00	[0.94 ; 1.06]	0.89	[0.84 ; 0.95]
1 SE * During School Hours	1.01	[0.97 ; 1.04]	0.98	[0.95 ; 1.01]
2 SE * During School Hours	0.72	[0.69 ; 0.74]	0.77	[0.74 ; 0.80]
3 SE * During School Hours	0.80	[0.76 ; 0.85]	0.77	[0.73 ; 0.82]
>3 SE * During School Hours	0.68	[0.64 ; 0.73]	0.73	[0.68 ; 0.79]

*Note.* 95% confidence intervals are computed using normal approximation methods, assuming normality of the log effect. HR = Hazard Ratio; SE = Sequential Error; RT = Response time.

**Table B3:** Markov Model Model Fit Indices

Model	Training Data		Testing Data	
	AIC	-2Log-Likelihood	AIC	-2Log-Likelihood
Baseline	2904426	2904424	2848467	2848465
Covariate	2371495	2371473	2383331	2383309
Interaction	2364586	2364516	2375501	2375431

## C Supplementary Material: Mixed Effects Logistic Regression

### C.1 Descriptive Statistics

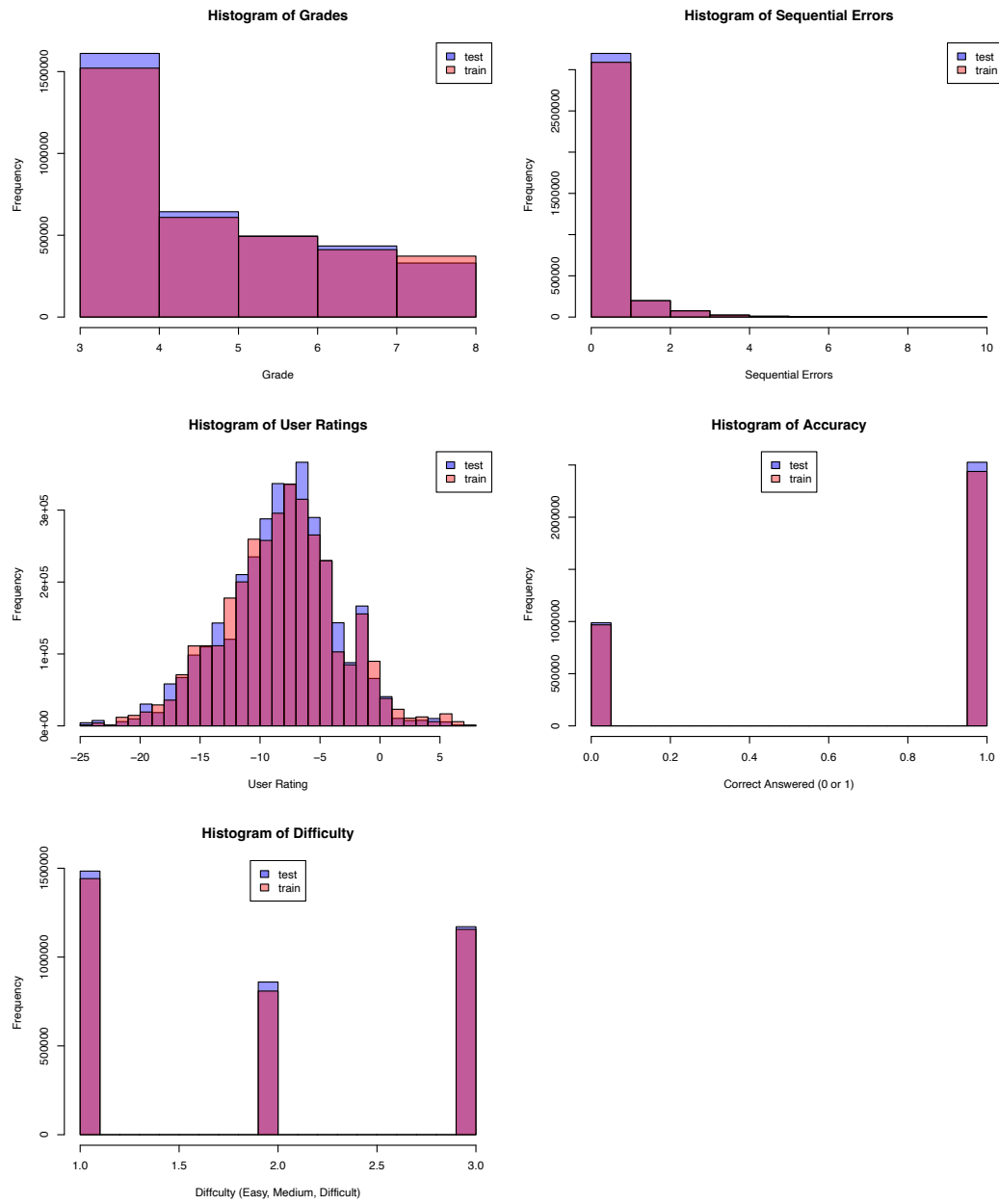


Figure C1: Distribution of key variables within the training and testing datasets.

## C.2 GLMER Model Results

**Table C1:** Fixed Effect Model Coefficients

	Training Data				Testing Data			
	Estimate	SE	z value	p value	Estimate	SE	z value	p value
(Intercept)	-3.48	0.02	-152.11	<0.001	-3.57	0.02	-149.97	<0.001
Sequential Error	0.81	0.01	119.57	<0.001	0.81	0.01	125.46	<0.001
Rating	-0.10	0.01	-8.83	<0.001	-0.09	0.01	-8.09	<0.001
Grade	-0.05	0.00	-12.07	<0.001	-0.03	0.00	-7.30	<0.001

*Note.* SE = Standard Error.

**Table C2:** Variance Estimates of Random Effects

	Training Data		Testing Data	
	Estimate	Std. Deviation	Estimate	Std. Deviation
(Intercept)	0.39	0.62	0.41	0.64
Sequential Error	0.14	0.38	0.13	0.36

**Table C3:** Correlation Between Fixed Effects

	Training Data				Testing Data			
	1.	2.	3.	4.	1.	2.	3.	4.
1. (Intercept)	1.000	-0.073	0.281	-0.886	1.000	-0.095	0.263	-0.891
2. Sequential Errors	-0.073	1.000	0.007	-0.018	-0.095	1.000	-0.005	0.006
3. User Rating	0.281	0.007	1.000	-0.286	0.263	-0.005	1.000	-0.269
4. Grade	-0.886	-0.018	-0.286	1.000	-0.891	0.006	-0.269	1.000

**Table C4:** Correlation Between Random Effects

Dataset	Variance-Covariance	Std. Correlation	$p$ value
Training	-0.02	-0.10	<0.001
Testing	-0.02	-0.10	<0.001