

# Determining supernova unknowns with the diffuse supernova neutrino background

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# Overview

- ① Neutrinos
- ② Core-collapse supernovae
- ③ Neutrino emission properties from core-collapse progenitor stars
- ④ Time-integrated neutrino fluxes
- ⑤ Diffuse supernova neutrino background
- ⑥ The DSNB event rate at future generation neutrino detectors
- ⑦ Combined likelihood analyses
- ⑧ Conclusions

**"Measuring the supernova unknowns at the next-generation neutrino telescopes through the diffuse neutrino background"**

by Klaes Moller, Anna M. Suliga, Irene Tamborra and Peter B. Denton.

*JCAP* **1805** (2018) 066

# Neutrinos

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# Fermions

Leptons	Quarks			Force carriers	
	u up	c charm	t top	$\gamma$ photon	H Higgs boson
	d down	s strange	b bottom	g gluon	
e electron	$\mu$ muon	$\tau$ tau		Z Z boson	
$\nu_e$ electron neutrino	$\nu_\mu$ muon neutrino	$\nu_\tau$ tau neutrino		W W bosons	

# Neutrino flavor and mass states

flavor basis      mass basis

$$\begin{bmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{bmatrix} = U \begin{bmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{bmatrix}$$

atmospheric

beam,  
reactor

solar,  
reactor

$$U = \begin{bmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{bmatrix} \begin{bmatrix} c_{13} & 0 & s_{13}e^{-i\delta_{CP}} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta_{CP}} & 0 & c_{13} \end{bmatrix} \begin{bmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

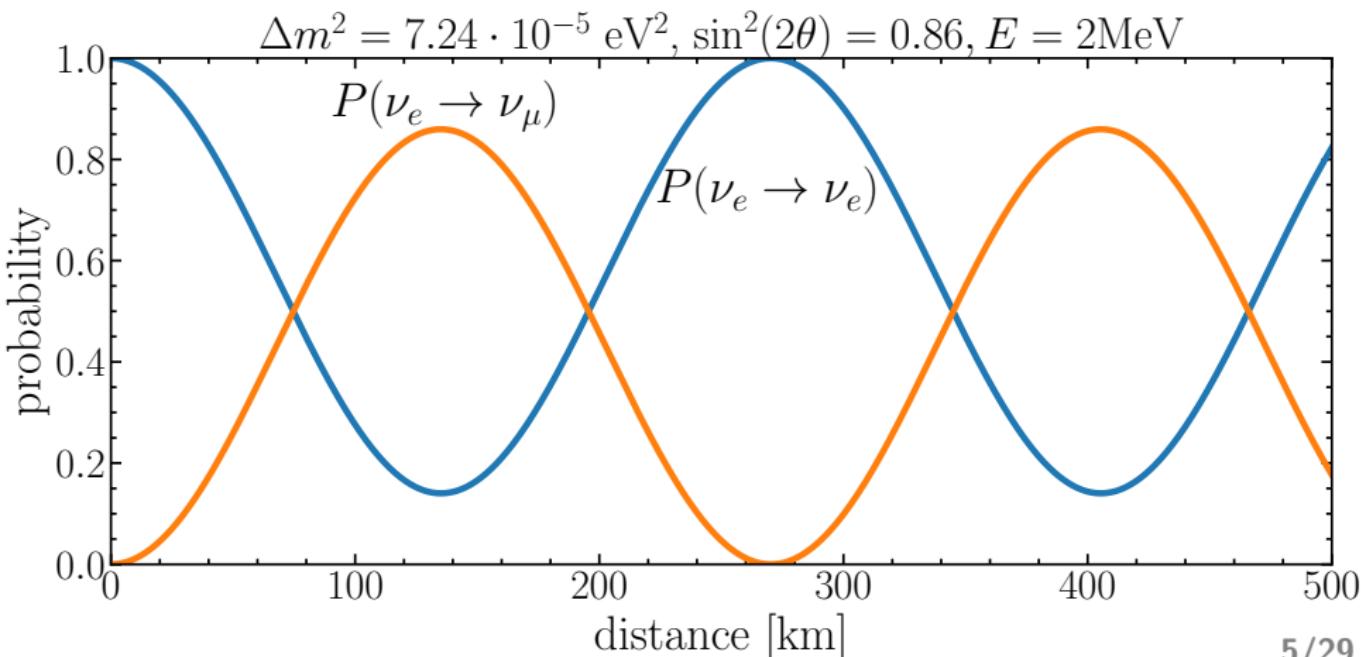
$$c_{ij} = \cos(\theta_{ij}), s_{ij} = \sin \theta_{ij}, \delta_{CP}$$

# Neutrino oscillations in vacuum

$2\nu$  mixing = easy dependence on

$$P_{\nu_e \rightarrow \nu_e} = 1 - \sin^2 2\theta \sin^2 \frac{\Delta m^2 L}{4E}$$

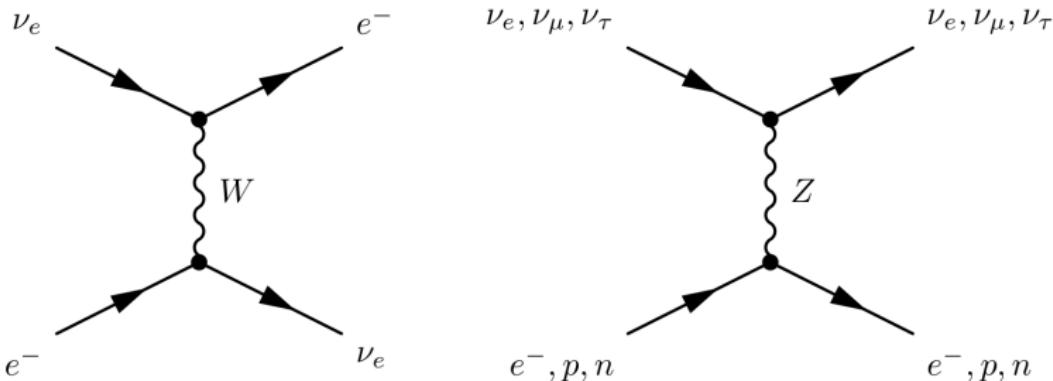
- mixing angle
- mass squared difference



# Neutrino oscillations in matter

$$P(\nu_e \rightarrow \nu_\mu) = \sin^2 2\tilde{\theta} \sin^2 \frac{\Delta \tilde{m}^2 L}{4E}$$

- $V_{CC} \rightarrow 0$ , vacuum oscillations  $V_{CC} \propto N_e$
- $V_{CC} \rightarrow \infty$ , suppression of oscillations
- $V_{CC} = \frac{\Delta m^2}{2E} \cos 2\theta$ , resonance enhancement of oscillations



# Density matrix evolution

$$\frac{d}{dx}\rho = -i[H, \rho],$$

$$H = U^\dagger \text{diag}(m_1^2, m_2^2, m_3^2) U + \text{diag}(V_{CC}, 0, 0)$$

**vacuum**                           **matter**

$$\rho = |\psi\rangle\langle\psi| = \begin{bmatrix} \rho_{ee} & \rho_{e\mu} & \rho_{e\tau} \\ \rho_{\mu e} & \rho_{\mu\mu} & \rho_{\mu\tau} \\ \rho_{\tau e} & \rho_{\tau\mu} & \rho_{\tau\tau} \end{bmatrix}$$

**Initial condition for very dense medium**

$$\rho = \begin{bmatrix} n_e & 0 & 0 \\ 0 & n_\mu & 0 \\ 0 & 0 & n_\tau \end{bmatrix}, \quad n_\alpha = F_\alpha^0 / (F_e^0 + F_\mu^0 + F_\tau^0)$$

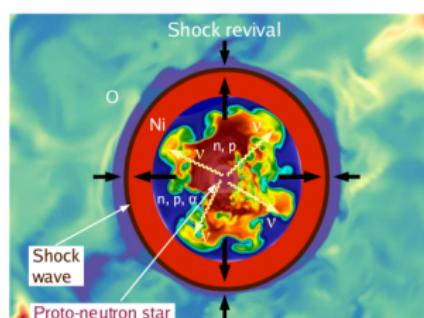
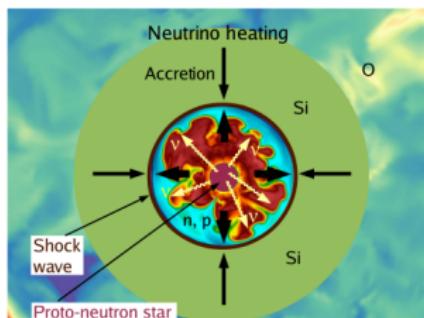
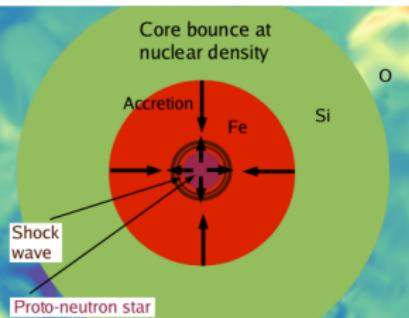
## Core-collapse supernovae

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# What is core-collapse supernova?

## Different phases of core-collapse supernova explosion

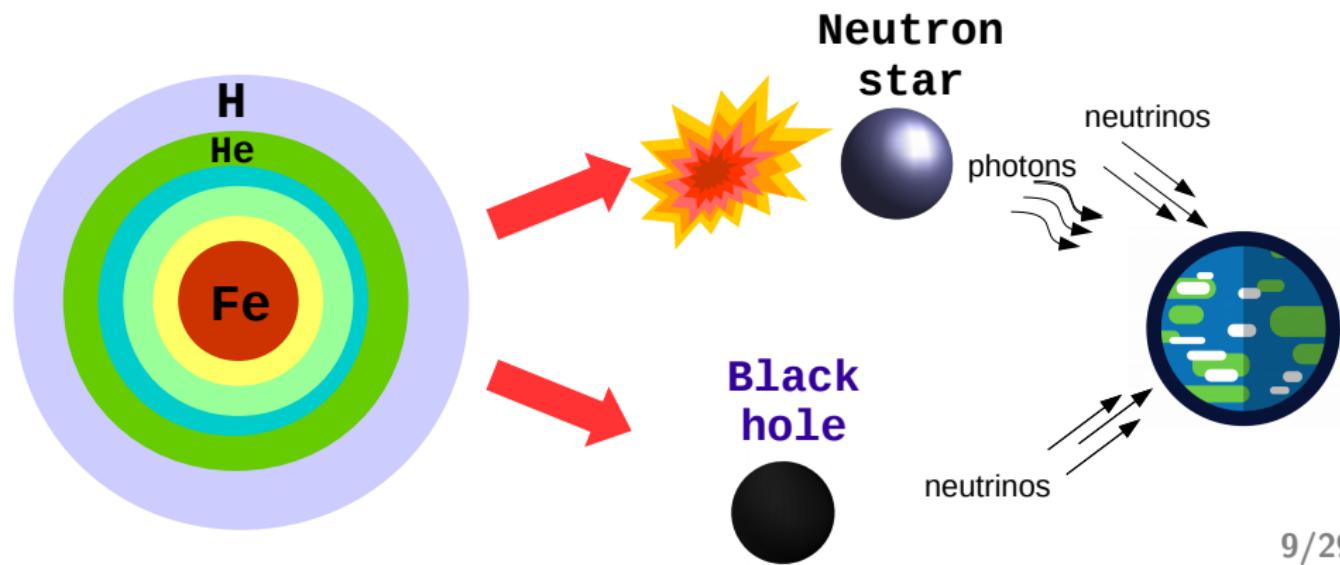
- neutronization phase,  
 $\nu_e$  burst  $\sim 40$  ms
- accretion phase,  
 $\sim 100$  ms
- cooling phase,  
 $\sim 10$  s



# Core-collapse supernovae

## Neutrinos:

- play a crucial role in the explosion mechanism
- can reveal the interior conditions of a collapsing star
- are the only messengers from the collapse to a black hole (+ GW)



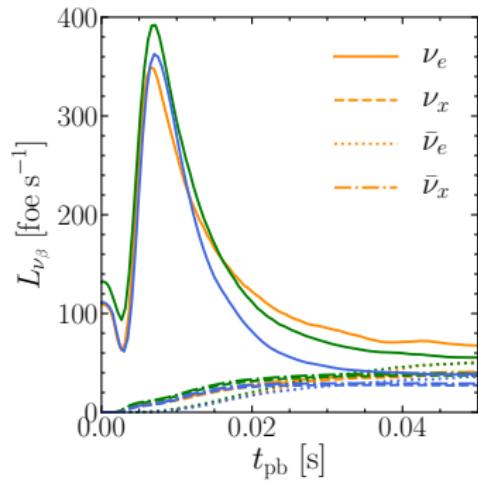
# **Neutrino emission properties from core-collapse progenitor stars**

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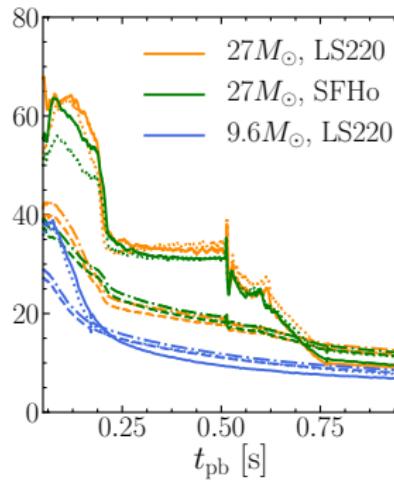
# Progenitor stars forming neutron stars

1 foe =  $10^{51}$  ergs

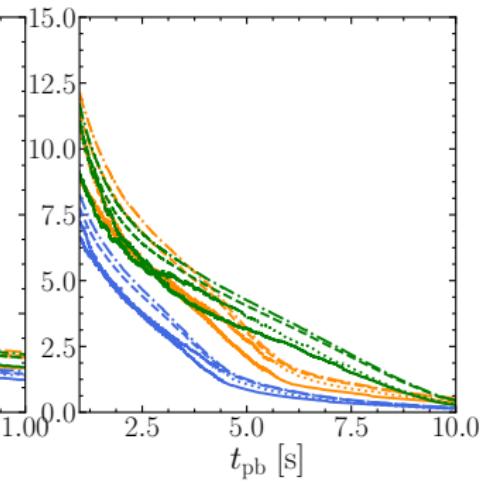
CC-SN progenitors



$\nu_e$  burst



accretion

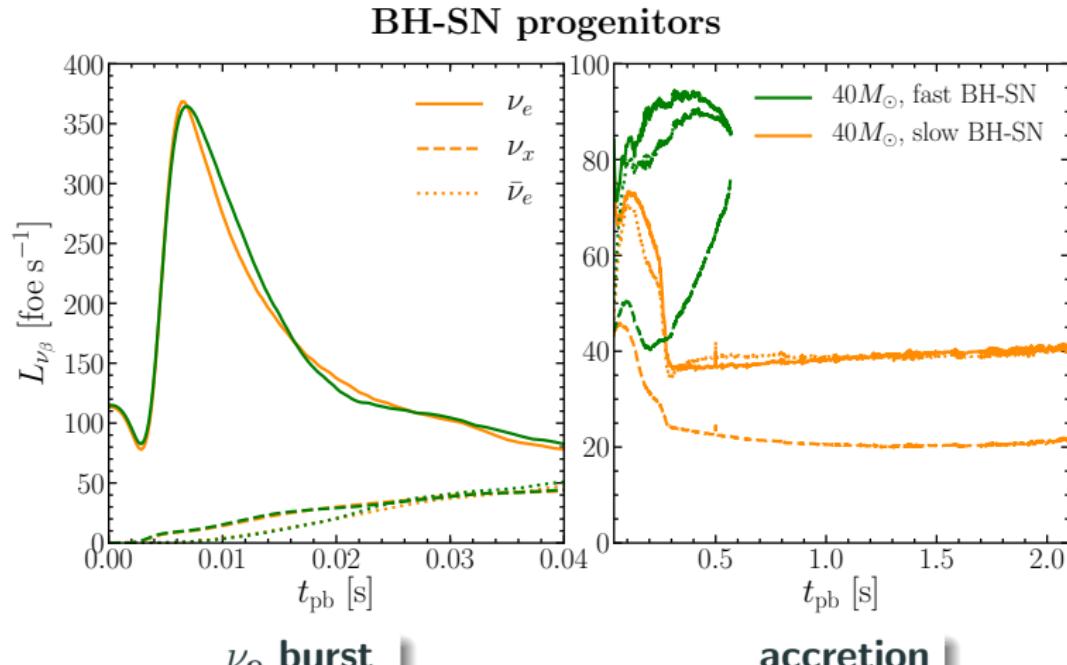


cooling

## CC-SN

equation of state = LS220 or SFHo, mass =  $9.6 M_\odot$  or  $27 M_\odot$

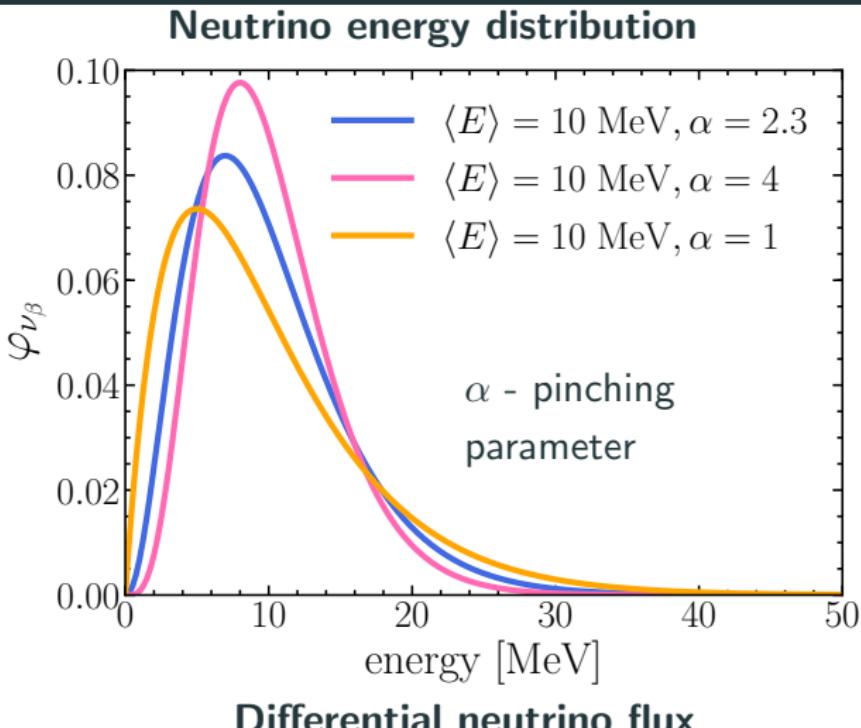
# Progenitor stars forming black holes



**BH-SN**

equation of state = LS220, mass =  $40 M_\odot$ ,  $t_{\text{BH}} = 0.57$  s or  $2.1$  s

# Neutrino fluxes



$$f_{\nu_\beta}^0(E, t_{\text{pb}}) = \frac{L_{\nu_\beta}(t_{\text{pb}})}{4\pi r^2} \frac{\varphi_{\nu_\beta}(E, t_{\text{pb}})}{\langle E_{\nu_\beta}(t_{\text{pb}}) \rangle} = \frac{F_{\nu_\beta}^0(E, t_{\text{pb}})}{4\pi r^2}$$

# Adiabatic oscillations

## Assumptions

- slowly changing matter profile
- oscillations can follow the change of matter

## Fluxes arriving at the Earth

$$F_\alpha = \sum_i |U_{\alpha i}|^2 F_i$$

~0.71 ~0.98

NO

$$F_{\bar{\nu}_e} = \cos^2 \theta_{12} \cos^2 \theta_{13} (F_{\bar{\nu}_e}^0 - F_{\bar{\nu}_x}^0) + F_{\bar{\nu}_x}^0 \approx \cos^2 \theta_{12} (F_{\bar{\nu}_e}^0 - F_{\bar{\nu}_x}^0) + F_{\bar{\nu}_x}^0$$

~0.02

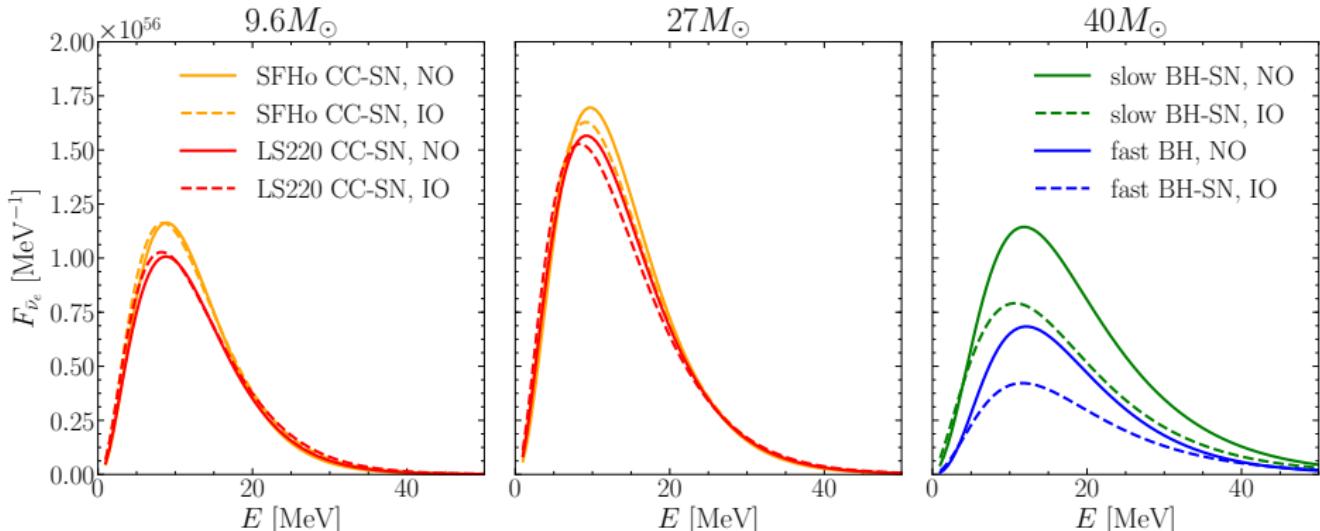
IO

$$F_{\bar{\nu}_e} = \sin^2 \theta_{13} F_{\bar{\nu}_e}^0 + \cos^2 \theta_{13} F_{\bar{\nu}_x}^0 \approx F_{\bar{\nu}_x}^0$$

## **Time-integrated neutrino fluxes**

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# Time-integrated neutrino fluxes



	<b>CC-SN</b>	<b>BH-SN</b>
<b>high-energy neutrinos</b>	fewer	more
<b>distinguish progenitor</b>	no	yes
<b>distinguish mass ordering</b>	no	yes

# **Diffuse supernova neutrino background**

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# Diffuse supernova neutrino background (DSNB)

$$\Phi_{\nu_\beta}(E) = \frac{c}{H_0} \int_{8M_\odot}^{125M_\odot} dM \int_0^{z_{\max}} dz \frac{R_{\text{SN}}(z, M)}{\sqrt{\Omega_M(1+z)^3 + \Omega_\Lambda}} \\ \times [f_{\text{CC-SN}} F_{\nu_\beta, \text{CC-SN}}(E', M) + f_{\text{BH-SN}} F_{\nu_\beta, \text{BH-SN}}(E', M)]$$

fraction of neutron-star-forming progenitors

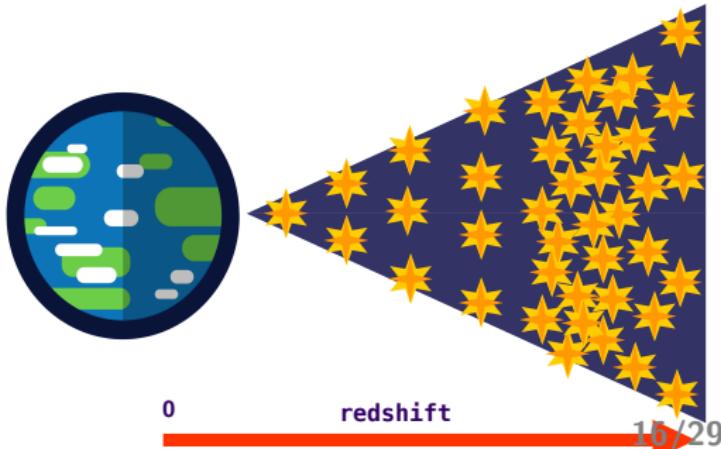
fraction of black-hole-forming progenitors

cosmological supernovae rate

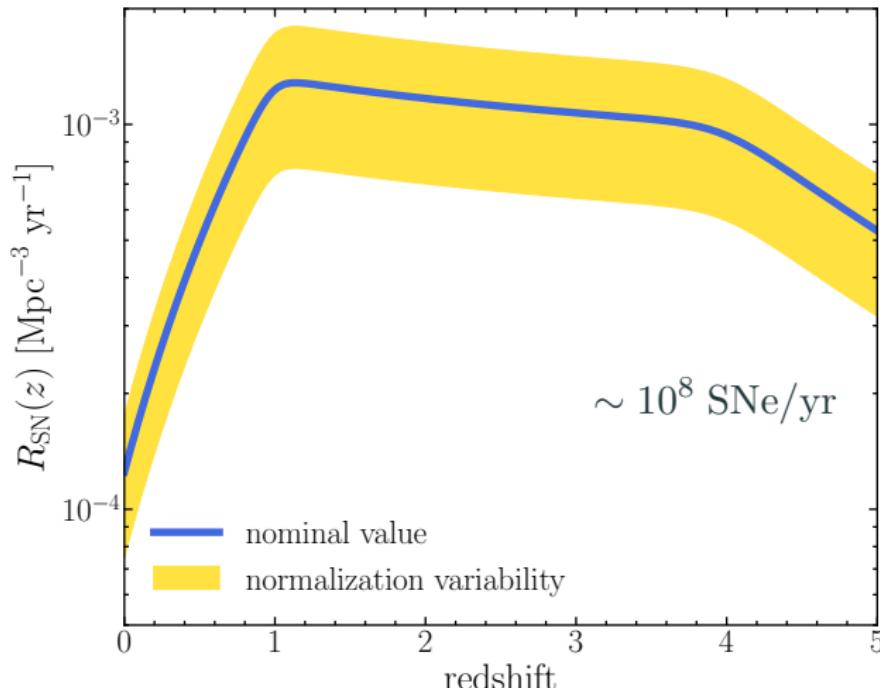
oscillated neutrino flux  
 $E' = (1+z)E$

The DSNB is sensitive to:

- $R_{\text{SN}}$
- $f_{\text{BH-SN}}$
- neutrino mass ordering
- equation of state
- mass accretion rate in BH-SN

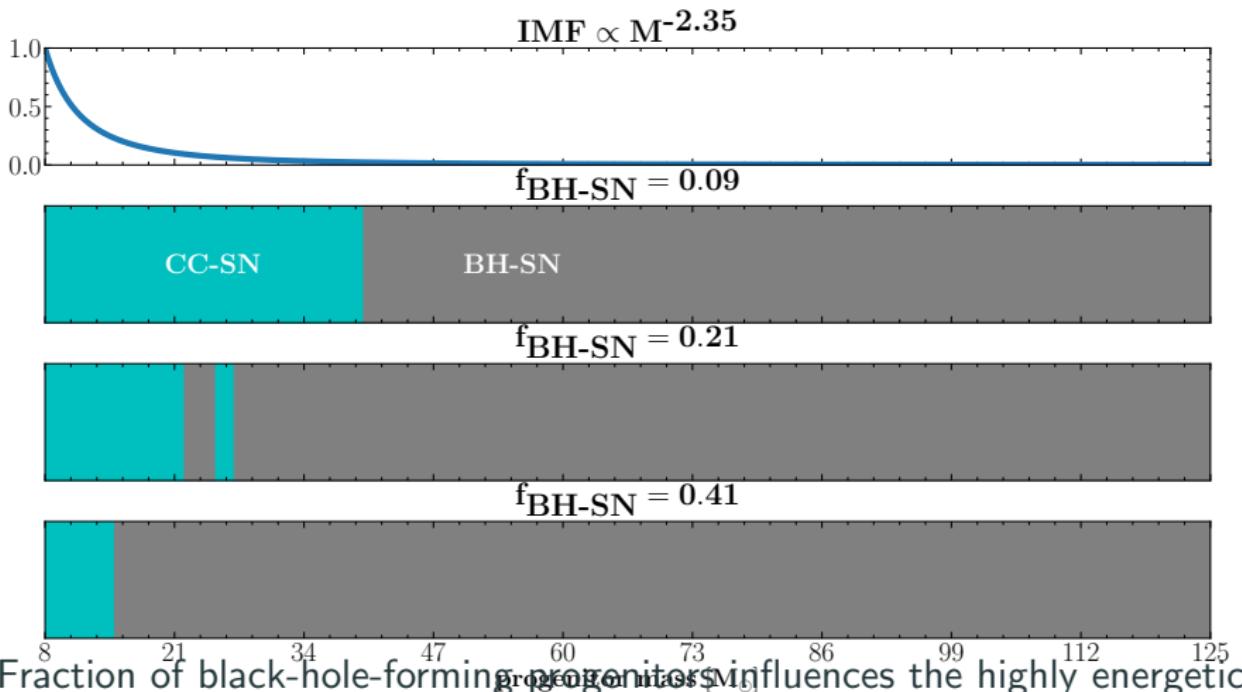


## Cosmological supernovae rate



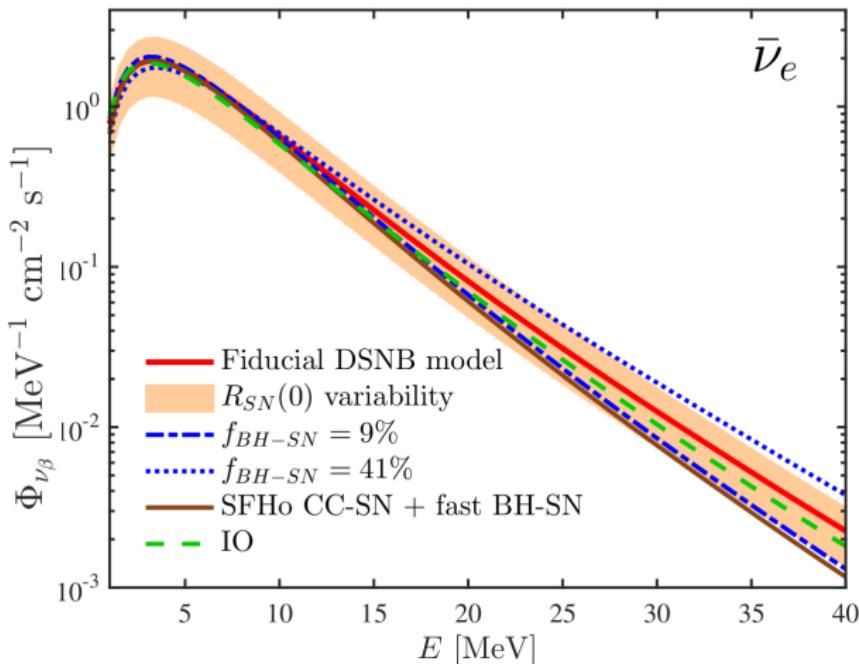
The supernovae rate influences the normalization of the DSNB.

# Fraction of BH-forming progenitors



Fraction of black-hole-forming progenitors influences the highly energetic part of the DSNB, above  $\sim 15$  MeV.

# Diffuse supernova neutrino background



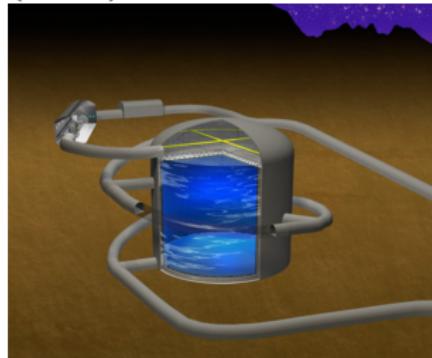
**Fiducial DSNB model:**  $R_{SN}(0) = 1.25 \times 10^{-4}$  Mpc $^{-3}$  yr $^{-1}$ ,  $f_{BH-SN} = 0.21$ ,  
equation of state = LS220, mass accretion rate = slow

## **The DSNB event rate at future generation neutrino detectors**

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# Future generation neutrino detectors

**Hyper-Kamiokande**  
(2025)



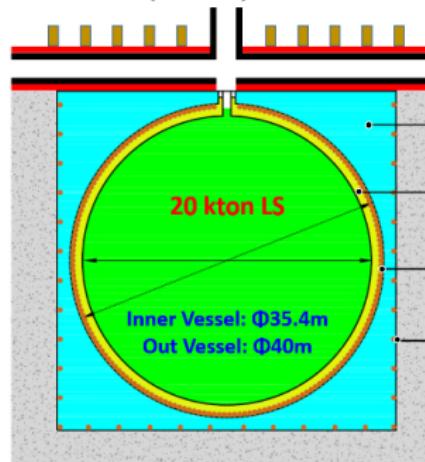
**fiducial volume**

2×187 kton

**main detection channel**



**JUNO (2020)**



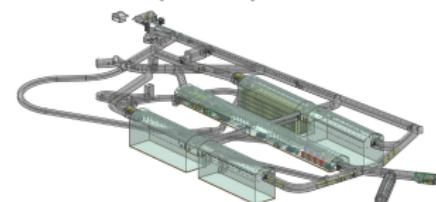
**fiducial volume**

17 kton

**main detection channel**



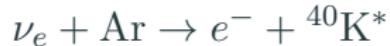
**DUNE (2027)**



**fiducial volume**

4×10 kton

**main detection channel**



**Super-Kamiokande**

**+ gadolinium**

**3 σ detection in 10 yrs**

## Sources of background

	atmospheric BG				solar $\nu_e$	reactor $\bar{\nu}_e$
	invisible $\mu$	spallation	NC	$\nu_e/\bar{\nu}_e$		
HK (Gd)	Yes	Yes	Yes	Yes	No	Yes
JUNO	No	No	Yes	Yes	No	Yes
DUNE	No	No	No	Yes	Yes	No

Yes - sets lower limit for the DSNB detection window

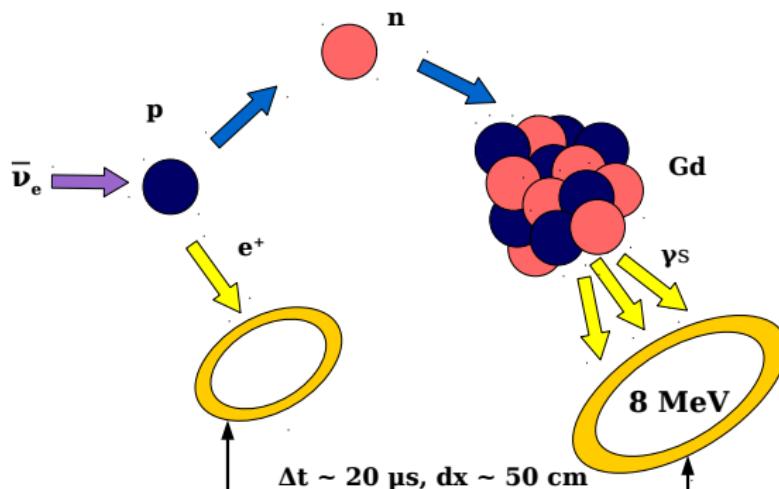
Yes - sets upper limit for the DSNB detection window

Yes - doesn't set limit for the DSNB detection window

# Gadolinium sulfate enrichment

## Neutron tagging in Gd-enriched water Cherenkov detectors

- coincidence detection of positron and neutron
- high cross section for neutron capture  $\sim 4900$  barn
- elimination of spallation background
- reduction of invisible muon background



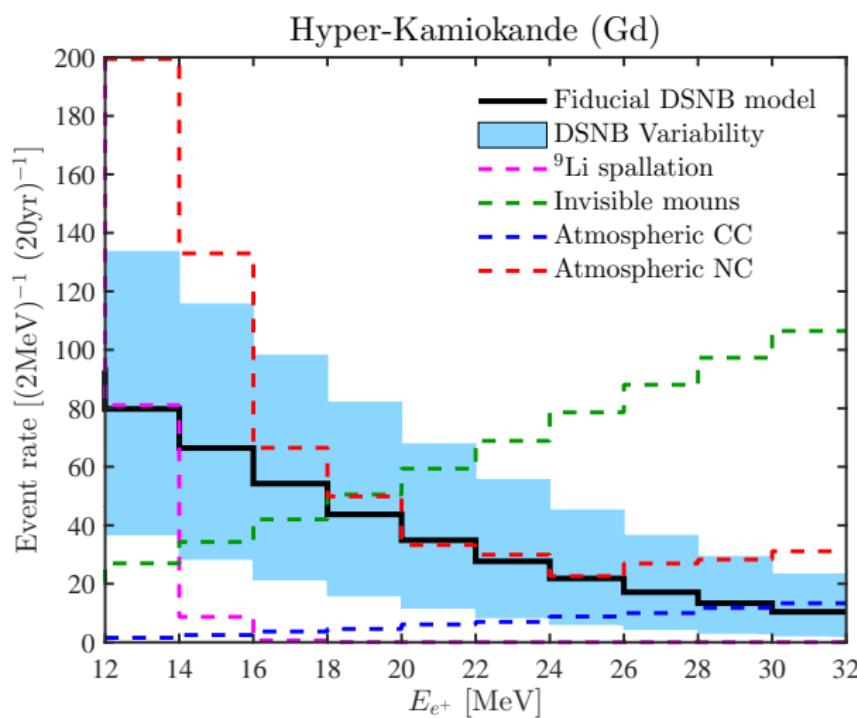
## Interaction rates in detectors

$$R = \int \Phi \sigma N_t f$$

flux cross number of  
section targets

$t$  detector efficiency

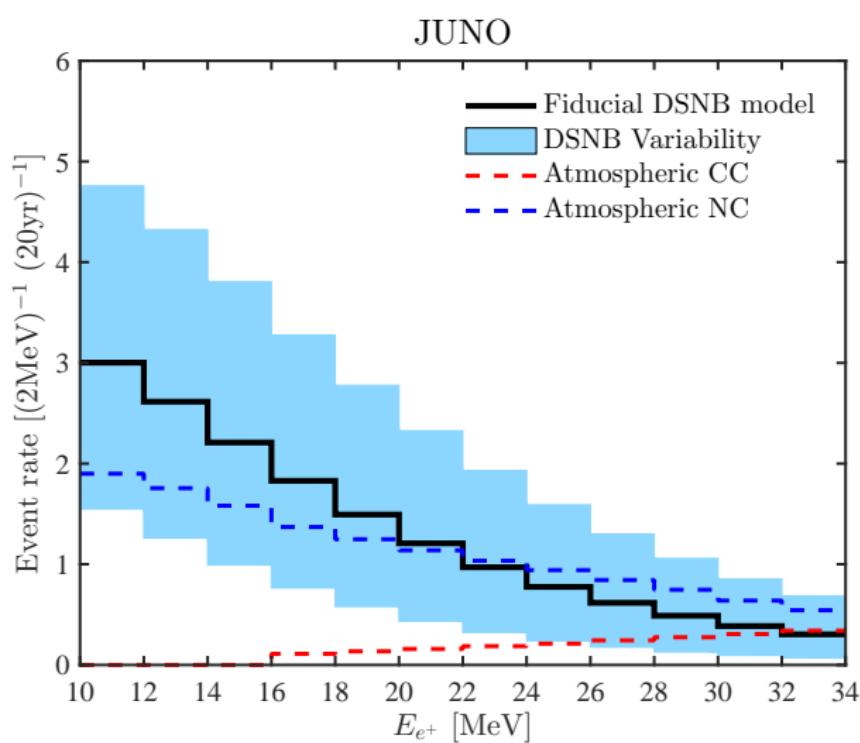
# The DSNB event rates



## Detectability prospects for 20 yrs

- HK (Gd) with NC:  
 $10 \sigma [4.8 - 15]$
- HK (Gd) w/o NC:  
 $12.5 \sigma [6.2 - 18]$

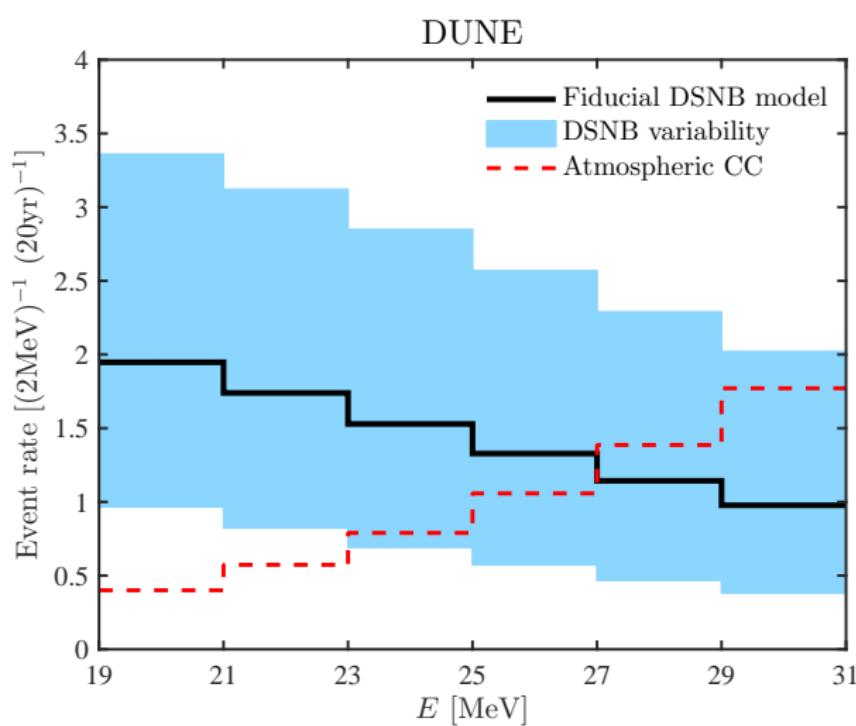
# The DSNB event rates



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- JUNO:  $3.4 \sigma [1.6-5.4]$

# The DSNB event rates



## Detectability prospects for 20 yrs

- HK (Gd) with NC:  
 $10 \sigma [4.8 - 15]$
- HK (Gd) w/o NC:  
 $12.5 \sigma [6.2 - 18]$
- JUNO:  $3.4 \sigma [1.6-5.4]$
- DUNE:  $2.8 \sigma [1.6-4]$

## Combined likelihood analyses

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# Combined likelihood analyses

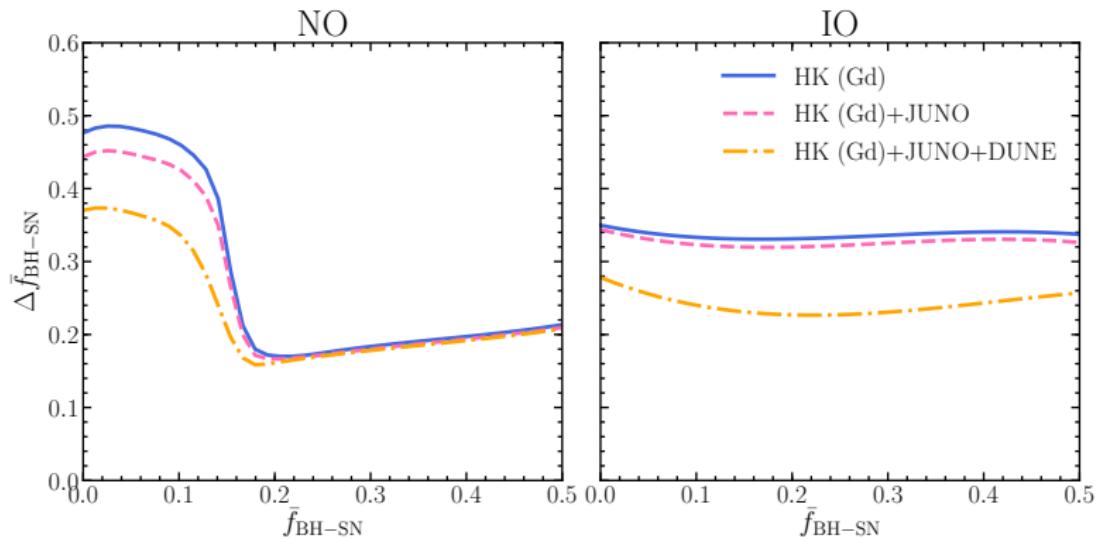
## Significance test

$$\chi^2 = \min_A \left( \sum_j \chi_{A,j}^2 + \chi_{\text{HK}}^2 + \chi_{\text{JUNO}}^2 + \chi_{\text{DUNE}}^2 \right)$$

The set of parameters to be marginalized over:

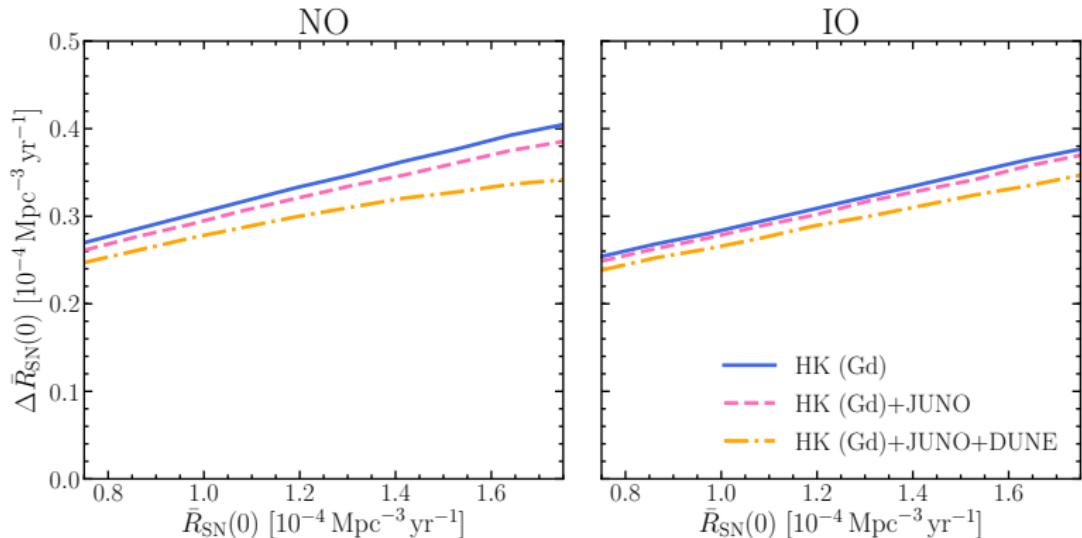
- $f_{\text{BH-SN}}$ ,  $\Delta_{f_{\text{BH-SN}}} = 0.2$
- $R_{\text{SN}}(0)$ ,  $\Delta_{R_{\text{SN}}(0)} = 0.25 \times 10^{-4} \text{ Mpc}^{-3} \text{ yr}^{-1}$
- background normalization uncertainty,  $\Delta_{\text{BG}} = 20\%$
- liquid argon cross section uncertainty,  $\Delta\sigma_{\text{LAr}} = 15\%$
- mass accretion rate - equation of state uncertainty

# Expected $1\sigma$ uncertainty: fraction of BH forming progenitors

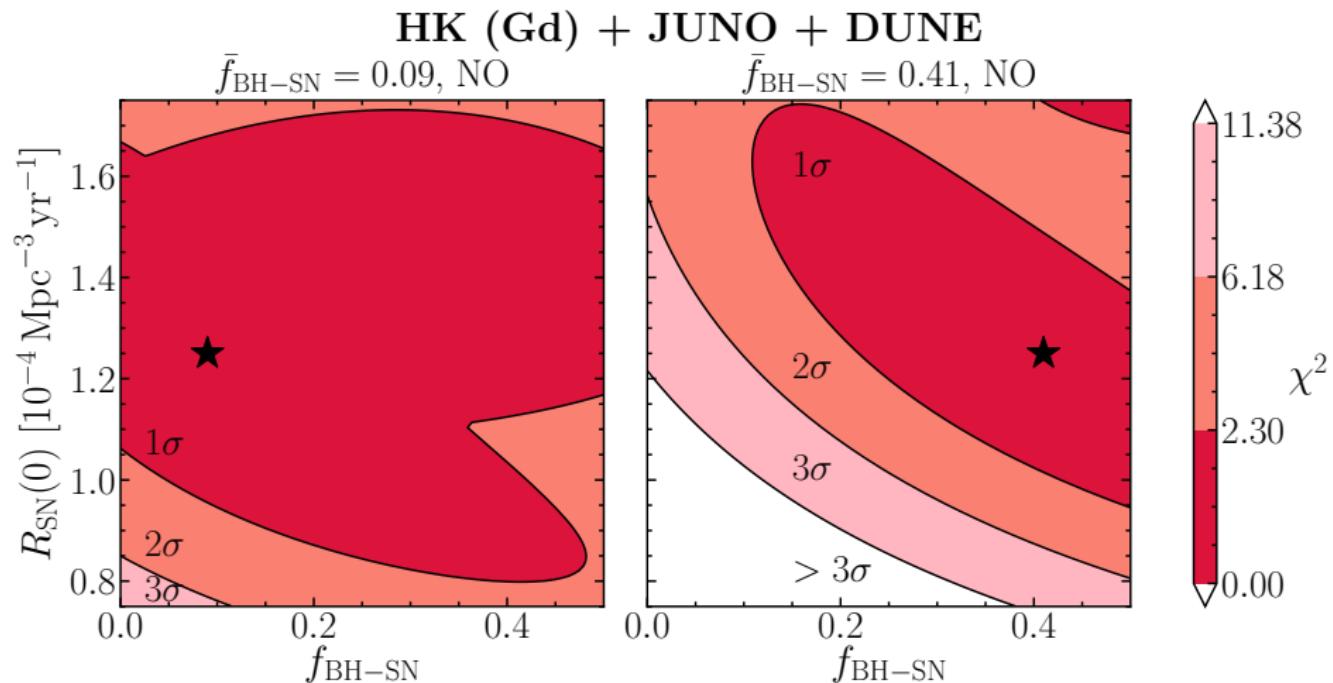


- The high uncertainty comes from  $f_{\text{BH-SN}}$ -mass accretion rate degeneracy
- DUNE is sensitive to neutrinos → helps to reduce the uncertainty

## Expected $1\sigma$ uncertainty: local supernova rate



Relative error of 20%-33% independent of the mass ordering.



## **Future improvements**

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## Future improvements

- more progenitors
- neutrino-neutrino interactions
- 3D models
- $f_{\text{BH-SN}}(z)$
- muon formation feedback

## Conclusions

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# Conclusions

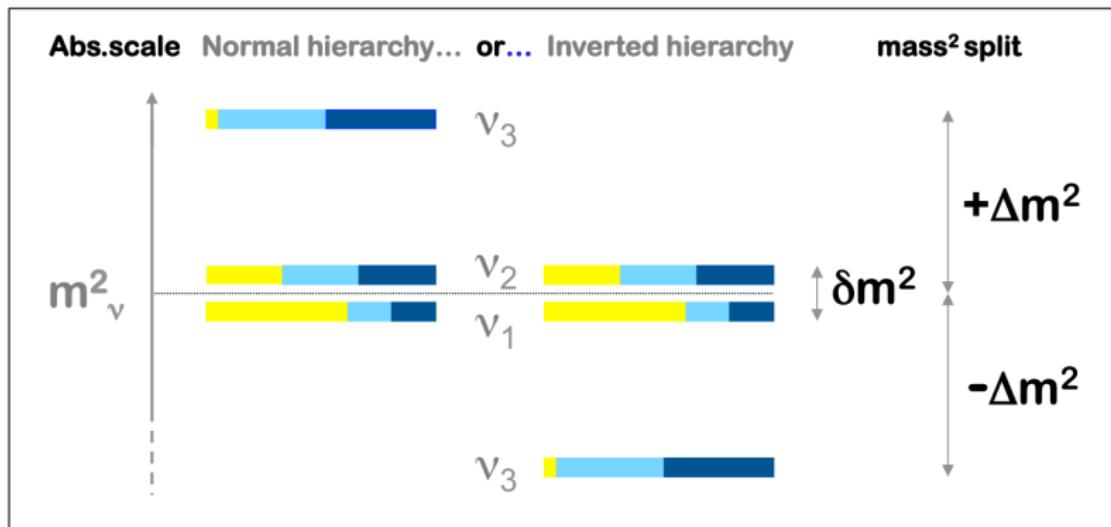
- Future neutrino detectors will detect and measure the DSNB
- The DSNB
  - is sensitive to the fraction of BH forming progenitors
  - is sensitive to the local supernovae rate
  - shows no discriminating power of the mass accretion rate
- Measurement = an independent check for EM and GW surveys

## **Backup slides**

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# Neutrino mass ordering

e  $\mu$   $\tau$



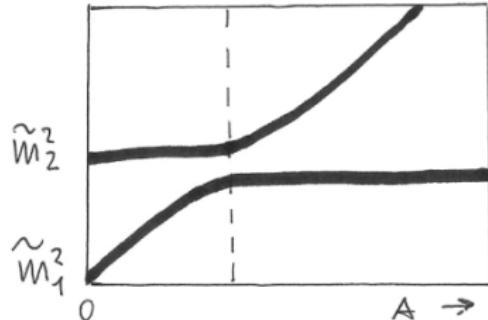
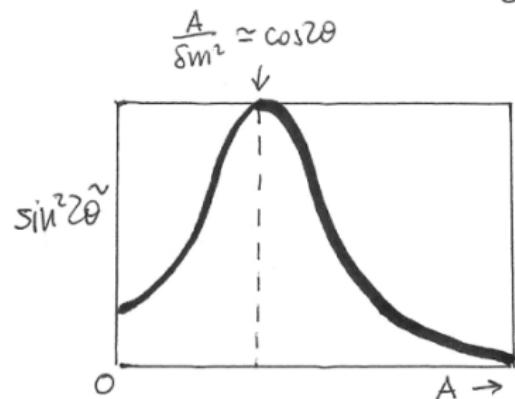
## Effective mixing parameters

$$\sin \tilde{2\theta} = \frac{\sin 2\theta}{\sqrt{(\cos 2\theta - \frac{A}{\Delta m^2})^2 + \sin^2 2\theta}},$$

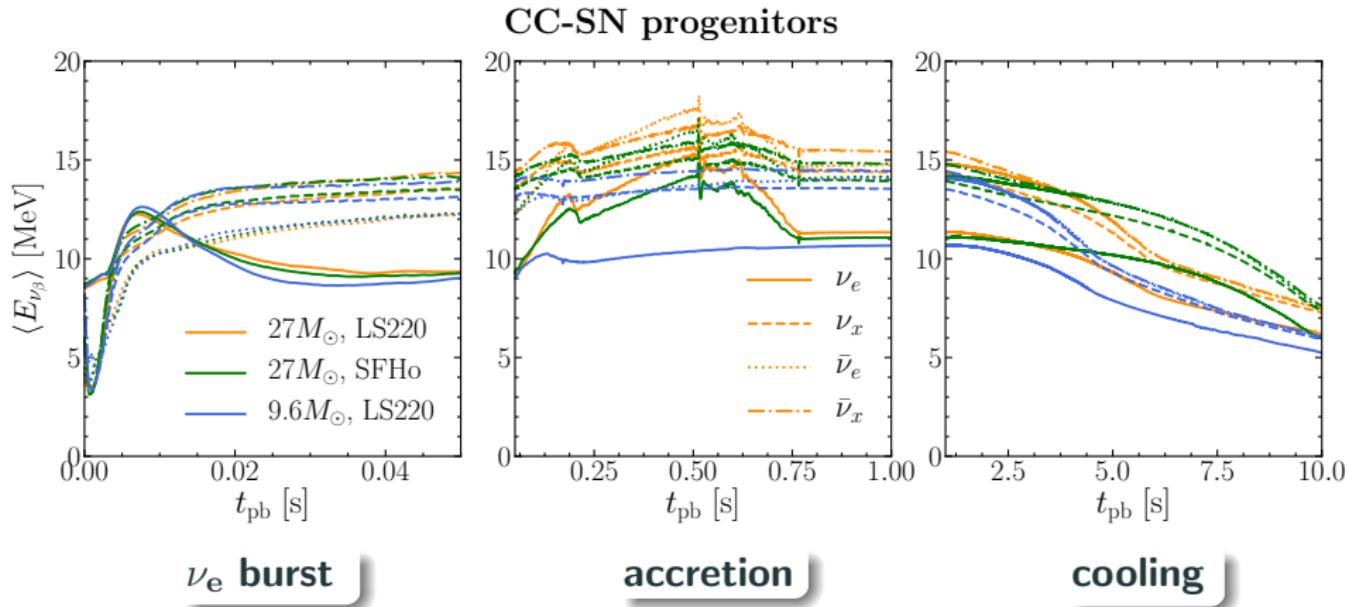
$$\cos \tilde{2\theta} = \frac{\cos^2 2\theta - \frac{A}{\Delta m^2}}{\sqrt{(\cos 2\theta - \frac{A}{\Delta m^2})^2 + \sin^2 2\theta}}$$

$$\tilde{\Delta m^2} = \Delta m^2 \frac{\sin 2\theta}{\sin \tilde{2\theta}}$$

$$A = 2\sqrt{2}G_F N_e E$$



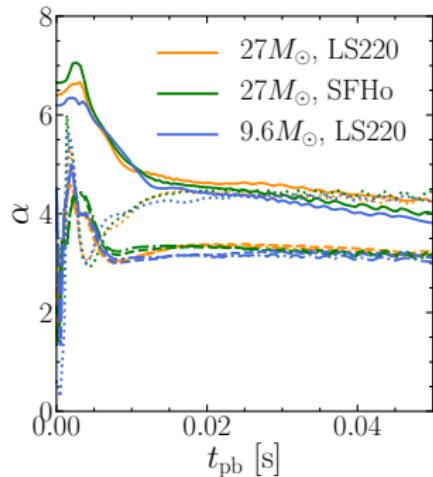
# Progenitor stars forming neutron stars



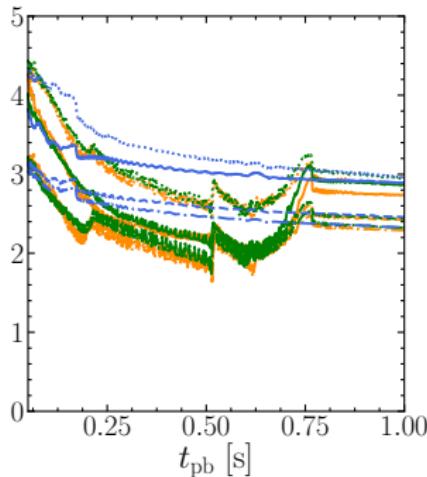
Early times  $\langle E_{\nu_e} \rangle < \langle E_{\bar{\nu}_e} \rangle < \langle E_{\nu_x} \rangle$ ,  
Late times  $\langle E_{\nu_e} \rangle < \langle E_{\nu_x} \rangle < \langle E_{\bar{\nu}_e} \rangle$

# Progenitor stars forming neutron stars

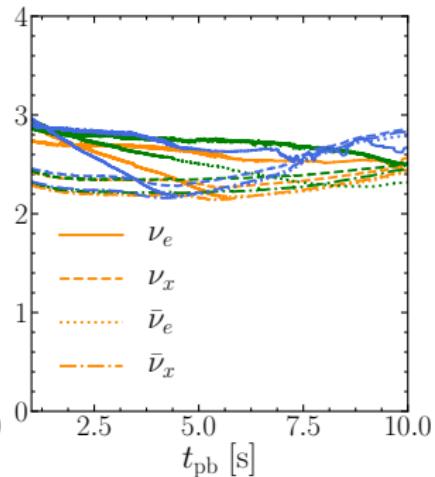
CC-SN progenitors



$\nu_e$  burst



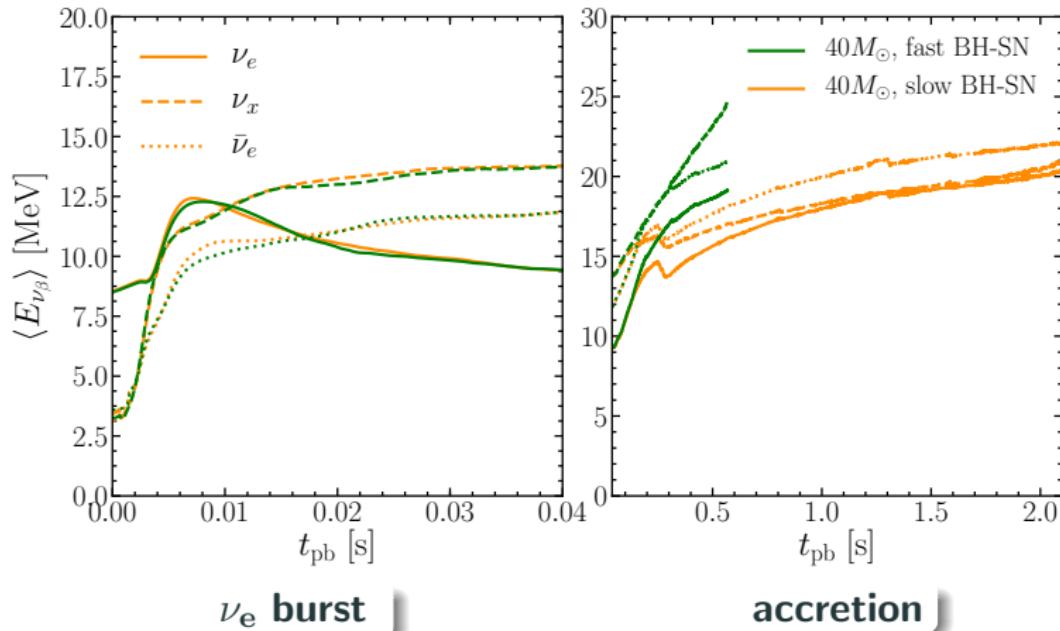
accretion



cooling

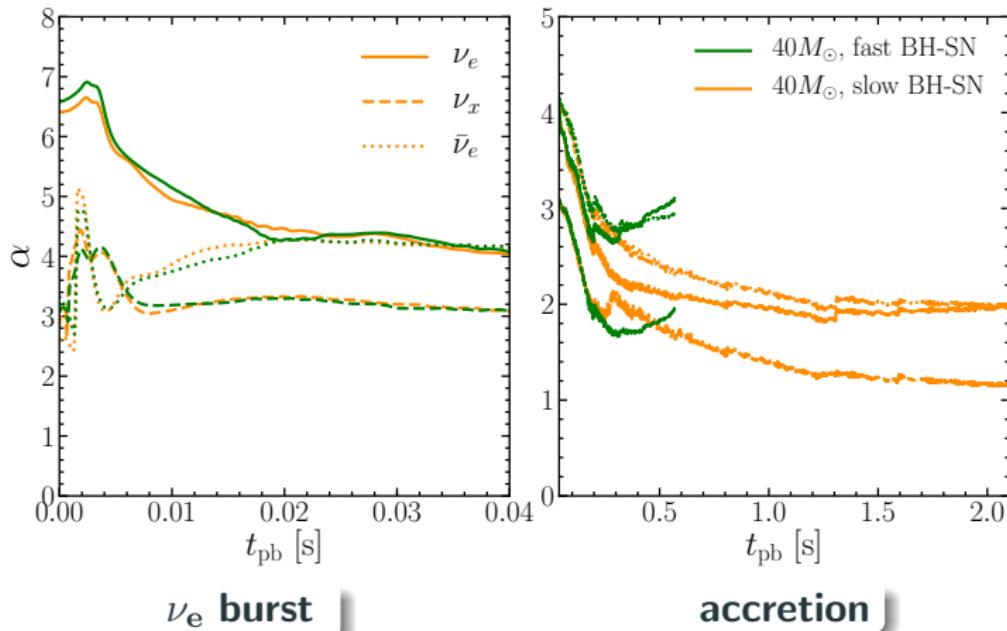
# Progenitor stars forming black holes

## BH-SN progenitors

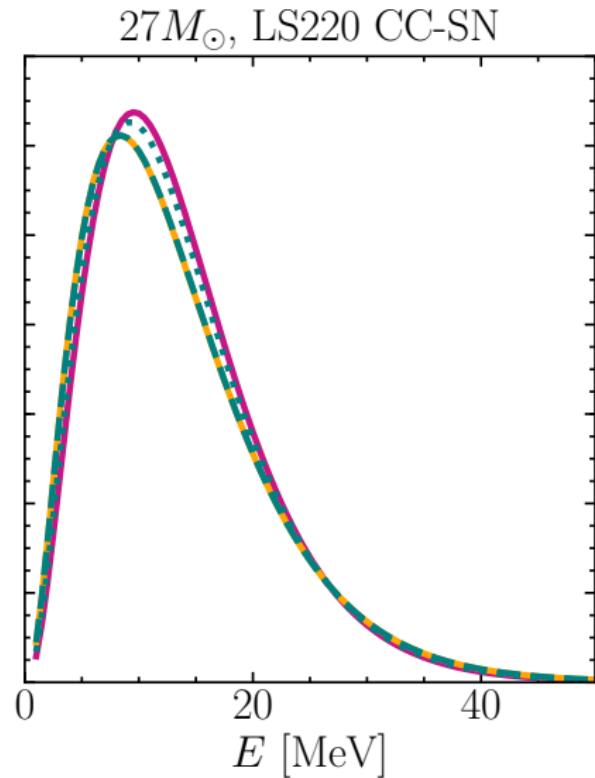
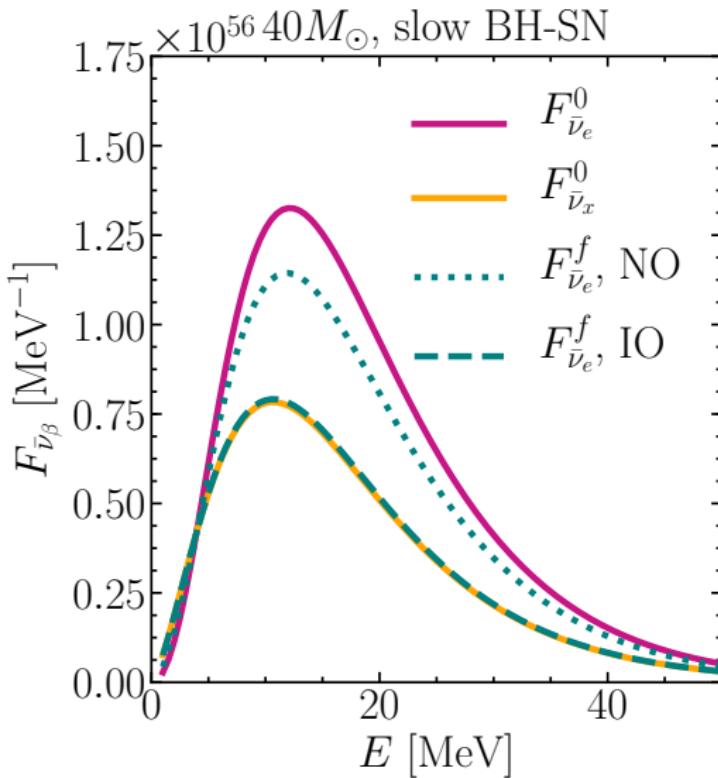


# Progenitor stars forming black holes

## BH-SN progenitors



# Time-integrated neutrino fluxes



# Neutrino fluxes

## Neutrino energy distribution

$$\varphi_{\nu_\beta}(E, t_{\text{pb}}) = \xi_{\nu_\beta}(t_{\text{pb}}) \left( \frac{E}{\langle E_{\nu_\beta}(t_{\text{pb}}) \rangle} \right)^{\alpha_\beta(t_{\text{pb}})} e^{-\frac{E(\alpha_\beta(t_{\text{pb}})+1)}{\langle E_{\nu_\beta}(t_{\text{pb}}) \rangle}}$$

normalization  $1/\xi_{\nu_\beta}(t_{\text{pb}}) = \int dE \varphi_{\nu_\beta}(E, t_{\text{pb}})$

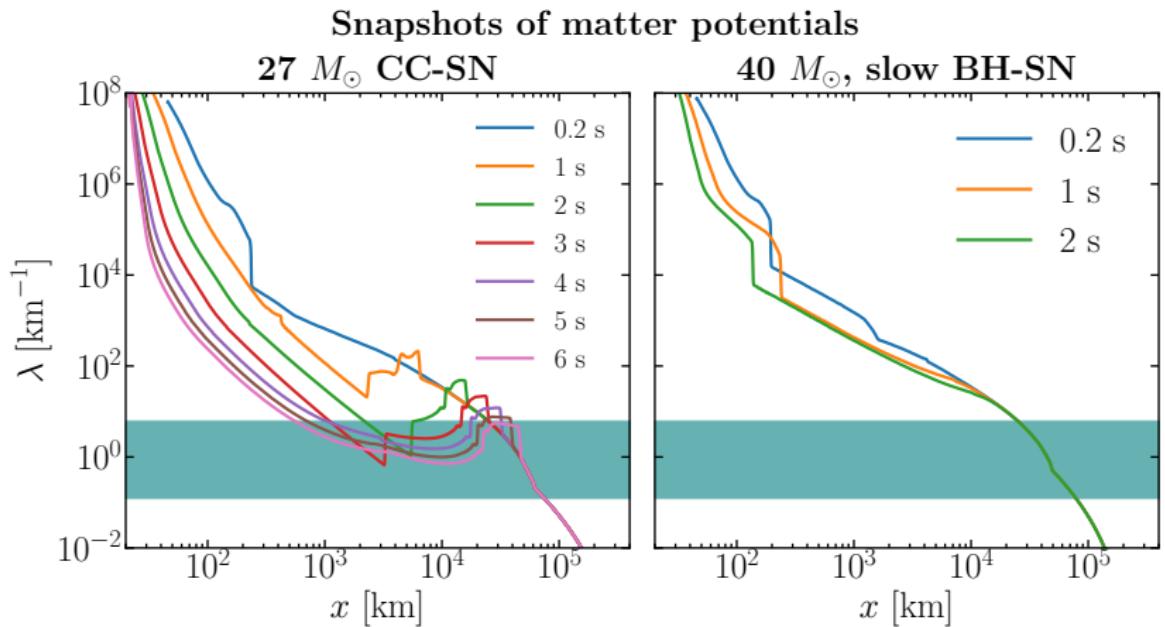
## Pinching parameter

$$\alpha_\beta(t_{\text{pb}}) = \frac{\langle E_{\nu_\beta}(t_{\text{pb}})^2 \rangle - 2\langle E_{\nu_\beta}(t_{\text{pb}}) \rangle^2}{\langle E_{\nu_\beta}(t_{\text{pb}}) \rangle^2 - \langle E_{\nu_\beta}(t_{\text{pb}})^2 \rangle}.$$

## Differential neutrino flux

$$f_{\nu_\beta}^0(E, t_{\text{pb}}) = \frac{L_{\nu_\beta}(t_{\text{pb}})}{4\pi r^2} \frac{\varphi_{\nu_\beta}(E, t_{\text{pb}})}{\langle E_{\nu_\beta}(t_{\text{pb}}) \rangle} = \frac{F_{\nu_\beta(E, t_{\text{pb}})}^0}{4\pi r^2}$$

# Matter potentials



## resonance potential

$$\lambda_{res} = \frac{\cos 2\theta_{13} \Delta m^2}{2E} = 2.538 \cos 2\theta_{13} \left( \frac{\Delta m^2}{eV^2} \right) \left( \frac{GeV}{E} \right) [\text{km}^{-1}]$$

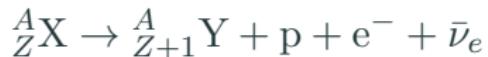
# Main sources of backgrounds

## cosmic rays interactions with atmosphere

$$\pi^+ \rightarrow \mu^+ + \nu_\mu \quad , \quad \pi^- \rightarrow \mu^- + \bar{\nu}_\mu$$

$$\mu^+ \rightarrow e^+ + \bar{\nu}_\mu + \nu_e \quad , \quad \mu^- \rightarrow e^- + \nu_\mu + \bar{\nu}_e$$

## reactor antineutrinos



## neutrinos from the Sun

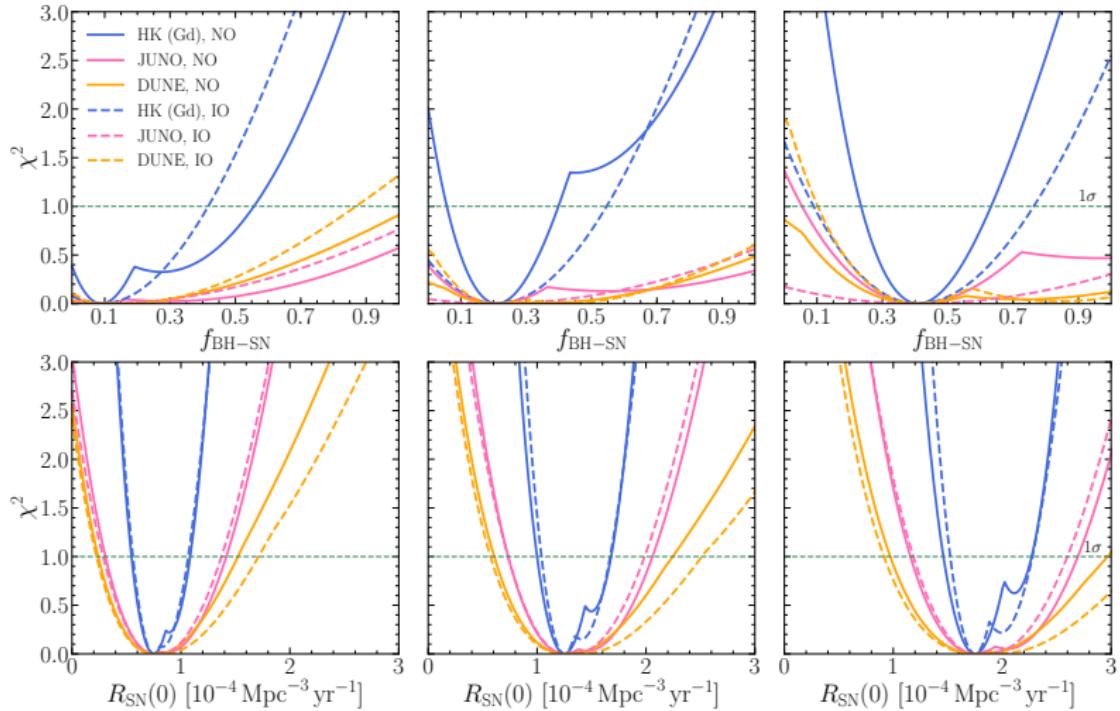
proton - proton chain reactions, i.e.,



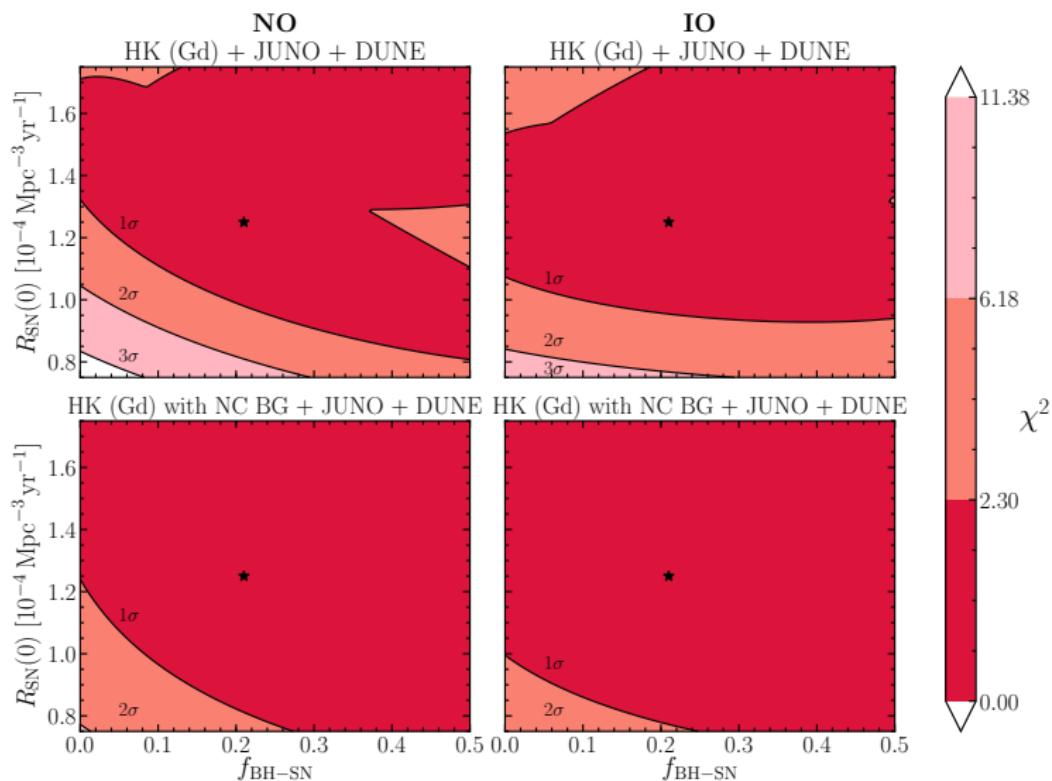
## Assumed uncertainties:

- $\Delta_{R_{\text{SN}}(0)} = 0.25 \times 10^{-4} \text{ Mpc}^{-3} \text{ yr}^{-1}$
  - $\Delta_{f_{\text{BH-SN}}} = 0.2$
  - $\Delta_{\text{BG}} = 20\%$
  - $\Delta\sigma_{\text{LAr}} = 15\%$
- Pull terms:  $\chi_{\text{BG}}^2 = \left( \frac{x}{\Delta_{\text{BG}}} \right)^2$ ,
- $$\chi_{R_{\text{SN}}(0)}^2 = \left( \frac{R_{\text{SN}}(0) - \bar{R}_{\text{SN}}(0)}{\Delta_{R_{\text{SN}}(0)}} \right)^2$$

# Expected 1D $\chi^2$ as a function of $f_{\text{BH-SN}}$ and $R_{\text{SN}}(0)$



# $\chi^2$ for the fraction of BH forming progenitors - local supernova rate plane



# Number of events in HK (Gd) energy window

