Evaluate the following limits:

1. 
$$\lim_{x\to\infty} \left(\frac{(1+\frac{1}{x})^x}{e}\right)^x$$

2. 
$$\lim_{x\to\infty} x^{\frac{1}{x}}$$

3. 
$$\lim_{x\to 0} x^x$$

4. 
$$\lim_{x\to 0} -x^x + x^{x^x}$$

5. 
$$\lim_{x\to 0} \frac{x^2 \sin(\frac{1}{x}) + x}{(1+x)^{\frac{1}{x}} - e}$$