

ASTR3010 — 08/17

Calculating FOV: Review

→ we can use the following formula to compute the true field of view:

$$\text{field of view} = \frac{\text{apparent field of view}}{\text{magnification}} \quad \left. \vphantom{\frac{\text{apparent field of view}}{\text{magnification}}} \right\} \text{usually provided by manufacturer}$$

• apparent FOV:

↳ eyepieces have apparent FOVs: number of degrees of sky your eyepiece would show if held directly up to sky.

→ not always specified!

→ a decent assumption for cheap scopes is 50° .

• true field of view:

↳ number of degrees visible when eyepiece is used with telescope.

→ given by dividing A_{FOV} by the magnification the eyepiece provides when used with the telescope.

• magnification:

↳ recall: we can compute the combined eyepiece—telescope magnification as follows—

$$m_{\text{net}} = \frac{\text{focal length of telescope}}{\text{focal length of eyepiece}}$$

→ we can alternatively use a different formula:

$$\text{field of view} = 2 \cdot \arctan\left(\frac{r}{f_{\text{telescope}}}\right) \quad \left. \vphantom{\frac{r}{f_{\text{telescope}}}}} \right\} \begin{array}{l} r = \text{radius of field stop/aperture of eyepiece} \\ f_t = \text{telescope focal length} \end{array}$$

→ equipment information:

• Celestron Firstscope

↳ $f_{\text{telescope}} = 300\text{mm}$

→ highest mag = $180\times$

→ lowest mag = $11\times$

• Eyepiece 1

↳ $f_{e1} = 20\text{mm}$

→ $\text{mag}_{e1} = 15\times$

→ $\text{AFOV} = 52^\circ$

• Eyepiece 2

↳ $f_{e2} = 4\text{mm}$

→ $\text{mag}_{e2} = 75\times$

→ $\text{AFOV} = 50^\circ$

• Wide Angle Eyepiece

↳ $f_w = 23\text{mm}$

→ $\text{AFOV} = 62^\circ$

→ FOV of telescope & eyepiece 1:

$$m_{\text{net}} = \frac{f_t}{f_{e1}} = \frac{300\text{mm}}{20\text{mm}} = 15\times$$

$$\text{FOV}_{t,e1} = \frac{\text{AFOV}_{e1}}{m_{\text{net}}} = \frac{52^\circ}{15} = 3.4\overline{6}^\circ$$

with camera:

$$m_{\text{net}} = 15\times$$

$$\text{effective AFOV} = \frac{\text{TFOV}}{\text{magnification of camera setup}} = 3.4\overline{6}^\circ$$

→ FOV of telescope & eyepiece 2:

$$m_{\text{net}} = \frac{f_t}{f_{e2}} = \frac{300\text{mm}}{4\text{mm}} = 75\times$$

$$\text{FOV}_{t,e2} = \frac{\text{AFOV}_{e2}}{m_{\text{net}}} = \frac{50^\circ}{75} = \frac{2}{3} = 0.\overline{6}^\circ$$

$$\text{eAFOV} = \frac{0.\overline{6}^\circ}{1} = 0.\overline{6}^\circ$$

→ FOV of telescope & eyepiece 3:

$$m_{\text{net}} = \frac{f_t}{f_w} = \frac{300\text{mm}}{23\text{mm}} = \frac{300}{23} \approx 13\times$$

$$\text{FOV}_{t,w} = \frac{\text{AFOV}_w}{m_{\text{net}}} = \frac{62^\circ}{300/23} = \frac{713}{150} = 4.75\overline{3}^\circ$$

$$\text{eAFOV} = \frac{4.75\overline{3}^\circ}{1} = 4.75\overline{3}^\circ$$

→ we must also consider how my smartphone camera may affect this process:

• iPhone 14 Pro

$$\hookrightarrow f_{\text{cam}} = 24\text{mm} \quad (\text{main lens has 24mm equivalent focal length})$$

$$\rightarrow \text{mag}_{\text{cam}} = 1$$

→ 48MP type $1/1.28$ ($9.8 \times 7.3\text{mm}$) camera sensor

$$\therefore \text{AFOV}_{\text{cam}} = 28.57^\circ$$

• we also need the FOV of the camera:

$$\text{FOV} = 2 \arctan\left(\frac{H}{2f}\right) \quad \left. \begin{array}{l} H = \text{horiz. dim. of camera sensor} \\ f = \text{focal length} \end{array} \right\}$$

$$\therefore \text{FOV}_{\text{cam}} = 2 \arctan\left(\frac{\sqrt{9.8^2 + 7.3^2}}{2 \cdot 24}\right) \approx 28.57^\circ$$

→ converting our measurements to arcseconds:

• recall — $1\text{deg} = 3600\text{ arcsec}$

$$\therefore \text{FOV}_1 = 3.4\overline{6}^\circ \cdot 3600\text{ arcsec/degree} \approx 12,492''$$

$$\text{FOV}_2 = 0.\overline{6}^\circ \cdot 3600\text{ arcsec/degree} \approx 2,112''$$

$$\text{FOV}_3 = 4.75\overline{3}^\circ \cdot 3600\text{ arcsec/degree} \approx 17,100''$$

→ lastly, we must compute the pixel scaling:

$$\text{pixel scale} = \frac{\text{FOV}}{\text{no. of pixels across sensor}} \quad \longrightarrow \text{computed above}$$

↳ 48,000,000 pixels total in a 4:3 default aspect ratio means:

$$\bullet \text{ horiz. pixels} = \sqrt{\frac{48 \text{ mp} \cdot 4}{3}} \cdot \frac{4}{\sqrt{4^2 + 3^2}} \approx 8064 \text{ pixels}$$

$$\therefore \text{pixel scale}_1 = \frac{12,492''}{8064 \text{ px}} \approx 1.55 \text{ arcsec/pixel}$$

$$\text{pixel scale}_2 = \frac{2,412''}{8064 \text{ px}} \approx 0.30 \text{ arcsec/pixel}$$

$$\text{pixel scale}_3 = \frac{17,100''}{8064 \text{ px}} \approx 2.12 \text{ arcsec/pixel}$$