Convention-formation in iterated reference games

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Abstract

What cognitive mechanisms support the emergence of linguistic conventions from repeated interaction? We present results from a large-scale, multi-player replication of the classic *tangrams task* which demonstrate three key empirical signatures constraining theories of convention-formation: arbitrariness, stability, and reduction of utterance length over time. These results motivate a theory of convention-formation where agents, though initially uncertain about word meanings in context, assume others are using language with such knowledge. Thus, agents may learn about meanings by reasoning about a knowledgeable, informative partner; if all agents engage in such a process, they successfully coordinate their beliefs, giving rise to a conventional communication system. We formalize this theory in a computational model of language understanding as social inference and demonstrate that it produces all three signatures.

Keywords: conventions; pragmatics; communication

Introduction

Just as drivers depend on shared behavioral conventions to safely navigate traffic, successful communication depends on a set of shared linguistic conventions. Speakers of different languages around the world refer to the same object in many different ways, yet when ordering a coffee in San Francisco, I can confidently use the English word "coffee" and assume that I will be understood. How do these conventions – classically characterized by Lewis (1969) as arbitrary but stable solutions to recurring coordination problems – form in the first place?

While *global* conventions adopted and sustained throughout a large population of speakers may develop over longer time scales, we also effortlessly coordinate on *local* conventions – or conceptual pacts (Brennan & Clark, 1996) – within the span of a single dialogue. For example, when discussing possible conditions to use in an upcoming experiment, a team of collaborators might begin the meeting using long descriptions to refer to each condition but end the meeting using conventional terms like "condition A" and "condition B." Since global conventions are hypothesized to emerge through diffuse, repeated interactions of this more local kind (Garrod & Doherty, 1994), the cognitive mechanisms underlying convention-formation in such games are of foundational interest.

In a seminal study by Krauss & Weinheimer (1964), pairs of participants played a cooperative language game where they were presented with arrays of ambiguous shapes in randomized orders. The players were assigned the roles of *director* and *matcher* and allowed to talk freely. The matcher's goal was to rearrange their shapes to match the director's board, and the director's goal was to communicate useful descriptions. Over multiple rounds, descriptions were dramati-

cally shortened: an early description like "upside-down martini glass in a wire stand," became simply "martini" by the end. Later studies (e.g. Clark & Wilkes-Gibbs, 1986) refined this paradigm, using larger arrays of tangram-like figures and emphasizing the intricate back-and-forth process through which speakers and listeners negotiate over references. These studies revealed a number of key empirical signatures that inform theories of convention-formation. Here, we focus on three: arbitrariness, stability, and the systematic reduction of utterance length over time.

Arbitrariness is a definitional property of conventions (Lewis, 1969): there must be multiple solutions that would be equally successful as long as both players "agree" (e.g. driving on the left vs. right side of the road). By the final round in a language game, for example, the same tangram might be called the 'dancer' to one pair and the 'skater' to another. The other definitional property we consider is *stability*: it is in everyone's best interest to keep using the convention, once established. Finally, *reduction* is more specific to the reference game paradigm and refers to the transformation of longer, complex expressions into simpler expressions over the course of interaction, as Krauss & Weinheimer (1964) observed. While this broad phenomenon has been replicated many times, exactly what is reduced remains an open empirical question.

Theories of convention-formation differ primarily in the extent to which sophisticated social reasoning and common ground is required. At one extreme, agents use simple heuristic updating rules and do not need to represent or reason about other agents at all (Barr, 2004; Centola & Baronchelli, 2015; Young, 2015). Simulations elegantly show how arbitrary signaling systems can spread and come to dominate large populations. However, due to their 'rich get richer' dynamic, it is not clear how emergence-through-use mechanisms alone could account for reduction in repeated interaction. At the other extreme, are theories in which agents explicitly consider their partner's beliefs and track what information is mutual knowledge, often formalized in a game theoretic setting (Lewis, 1969). Wilkes-Gibbs & Clark (1992) and others have proposed that agents engage in a collaborative process of establishing mutual knowledge, though the mechanisms allowing conventions to emerge under such conditions have not been instantiated in a formal model to our knowledge.

In this paper, we argue for a theoretical position on the spectrum between these poles: *conventions form when agents assume conventions already exist*. In other words, agents believe there is a true lexicon used by other agents but are initially unsure of its identity. Through their interactions with a partner who is assumed to be knowledgeable and informative,

agents can learn this true lexicon even though their partner in fact begins in the same state of ignorance. Agents thus coordinate on the same lexicon, which becomes conventional.

To support this theory, we first conduct a large-scale, multiplayer replication of the tangrams task, which has traditionally been limited to relatively small sample sizes in the lab. We demonstrate signatures of arbitrariness, stability, and reduction which have been difficult to study at a fine-grained level due to the sparseness of existing data. Next, we formulate our theory in a computational model of communication in repeated reference games, based on recent successes capturing language understanding as social inference (Goodman & Frank, 2016; Goodman & Stuhlmller, 2013) and show that this model qualitatively produces all three empirical signatures.

Replication of tangrams task

To collect a corpus of reference game dialogue that supports more detailed analyses of convention-formation, we ported the tangrams task used in Clark & Wilkes-Gibbs (1986) to a real-time, multi-player web environment.

Methods

Participants 200 participants were recruited from Amazon's Mechanical Turk and paired into dyads to play a real-time communication game using the framework in Hawkins (2015). We excluded games that terminated before the completion of 6 rounds and where participants reported a native language different from English, leaving a corpus of X complete games with a total of Xutterances.

Stimuli On every trial of the game, both participants were shown a 6×2 grid containing twelve tangram shapes, reproduced from Clark & Wilkes-Gibbs (1986). Cells were labeled with fixed numbers from one to twelve in order to help participants easily refer to locations in the grid (see Fig. ??).

Procedure After passing a short quiz about task instructions, participants were randomly assigned the role of either 'director' or 'matcher' and automatically paired into virtual rooms containing a chat box and grid of stimuli. Both participants could freely use the chat box to communicate at any time. The director's tangrams were fixed in place, but the matcher could click and drag the shapes to reorder them. The director had to send messages about the locations of different tangrams on their fixed board (e.g. "#1 looks like an X", "2 is the one with the Y"); the matcher had to identify the corresponding tangram shapes and move them to the correct locations. When the players were satisfied that their boards matched, the matcher clicked a 'submit' button that gave players feedback on their score (out of 12) and scrambled the tangrams for the next round. After six rounds, players were redirected to a short exit survey. We collected the raw text of every message sent and every swapping action taken by the matcher.

Results

Arbitrariness and stability We begin by examining signatures of *arbitrariness* and *stability* in our data. We operationalize these concepts using the information-theoretic measure of entropy:

$$H(W) = \sum_{w} P(w) \log P(w)$$

Broadly speaking, entropy measures the predictability of a distribution. It is maximized when all elements are equally likely and declines as the distribution becomes more structured, i.e. when the probability mass is concentrated on a subset of elements.

To derive predictions, we consider a permutation-test null model in which utterances are scrambled within each round. The empirical entropy of individual games should only differ from the null distribution if *both* arbitrariness and stability hold. First, note that if stability did *not* hold, scrambling would have no effect on the entropy within individual games: speakers would already use different words each round, and swapping out the identity of those words would not affect the entropy of the word distribution.

If stability holds but arbitrariness does not, all players would adopt the single optimal (non-arbitrary) way to refer to each tangram. Therefore, the entropy of their word distributions also should not be affected by scrambling: a speaker's real words would be swapped out for the same words, just generated by another speaker. Finally, if both arbitrariness and stability hold, then different speakers adopt different referring expressions that persist from round to round. Hence, scrambling should *increase* the average game's entropy from a relatively low level: each game's idiosyncratic, concentrated distribution of words would be mixed together to form more heterogeneous and therefore high-entropy distributions.

To test this prediction, we computed the average withingame entropy for 1000 different permutations of speaker utterances. We permuted utterances within rounds rather than across the entire data set to control for the fact that earlier rounds have longer utterances and thus a larger vocabulary than later rounds (see the following section). Since this permutation scheme keeps the number of messages per participant constant and simply swaps out the content of those messages, it also controls for the fact that some speakers sent more messages than others. We found that our null distribution lay within the interval [X, Y], which is significantly higher than the true entropy (averaged across games) of Z p < 0.001. This pattern is consistent only with signatures of both arbitrariness and stability.

Reduction Next, we turn to a set of analyses examining reduction in utterance length over the course of the experiment. At the coarsest level, we find that the mean number of words used by speakers decreases over time (see Fig. ??). This decrease replicates a highly reliable reduction effect found throughout the literature on iterated reference games (Brennan & Clark, 1996; Krauss & Weinheimer, 1964), although perhaps due to our purely textual (vs. spoken) interface, par-

ticipants in our task used many fewer words overall than previously reported. The following analyses break down this broad reduction into a finer-grained set of phenomena.

The next level of granularity motivating our model approach concerns which kinds of words are most likely to be dropped. Is the speaker adopting a shorthand where they drop uninformative function words, or are they simplifying or narrowing their descriptions by omitting meaningful details (Clark & Wilkes-Gibbs, 1986)? We used the Stanford CoreNLP part-of-speech tagger (Toutanova, Klein, Manning, & Singer, 2003) to count the number of words belonging to each part of speech in each message. Fig. ?? shows the percent reduction of different parts of speech from the first round to the sixth round. We find that determiners ('the', 'a', 'an') are the most likely class of words to be dropped with an X% reduction rate, on average. Nouns ('dancer', 'rabbit') are the least likely class to be dropped with only an Y\% rate. Closedclass parts of speech are strictly more likely to be dropped than open-class parts of speech.

While this finding suggests that speakers might just be adopting a shorthand using more ungrammatical fragments as the game proceeds, we find a more complex dynamic by examining the table of unigrams and bigrams most likely to be dropped (see Table ??). Note that alongside dropped articles, there are a number of words that form conjunctions ('and') and modifiers ('of', 'with', 'the right'). In other words, it may be more likely that when function words are dropped, it is primarily as part of larger grammatical units that provide additional information in identifying the target.

We explicitly examined this hypothesis by running the Stanford constituency parser (Schuster & Manning, 2016), tagging the occurrence of subordinate/adverbial clauses ('sitting facing left') and adjectival clauses ('angel that is praying').¹ We found that both were reduced over the course of the game (see Fig. ??), lending additional support for the hypothesis that meaningful details are increasingly omitted. Initial phrases pile on multiple ambiguous, partially redundant modifiers and descriptors: as the game progresses and ambiguity of reference decreases, these additional meaningful units become less useful and can be dropped.

Listener feedback Finally, the theory proposed by Clark & Wilkes-Gibbs (1986) argues that lexical conventions are established through a collaborative process requiring both speaker and listener input. This predicts that (1) listener feedback should be highest on the first round and drop off once meanings are agreed upon, and (2) dyads with more initial listener feedback should converge on more efficient conventions. We find correlational evidence of both patterns in our data. The number of listener messages decreases significantly over the game (t = -13.23, see Fig. ??), and there is a weak but significant effect of initial listener messages on overall reduction (X).

Model

Here, we present a probabilistic model of language production under uncertainty, which captures several of the signature properties of conventions shown above. This model belongs to the family of Rational Speech Act (RSA) models, which have been successful in explaining a wide range of linguistic phenomena - including scalar implicature, adjectival vagueness, overinformativeness, indirect questions, and nonliteral language use – as arising from a process of recursive social reasoning. Most previous applications of RSA have focused on the listener's problem of language comprehension, but the puzzle of conventionalization is primarily a question of speaker production. An nth order pragmatic speaker trying to convey a particular state of affairs $s \in \mathcal{S}$ assuming lexicon \mathcal{L} is assumed to select an utterance $u \in \mathcal{U}$ by trading off its expected informativity (with respect to a rational listener agent) against its cost, usually based on length (Goodman & Frank, 2016):

$$S_n(u|s, \mathcal{L}) \propto \exp(\alpha \log L_n(s|u, \mathcal{L}) - \cos(u))$$

where α is an optimality parameter controlling the extent to which the speaker maximizes over the expected listener distribution. The listener, in turn, reasons about what utterances would be most likely to be produced by a speaker intending to convey u:

$$L_n(s|u,\mathcal{L}) \propto P(s)S_{n-1}(u|s,\mathcal{L})$$

This recursion bottoms out in a *literal listener* who directly looks up the meaning of the utterance in the lexicon:

$$L_0(s|u, \mathcal{L}) \propto \mathcal{L}(u, s) \cdot P(s)$$

As in several other recent applications of RSA (Graf, Degen, Hawkins, & Goodman, 2016), we use a graded semantics, where utterances are better or worse descriptions of particular referents. For instance, the utterance "dancer" may initially be expected to apply to a photorealistic image of a ballerina ($\mathcal{L}(\text{'dancer'}, ballerina) = 0.99$) more than an abstract image of one ($\mathcal{L}(\text{'dancer'}, abstract ballerina) = 0.6$), but apply to both better than a non-category member like an image of a dog ($\mathcal{L}(\text{'dancer'}, dog) = 0.05$).

Our approach to convention-formation begins with the additional assumption of *lexical uncertainty* (Bergen, Levy, & Goodman, 2016; Smith, Goodman, & Frank, 2013). In other words, we assume that instead of having perfect knowledge of \mathcal{L} , the speaker has uncertainty over the exact meanings of lexical items in the current context (i.e. it is initially unclear which of the ambiguous tangram shapes "the dancer" might refer to). They begin with some prior $P(\mathcal{L})$ over meanings, which may be initially biased toward certain meanings, and update these beliefs through repeated interactions with a knowledgeable partner:

$$P(\mathcal{L}|d) \propto P(\mathcal{L}) \prod_{i} L_{n-1}(s_i|u_i,\mathcal{L})$$

¹Specifically, we used the Universal Dependencies tags csubj, ccomp, xcomp, and advcl for subordinate clauses and acl for adjectival clauses (Schuster & Manning, 2016)

where $d = \{s_i, u_i\}$ is a set of observations of s_i and u_i coming from previous exchanges². The speaker then marginalizes over this posterior distribution when reasoning about the listener, giving rise to the form of the pragmatic listener model we use throughout our model results (only going up to n = 2 in our recursion for simplicity):

$$S(u|s,d) \propto \exp(\alpha \log \left(\sum_{\mathcal{L}} P(\mathcal{L}|d) L_1(s|u,\mathcal{L})\right) - \cos(u))$$

A listener with lexical uncertainty can be defined similarity, simply swapping out L_{n-1} in the lexicon posterior update with a knowledgeable speaker S_n :

$$L(s|u,d) \propto \sum_{\mathcal{L}} P(\mathcal{L}|d) L_1(s|u,\mathcal{L})$$

This model is implemented in the probabilistic programming language WebPPL (Goodman & Stuhlmller, electronic).³ Following Smith et al. (2013), we begin by showing how a random initial choice is taken to be evidence for a particular lexicon and becomes the base for successful communication even though neither party knows its meaning at the outset.

Results

Arbitrariness and stability Consider an environment with two abstract shapes $(\{s_1, s_2\})$, where the speaker must choose between two utterances $(\{u_1, u_2\})$ incurring equal cost. Their prior $P(\mathcal{L})$ over the meaning of each utterance is given by a (discretized) Dirichlet distribution, so on the first round both utterances are equally likely to apply to either shape. If the speaker was trying to get their partner to pick s_1 , then, since each utterance is equally (un)informative, they would randomly sample one (say, u_1), and observe the listener's selection of a shape (say, s_1). On the next round, the speaker uses the observed pair $\{u_1, s_1\}$ to update their beliefs about the lexicon, uses these beliefs to generate a new utterance, and so on. To examine expected dynamics over multiple rounds, we enumerate over all possible trajectories our simulated speaker and listener models could produce.

We observe several important qualitative effects in our simulations. First, the fact that a knowledgeable listener responds to utterance u with s provides evidence for lexicons in which u is a good fit for s, hence the likelihood of the speaker using u to refer to s increases on subsequent rounds (see Fig.??). In other words, the initial symmetry between the meanings can be broken by initial random choices, leading to completely arbitrary but stable mappings in future rounds. Second, because the listener is also learning the lexicon from these observations under the same set of assumptions, they converge

on a shared set of meanings; hence, expected *accuracy* rises on future rounds (see Fig. ??). Third, because one's partner is assumed to be pragmatic, agents can also learn about *unheard* utterances: observing $\{u_1, s_1\}$ also provides evidence for lexicons in which u_2 is a good fit for s_2 by standard Gricean reasoning. Finally, *failed references* lead to conventions just as effectively as successful references: if the speaker intends s_1 and says u_1 , but then the listener incorrectly picks s_2 , the speaker will take this as evidence that u_1 actually means s_2 and use it that way on subsequent rounds.

Reduction in utterance length Finally, we show how our model explains reduction of utterance length over multiple interactions. For utterances to be reduced, of course, they must vary in length. Motivated by our empirical observation that meaningful clauses are the primary unit of reduction, we extend our grammar to include *conjunctions*. This is one of the simplest ways to constructing longer utterances compositionally from lexical primitives, using the product rule:

$$\mathcal{L}(u_i \text{ and } u_i, o) = \mathcal{L}(u_i, o) \times \mathcal{L}(u_i, o)$$

Analogous to our tangram stimuli, which have many ambiguous features and figurative perspectives that may be evoked in speaker descriptions, we consider a simplified scenario where speakers can refer to two different features of the two objects $\{o_1,o_2\}$. The speaker has four primitive words at their disposal – two words for shape $(\{u_{s1},u_{s2}\})$ and two for color $\{u_{c1},u_{c2}\}$ – and has uncertainty over the initial meanings of all four.

While we established in the previous section that conventions can emerge over a reference game in the complete absence of initial preferences, players often bring such preferences to the table. A player who hears 'ice skater' on the first round of our tangrams task is more likely to select some objects more than others, even though they still have some uncertainty over its meaning in the context. To show that our model can accommodate this fact, we allow the speaker's initial prior meanings to be slightly biased. u_{s1} and u_{c1} are more likely to mean o_1 ; u_{s2} and u_{c2} are more likely to mean o_2 .

We ran 1000 forward samples of 6 rounds of speaker-listener interaction, and averaged over the utterance length at each round.⁴ Our results are shown in Figure ??: the expected utterance length decreases systematically over each round. To illustrate in more detail how this dynamic is driven by an initial rational preference for redundancy relaxing as reference becomes more reliable, we walk step-by-step through a single trajectory.

Consider a speaker who wants to refer to object o_1 . They believe their knowledgeable partner is slightly more likely to interpret their language using a lexicon in which u_{s1} and u_{c1} apply to this object, due to their initial bias. However, there is still a reasonable chance that one or the other alone actu-

²There is a broader debate over the timescales at which lexicons and lexicon learning mechanisms operate; here, we assume a discourse-level structure to the lexicon, where there is uncertainty over how words are used *in the given conversation*. See Frank, Goodman, & Tenenbaum (2009) for a related approach at the scale of cross-situational word learning.

³All results can be reproduced running our code in the browser at http://forestdb.org/models/conventions.html

 $^{^4}$ In our simulations, we used $\alpha=13$ and found the basic reduction effect over a range of different biases, with different intercepts and slopes

ally refers strongly to o_2 in the true lexicon. Thus, it is useful to produce the conjunction " u_{s1} and u_{c1} " to hedge against this possibility, despite its higher cost. Upon observing the listener's response (say, o_1), the evidence is indeterminate about the separate meanings of u_{s1} and u_{c1} but both become increasingly likely to refer to o_1 . In the trade-off between informativity and cost, the shorter utterances remain probable options. Once the speaker chooses one of them, the symmetry collapses and that utterance remains most probable in future rounds. In this way, meaningful sub-phrases are omitted over time as the speaker becomes more confident about the true lexicon.

General Discussion

In this paper, we revisited the classic phenomenon of convention-formation in a large-scale replication of the tangrams task, finding evidence of arbitrariness and stability as well as finer-grained reduction of meaningful clauses. We argued that several empirical signatures including arbitrariness, stability, and the reduction of utterance length over repeated interactions can be explained by our model of informative communication under lexical uncertainty. This model formalizes a theory where conventions emerge via initially uncertain agents assuming that conventions are already in place and inferring them by reasoning about a knowledgeable, informative partner.

Theories of convention-formation vary in the extent to which social reasoning about common ground is required. Our agents lie on a spectrum between the heuristic updating agents of Barr (2004) and the sophisticated agents of Clark & Wilkes-Gibbs (1986), who collaboratively build up explicit representations of mutual knowledge. Speakers and listeners in our model implicitly coordinate their beliefs through a shared history of observations, which serves as "common ground" in an informal sense. They make critical use of pragmatic, social reasoning in order to learn meanings, but do not explicitly consider the fact that this history is shared, or represent their partner's own uncertainty.

By capturing reduction, which purely heuristic theories have not yet demonstrated, we showed that minimal assumptions of social reasoning go a long way in accounting for key phenomena. Still, our model falls short in some ways. For instance, because we do not provide a mechanisms for the listener agent to respond with confirmation, repair, or followup questions, we cannot make explicit predictions about the reduction in listener messages (as in Fig. ??) or the impact of early listener responses on conventionalization. These phenomena require our model to deal with planning over extended dialogues, and to potentially weaken the assumption that one's partner knows the true lexicon with complete certainty. Similarly, while our model was explicitly designed with linguistic conventions in mind, it remains to be seen whether the same formulation generalizes to broader behavioral conventions. For example, the real-time coordination games used in Hawkins & Goldstone (2016) may not require players to reason about a structured lexicon with noise, but an action policy representation may play a similar role. While there remain many complex aspects of convention-formation in communication games left for future research, our approach nonetheless serves as a lower bound on the degree of social reasoning needed to capture lexical conventions in these games.

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