## **Principal Components Analysis**

#Abstract This contribution develops an analysis on the dataset 'bad-drivers.csv' (taken from github.com/fivethirtyeight/data) by running the Principal Components Analysis. In particular, the study is focused on the different steps in the computation of the principal componets.

1. How to choose Principal Components 2. Proportion Variance Explained 3. Thanks to this it is now possible to consider just three of the principal components, always keeping in mind that the goal is to lower the cross-validation risk estimate. #Description of the dataset I chose the dataset 'bad-drivers.csv' (taken from github.com/fivethirtyeight/data), that considers data whose sources are: National Highway Traffic Safety Administration and National Association of Insurance Commissioners. This folder contains data behind the story 'Dear Mona, Which State Has The Worst Drivers?', where Mona Chalabi, a British data journalist answer some questions about drivers and car accidents in the USA. She says that historic data that could indicate where America's worst drivers are: the number of car crashes in each state (especially those where the driver was negligent in some way), how much insurance companies pay out, and how much insurance companies charge drivers. The reported variables are: . State (a specific country in the USA); . Number of drivers involved in fatal collisions per billion miles; . Percentage of drivers involved in fatal collisions who were speeding; . Percentage of drivers involved in fatal collisions who were alcohol impaired; . Percentage of drivers involved in fatal collisions who were not distracted; Percentage of drivers involved in fatal collisions who had not been involved in any previous accidents; . Car insurance premiums; . Losses incurred by insurance companies for collisions per insured driver. I chose to compute the predictions on the variable 'Losses incurred by insurance companies for collisions per insured driver' (variable y).

##Analysis The Principal Component Analysis is one of the unsupervised learning methods and, as all unsupervised methods, it is much more challenging than supervised learning: in fact, it is often performed as an exploratory data analysis, whose goal is to check if there exist a possible dimension of the dataset in which I can study my data and see the relation between the variables. My goal here is to find a low-dimension representation of the dataset by defining the principal components. First of all, I imported the dataset, renamed all the columns and chose not to consider the first column of the dataset in order to make it easier to do the whole analysis. These are the first fifteen rows as example:

```
\label{lem:condition} a <-\ bad\_drivers Number. of. drivers. involved. in. fatal. collisions. per. billion. miles b <-bad\_drivers Percentage. Of. Drivers. Involved. In. Fatal. Collisions. Who. Were. Alcohol. Impaired d<<-br/>
```

bad drivers <- data.frame(a,b,c,d,e,f,g) bad drivers

n <- nrow(bad drivers) #number of rows p <- ncol(bad drivers) #number of columns

## mean and std:

mean <- colMeans(bad\_drivers) std <- apply(bad\_drivers, 2, sd) table <- round(cbind(mean, std),2) table

 $<sup>-</sup>bad_drivers$ Percentage.Of.Drivers.Involved.In.Fatal.Collisions.Who.Were.Not.Distracted e <- bad\_driversPercentage.Of.Dri $-bad_drivers$ Car.Insurance.Premiums.... g <- bad\_drivers\$Losses.incurred.by.insurance.companies.for.collisions.per.insured.dr

## PCA starting from correlation matrix

#### calculate matrix R:

corr <- cor(bad\_drivers) round(corr,3)

## calculate eigenvalues and eigenvectors:

eigen(corr) eigenvalues <- eigen(corr) values eigenvectors <- eigen(corr) vectors

# Dall'analisi degli autovalori, le uniche componenti principali di rilevanza

#sono la prima e la seconda (le altre, infatti, hanno autovalori, quindi varianza, #minori di 1). Vediamo cosa accade se si sceglie il numero di componenti principali #sulla base della percentuale di # varianza spiegata: pvarsp = eigenvalues/p pvarspcum = cumsum(pvarsp) tab <- round(cbind(eigenvalues,pvarsp100,pvarspcum100),2) colnames(tab)<-c("eigenvelues", "% variance", "% cum variance") tab

## Use Scree Diagram to select the components:

plot(eigenvalues, type="b", main="Scree Diagram", xlab="Number of Component", ylab="Eigenvalues") abline(h=1, lwd=3, col="red")

#### We select 4 components

# Interpret the principal components selected by their coefficient vectors:

eigen(corr)\$vectors[,1:4]

#Matrix of the components, obtained by multiplying the eigenvector by the root of the respective eigenvalue (if necessary we can change the sign for interpretative reasons) comp <-round(cbind(-eigen(rho)vectors[, 1] \* sqrt(eigenvalues[1]), -eigen(rho)vectors[, 2]sqrt(eigenvalues[2]), -eigen(rho)vectors[, 3]\*sqrt(eigenvalues[3]), -eigen(rho)vectors[, 3]\*sqrt(eigenvalues[3]), -eigen(rho)vectors[, 3]\*sqrt(eigenvalues[3]), -eigen(rho)vectors[, 3]\*sqrt(eigenvalues[4])), rownames(comp)<-rownames(table) colnames(comp)<-c("Comp1", "Comp2", "Comp3", "Comp4") comp

# The sum of the squares of the values of each row of the component

#matrix is the respective 'communality', # The communality is the sum of the squared component loadings #up to the number of components you extract. communality<-comp[,1] $^{2+\text{comp}[,2]}2+\text{comp}[,3]^{2+\text{comp}[,4]}2$  comp<-cbind(comp,communality) comp

# Calculate the scores for the selected components and graph them:

bad\_drivers.scale <- scale(bad\_drivers, T, T) score <- bad\_drivers.scale%\*%autovec[,1:4] # normalized scores changed sign (non-normalized scores divided by #square root of the respective eigenvalue) ## score chart scorez<-round(cbind(-score[,1]/sqrt(eigenvalues[1]),-score[,2]/sqrt(eigenvalues[2]),-score[,3]/sqrt(eigenvalues[3]),-score[,4]/sqrt(eigenvalues[4])),4) plot(scorez, main="Scores plot") text(scorez, rownames(bad\_drivers)) abline(v=0,h=0,col="red") # Loadings plot plot(comp[,1:4], main="Loadings plot", xlim=range(-1,1)) text(comp, rownames(comp)) abline(v=0,h=0,col="red")