

Distribution	PDF	Mean	Variance	MGF
Binomial	$p(y) = \binom{n}{y} p^y (1-p)^{n-y}, y = 0, 1, \dots, n$	np	$np(1-p)$	$[pe^t + (1-p)]^n$
Geometric	$p(y) = p(1-p)^{y-1}, y = 1, 2, \dots$	$\frac{1}{p}$	$\frac{1-p}{p^2}$	$\frac{pe^t}{1-(1-p)e^t}$
Hypergeometric	$p(y) = \frac{\binom{r}{y} \binom{N-r}{n-y}}{\binom{N}{n}}, y = 0, 1, \dots$	$\frac{nr}{N}$	$n \frac{r}{N} \frac{N-r}{N} \frac{N-n}{N-1}$	DNE in closed form
Poisson	$p(y) = \frac{\lambda^y e^{-\lambda}}{y!}, y = 0, 1, 2, \dots$	λ	λ	$e^{\lambda(e^t-1)}$
Negative Binomial	$p(y) = \binom{y-1}{r-1} p^r (1-p)^{y-r}, y = r, r+1, \dots$	$\frac{r}{p}$	$\frac{r(1-p)}{p^2}$	$\left[\frac{pe^t}{1-(1-p)e^t} \right]^r$
Uniform	$f(y) = \frac{1}{\theta_2 - \theta_1}$	$\frac{\theta_1 + \theta_2}{2}$	$\frac{(\theta_2 - \theta_1)^2}{12}$	$\frac{e^{t\theta_2} - e^{t\theta_1}}{t(\theta_2 - \theta_1)}$
Normal	$f(y) = \frac{1}{\sigma\sqrt{2\pi}} e^{-\frac{(y-\mu)^2}{2\sigma^2}}$	μ	σ^2	$e^{\mu t + \frac{t^2 \sigma^2}{2}}$
Exponential	$f(y) = \frac{1}{\beta} e^{-y/\beta}$	β	β^2	$(1 - \beta t)^{-1}$
Gamma	$f(y) = \frac{y^{\alpha-1} e^{-y/\beta}}{\Gamma(\alpha) \beta^\alpha}$	$\alpha\beta$	$\alpha\beta^2$	$(1 - \beta t)^{-\alpha}$
Chi-square	$f(y) = \frac{y^{v/2-1} e^{-y/2}}{2^{v/2} \Gamma(v/2)}$	v	$2v$	$(1-2t)^{-v/2}$
Beta	$f(y) = \left[\frac{\Gamma(\alpha+\beta)}{\Gamma(\alpha)\Gamma(\beta)} \right] y^{\alpha-1} (1-y)^{\beta-1}$	$\frac{\alpha}{\alpha+\beta}$	$\frac{\alpha\beta}{(\alpha+\beta)^2(\alpha+\beta+1)}$	DNE in closed form

Some Relevant Distribution Relationships Assume Y_i are i.i.d, $i = 1, 2, \dots, n$, and $Y_i \sim \text{Normal}(\mu, \sigma^2)$

$$\bar{Y} = \frac{1}{n} \sum_{i=1}^n Y_i, \quad Z = \frac{\bar{Y} - \mu}{\sigma/\sqrt{n}} \sim \text{Normal}(0, 1), \quad \sum_{i=1}^n \left(\frac{Y_i - \mu}{\sigma} \right)^2 \sim \chi_{(n)}^2, \quad \chi_{(n)}^2 = \text{Gamma}(n/2, 2)$$

$$\frac{(n-1)S^2}{\sigma^2} = \sum_{i=1}^n \frac{(Y_i - \bar{Y})^2}{\sigma^2} \sim \chi_{(n-1)}^2, \quad S^2 = \frac{1}{n-1} \sum_{i=1}^n (Y_i - \bar{Y})^2$$

$$t_v = \frac{Z}{\sqrt{W/v}} \text{ where } Z \sim \text{Normal}(0, 1), W \sim \chi_{(v)}^2, \text{ and } Z, W \text{ are independent}$$

$$F_{v_1, v_2} = \frac{W_1/v_1}{W_2/v_2} \text{ where } W_1 \sim \chi_{(v_1)}^2, W_2 \sim \chi_{(v_2)}^2 \text{ and } W_1, W_2 \text{ are independent, } F_{n_1-1, n_2-1} \sim \frac{S_1^2/\sigma_1^2}{S_2^2/\sigma_2^2}$$

$$\text{Exp}(\beta) = \text{Gamma}(\alpha = 1, \beta), \quad (\text{Normal}(0, 1))^2 = \chi_{(1)}^2 = \text{Gamma}(1/2, 2)$$

$$\mu = np, \sigma = \sqrt{np(1-p)}$$

$$Y_{(1)} = \min(Y_1, Y_2, \dots, Y_n) \quad f_{Y_{(1)}}(y) = n[1 - F_{Y_i}(y)]^{n-1} f_{Y_i}(y), \quad Y_{(n)} = \max(Y_1, Y_2, \dots, Y_n) \quad f_{Y_{(n)}}(y) = n[F_{Y_i}(y)]^{n-1} f_{Y_i}(y)$$

Derived Confidence Intervals

Large Sample C.I for p and μ :

$$\hat{p} \pm Z_{\alpha/2} \sqrt{\frac{\hat{p}(1-\hat{p})}{n}}, \quad \bar{Y} \pm Z_{\alpha/2} \frac{S}{\sqrt{n}}$$

Large Sample C.I for $\mu_1 - \mu_2$ and $p_1 - p_2$:

$$\bar{Y}_1 - \bar{Y}_2 \pm Z_{\alpha/2} \sqrt{\frac{S_1^2}{n_1} + \frac{S_2^2}{n_2}}, \quad (\hat{p}_1 - \hat{p}_2) \pm z_{\alpha/2} \sqrt{\frac{\hat{p}_1(1-\hat{p}_1)}{n_1} + \frac{\hat{p}_2(1-\hat{p}_2)}{n_2}}$$

Small Sample C.I for μ :

$$\bar{Y} \pm t_{\alpha/2} \left(\frac{S}{\sqrt{n}} \right) \quad \text{where } t \text{ has } (n-1) \text{ df}$$

Small Sample C.I for $\mu_1 - \mu_2$:

$$(\bar{Y}_1 - \bar{Y}_2) \pm t_{\alpha/2} S_p \sqrt{\frac{1}{n_1} + \frac{1}{n_2}} \quad \text{where } t \text{ has } (n_1 + n_2 - 2) \text{ df} \quad S_p^2 = \frac{(n_1 - 1)S_1^2 + (n_2 - 1)S_2^2}{n_1 + n_2 - 2}$$

C.I for σ^2 :

$$\left(\frac{(n-1)S^2}{\chi_{\alpha/2}^2}, \frac{(n-1)S^2}{\chi_{1-\alpha/2}^2} \right) \quad \text{where } \chi^2 \text{ has } (n-1) \text{ df}$$

$$\text{Large-Sample Test for Mean: } Z = \frac{\bar{Y} - \mu_0}{S/\sqrt{n}}$$

	Alternative Hypothesis	Reject Region for Level α Test (Related to Standard Normal)
Upper-Tailed Test	$H_a : \mu > \mu_0$	$Z \geq Z_\alpha$
Lower-Tailed Test	$H_a : \mu < \mu_0$	$Z \leq -Z_\alpha$
Two-Tailed Test	$H_a : \mu \neq \mu_0$	$Z \geq Z_{\alpha/2} \text{ or } Z \leq -Z_{\alpha/2}$

Large-Sample Test for Proportion: $Z = \frac{\hat{p} - p_0}{\sqrt{p_0(1-p_0)/n}}$

	Alternative Hypothesis	Reject Region for Level α Test (Related to Standard Normal)
Upper-Tailed Test	$H_a : p > p_0$	$Z \geq Z_\alpha$
Lower-Tailed Test	$H_a : p < p_0$	$Z \leq -Z_\alpha$
Two-Tailed Test	$H_a : p \neq p_0$	$Z \geq Z_{\alpha/2}$ or $Z \leq -Z_{\alpha/2}$

Small-Sample Test for Mean: $T = \frac{\bar{Y} - \mu_0}{s/\sqrt{n}}$

	Alternative Hypothesis	Reject Region for Level α Test (Related to T-Distribution)
Upper-Tailed Test	$H_a : \mu > \mu_0$	$T \geq t_{\alpha, n-1}$
Lower-Tailed Test	$H_a : \mu < \mu_0$	$T \leq -t_{\alpha, n-1}$
Two-Tailed Test	$H_a : \mu \neq \mu_0$	$T \geq t_{\alpha/2, n-1}$ or $T \leq -t_{\alpha/2, n-1}$

Small-Sample Test Between 2 Means: $T = \frac{\bar{Y}_1 - \bar{Y}_2 - D_0}{S_p \sqrt{\frac{1}{n_1} + \frac{1}{n_2}}}, \quad S_p = \sqrt{\frac{(n_1 - 1)S_1^2 + (n_2 - 1)S_2^2}{n_1 + n_2 - 2}}$

	Alternative Hypothesis	Reject Region for Level α Test (Related to T-Distribution)
Upper-Tailed Test	$H_a : \mu_1 - \mu_2 > D_0$	$T \geq t_{\alpha, n_1+n_2-2}$
Lower-Tailed Test	$H_a : \mu_1 - \mu_2 < D_0$	$T \leq -t_{\alpha, n_1+n_2-2}$
Two-Tailed Test	$H_a : \mu_1 - \mu_2 \neq D_0$	$T \geq t_{\alpha/2, n_1+n_2-2}$ or $T \leq -t_{\alpha/2, n_1+n_2-2}$

Test for Variance: $\chi^2 = \frac{(n-1)S^2}{\sigma_0^2}$

	Alternative Hypothesis	Reject Region for Level α Test (Related to χ^2 -Distribution)
Upper-Tailed Test	$H_a : \sigma^2 > \sigma_0^2$	$\chi^2 > \chi_{\alpha, n-1}^2$
Lower-Tailed Test	$H_a : \sigma^2 < \sigma_0^2$	$\chi^2 < \chi_{1-\alpha, n-1}^2$
Two-Tailed Test	$H_a : \sigma^2 \neq \sigma_0^2$	$\chi^2 > \chi_{\alpha/2, n-1}^2$ or $\chi^2 < \chi_{1-\alpha/2, n-1}^2$

Test for Equal Variances: $F = \frac{S_1^2}{S_2^2}$

	Alternative Hypothesis	Reject Region for Level α Test (Related to F-Distribution)
Upper-Tailed Test	$H_a : \sigma^2 > \sigma_0^2$	$F > F_{\alpha, n_1-1, n_2-1}$
Lower-Tailed Test	$H_a : \sigma^2 < \sigma_0^2$	$F < F_{1-\alpha, n_1-1, n_2-1}$
Two-Tailed Test	$H_a : \sigma^2 \neq \sigma_0^2$	$F > F_{\alpha/2, n_1-1, n_2-1}$ or $F < F_{1-\alpha/2, n_1-1, n_2-1}$

Least-Squares Estimators for the Simple Linear Regression Model:

$$\hat{\beta}_1 = \frac{S_{xy}}{S_{xx}}, \quad \hat{\beta}_0 = \bar{y} - \hat{\beta}_1 \bar{x}, \quad S_{xy} = \sum_{i=1}^n (x_i - \bar{x})(y_i - \bar{y}) = \sum_{i=1}^n x_i y_i - n(\bar{x})(\bar{y}), \quad S_{xx} = \sum_{i=1}^n (x_i - \bar{x})^2 = \sum_{i=1}^n x_i^2 - n\bar{x}^2,$$

$$V(\hat{\beta}_1) = \frac{\sigma^2}{S_{xx}}, \quad V(\hat{\beta}_0) = \sigma^2 \left(\frac{1}{n} + \frac{\bar{x}^2}{S_{xx}} \right)$$

Linear Regression: Total Sum of Squares, Sum of Squares Error, Sum of Squares Regression

$$SSY = \sum_{i=1}^n (Y_i - \bar{Y})^2 = \sum_{i=1}^n Y_i^2 - n\bar{Y}^2, \quad SSE = \sum_{i=1}^n (Y_i - \hat{Y}_i)^2 = SSY - SS_{\text{reg}}, \quad SS_{\text{reg}} = \sum_{i=1}^n (\hat{Y}_i - \bar{Y})^2 = \hat{\beta}_1 S_{xy} = \hat{\beta}_1^2 S_{xx}$$

One Way ANOVA: Total Sum of Squares, Sum of Squares for Error, Sum of Squares for Treatments

$$n = \sum_{i=1}^k n_i, \quad \bar{Y}_{i\bullet} = \frac{1}{n_i} \sum_{j=1}^{n_i} Y_{ij}, \quad \bar{Y} = \frac{1}{n} \sum_{i=1}^k \sum_{j=1}^{n_i} Y_{ij}, \quad \text{Total } SS = \sum_{i=1}^k \sum_{j=1}^{n_i} (Y_{ij} - \bar{Y})^2 = \sum_{i=1}^k \sum_{j=1}^{n_i} Y_{ij}^2 - n\bar{Y}^2,$$

$$SSE = \sum_{i=1}^k \sum_{j=1}^{n_i} (Y_{ij} - \bar{Y}_{i\bullet})^2 = \sum_{i=1}^k (n_i - 1)S_i^2 = \text{Total } SS - SST, \quad SST = \sum_{i=1}^k n_i (\bar{Y}_{i\bullet} - \bar{Y})^2 = \sum_{i=1}^k n_i \bar{Y}_{i\bullet}^2 - n\bar{Y}^2$$

$$MST = \frac{SST}{k-1}, \quad MSE = \frac{SSE}{n-k}, \quad F = \frac{MST}{MSE}$$