Name and surname:

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## Calculus I - MAC 2311 - Section 001

## The last quiz 04/25/2018

**Instructions:** The total number of points of this quiz is 10. You will get an extra point if you solve correctly the last exercise.

1) [2 points] State the Fundamental Theorem of Calculus (Part 1 and Part 2).

2) a) [1.5 points] Compute the following indefinite integral:

$$\int \frac{5x^6 + 2x^3 - 3x^2}{x^2} + \cos(x) \, dx.$$

b) [1.5 points] Use your previous work for computing

$$\int_{1}^{\pi} \frac{5x^6 + 2x^3 - 3x^2}{x^2} + \cos(x) \, dx.$$

3) [3 points] Let 
$$g(x) = \int_0^{x^3} e^t \sin(t^2) dt$$
. Compute  $g'(x)$ .

3) [2 points] Express the following limit of Riemann sums as a definite integral over the interval [-2, 1]:

$$\lim_{n \to \infty} \sum_{i=1}^{n} \frac{\sin^{2}(x_{i}^{*}) + (x_{i}^{*})^{2}}{\sqrt{x_{i}^{*} + 3}} \Delta x.$$

3) [Bonus] Using Part 2, prove Part 1 of the Fundamental Theorem of Calculus.