



$$\text{parent.grad} += \text{child.grad} * \text{local-deriv}$$

z10.backward()  
 "I want to derivate of z10 with respect to every leaf parameter."

0th iterations

$$z_{10}.\text{grad} = 1 \quad \left( \frac{\partial z_{10}}{\partial z_{10}} = 1 \right)$$

"The output changes at same rate as itself."

$$z_{10} = z_8 * z_9$$

$\downarrow$  relu()       $\hookrightarrow$  wo

$$\frac{\partial z_{10}}{\partial z_8} = z_9 = 6 \quad \frac{\partial z_{10}}{\partial z_9} = z_8 = 22$$

$$z_9.\text{grad} += z_{10}.\text{grad} * \frac{\partial z_{10}}{\partial z_9}$$

$$z_8.\text{grad} += z_{10}.\text{grad} * \frac{\partial z_{10}}{\partial z_8} = 1 * 29 = 6 \quad \parallel \quad z_9.\text{grad} = 1 * 28 = 22$$

Since z9 is a leaf, the final gradient is z9.grad = 22  
 $\downarrow$   
 wo.grad = 22

1-st iteration

$$z_8.\text{grad} = 6 \quad z_8 = z_7 * \text{relu}(z_5 + z_6)$$

$$\frac{\partial z_8}{\partial z_7} = 1 \text{ if } z_7 > 0 \quad z_7.\text{grad} += z_8.\text{grad} * \frac{\partial z_8}{\partial z_7} = 6 * 1 = 6$$

2nd iteration

$$z_7.\text{grad} = 6 \quad z_7 = z_5 + z_6$$

$$\frac{\partial z_7}{\partial z_5} = 1$$

$$\frac{\partial z_7}{\partial z_6} = 1$$

$$z_6.\text{grad} += z_7.\text{grad} * \frac{\partial z_7}{\partial z_6} = 6 * 1 = 6$$

$$z_5.\text{grad} += z_7.\text{grad} * \frac{\partial z_7}{\partial z_5} = 6 * 1 = 6$$

3rd iteration

$$z_6.\text{grad} = 6 \quad z_6 = z_1 * z_4$$

$$\frac{\partial z_6}{\partial z_4} = z_1$$

$$z_4.\text{grad} += 6 * z_1$$

$$z_4.\text{grad} = 12$$

$$\frac{\partial z_6}{\partial z_1} = z_4$$

$$z_1.\text{grad} = 6 * z_4$$

$$z_1.\text{grad} = 30$$

$$w_i.\text{grad} = 12$$

4th iteration

$$z_5.\text{grad} = 6$$

$$z_5 = z_2 * z_3$$

$$z_2.\text{grad} += 6 * 4 = 24$$

$$\frac{\partial z_5}{\partial z_2} = z_3$$

$$z_3.\text{grad} += 6 * 3 = 18$$

$$\frac{\partial z_5}{\partial z_3} = z_2$$

$$w_r.\text{grad} = 18$$