# Language Technology

http://cs.lth.se/edan20/

Chapter 5, part 3: Dense Representations

#### Pierre Nugues

Pierre.Nugues@cs.lth.se
http://cs.lth.se/pierre\_nugues/

September 10, 2020



### **Dimension Reduction**

One-hot encoding of TFIDF encoding can produce very long vectors: Imagine a vocabulary one one million words per language with 100 languages.

A solution is to produce dense vectors also called word embeddings using a dimension reduction

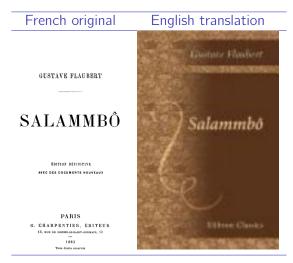
This reduction is very close to principal component analysis or singular value decomposition

It can be automatically obtained through training or initialized with pretrained vectors



#### A Data Set: Salammbô

A corpus is a collection - a body - of texts.





### Supervised Learning

#### Letter counts from Salammbô

Chapter	French		English	
	# characters	# A	# characters	# A
Chapter 1	36,961	2,503	35,680	2,217
Chapter 2	43,621	2,992	42,514	2,761
Chapter 3	15,694	1,042	15,162	990
Chapter 4	36,231	2,487	35,298	2,274
Chapter 5	29,945	2,014	29,800	1,865
Chapter 6	40,588	2,805	40,255	2,606
Chapter 7	75,255	5,062	74,532	4,805
Chapter 8	37,709	2,643	37,464	2,396
Chapter 9	30,899	2,126	31,030	1,993
Chapter 10	25,486	1,784	24,843	1,627
Chapter 11	37,497	2,641	36,172	2,375
Chapter 12	40,398	2,766	39,552	2,560
Chapter 13	74,105	5,047	72,545	4,597
Chapter 14	76,725	5,312	75,352	4,871
Chapter 15	18,317	1,215	18,031	1,119

Data set: https://github.com/pnugues/ilppp/tree/master programs/ch04/salammbo

## Principal Component Analysis

We will use a small dataset to explain principal component analysis: The characters in *Salammbô* 

Chapter   Chap																													
Column   C	Ch.	,5,	.р.	.6.	.q.	'e'	'F'	.9.	ъ.	7	7	'k'	- 4	'm'	'n'	.0,	,b,	,d,	- 7	15	't'	.0.	ν.	'W'	,×,	- 'y'	'Z'	.9.	.9.
0.5   10.62   12.2   22.5   24.6   10.7   10.7   25.5   25	01 fr	2503	365	857	1151	4312	264	349	295	1945	65	- 4	1946	726	1896	1372	789	248	1948	2996	1938	1792	414	0	129	94	20	128	36
04 F 2487 303 864 137 4189 314 231 227 2028 137 31 1796 72 1989 1314 31 27 100 43 105 75 75 105 75 1	02 fr	2992	391	1006	1388	4993	319	360	350	2345	81	6	2128	823	2308	1560	977	281	2376	3454	2411	2069	499	0	175	89	23	136	50
Section   Conference   Confer	03 fr	1042	152	326	489	1785	136	122	126	784	41	7	816	397	778	612	315	102	792	1174	856	707	147	0	42	31	7	39	9
OF   1205   2006   2008   2010   1206   2005   2008   2010   1206   2015   2010   20	04 fr	2487	303	864	1137	4158	314	331	287	2028	57	3	1796	722	1958	1318	773	274	2000	2792	2031	1734	422	0	138	81	27	110	43
07   5062   706   1707   2388   861   623   622   623   624   625	05 fr	2014	268	645	949	3394	223	215	242	1617	67	3	1513	651	1547	1053	672	166	1601	2192	1736	1396	315	1	83	67	18	90	67
0   0   0   0   0   0   0   0   0   0	06 fr	2805	368	910	1266	4535	332	384	378	2219	97	3	1900	841	2179	1569	868	285	2205	3065	2293	1895	453	0	151	80	39	131	42
0 7 210 29 29 771 92 29 29 272 29 29 29 29 29 29 20 20 21 21 21 20 20 21 21 21 20 20 21 21 21 21 21 21 21 21 21 21 21 21 21	07 fr	5062	706	1770	2398	8512	623	622	620	4018	126	19	3726	1596	3851	2823	1532	468	4015	5634	4116	3518	844	0	272	148	71	246	50
10   176   176   249   546   865   302   179   242   215   139   66   5   1402   598   124   245   159   150   150   142   139   141   170   141   170   141   170   141   170   141   170   170   141   170   1	08 fr	2643	325	869	1085	4229	307	317	359	2102	85	4	1857	811	2041	1367	833	239	2132	2814	2134	1788	437	0	135	64	30	130	43
11 7 2041 31 1217 1079 4018 238 277 438 288 277 330 1885 144 0 1886 900 1966 1356 763 230 1912 2564 2218 1737 425 0 144 61 25 101 40 1275 1276 277 4818 2329	09 fr	2126	289	771	920	3599	278	289	279	1805	52	6	1499	619	1711	1130	651	187	1719	2404	1763	1448	348	0	119	58	20	90	24
12 F 276 373 978 123 277 413 297 398 124 416 299 390 390 390 390 273 68 2 1965 812 298 141 868 272 276 1313 274 1923 455 0 189 98 37 129 33 13 F 596 775 273 678 648 278 145 2	10 fr	1784	249	546	805	3002	179	202	215	1319	60	5	1462	598	1246	922	557	172	1242	1769	1423	1191	270	0	65	61	11	73	18
13 F 9647 755 1730 2273 8678 648 866 642 380 174 22 3766 1807 3864 2756 1507 485 425 4081 1809 487 3480 1807 62 0 281 145 4 22 375 141 147 5312 541 147 5312 541 147 5312 541 147 5312 541 147 5312 541 147 54												0												0					
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	12 fr	2766	373	935	1237	4618	329	350	349	2273	65	2	1955	812	2285	1419	865	272	2276	3131	2274	1923	455	0	149	98	37	129	33
15   125   173   402   582   216   150   134   148   90   27   6   950   387   90   607   417   103   905   136   108   905   90   60   83   36   3   48   20	13 fr	5047	725	1730	2273	8678	648	566	642	3940	140	22	3746	1597	3984	2736	1550	425	4081	5599	4387	3480	767	0	288	119	41	209	55
01 m 2217 451 795 1316 5867 586 662 2050 1823 22 200 1254 686 1851 1897 525 15 1764 1842 2847 764 286 683 20 401 18 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0										4278		2			4255	2713											41		
	15 fr	1215	173	402	582	2195	150	134	148	969	27	6	950	387	906	697	417	103	985	1395	1037	893	206	0	63	36	3	48	20
03   04   05   05   05   05   05   05   05	01 en	2217	451	729	1316	3967	596	662	2060	1823	22	200	1204	656	1851	1897	525	19	1764	1942	2547	704	258	653	29	401	18	0	0
04 = 2274 454 736 1315 3814 595 599 1879 1885 2 7 188 187 2 189 1873 696 171 1865 514 33 1726 1888 7 187 64 745 26 663 60 467 19 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0											13																	0	0
	03 en																										15	0	0
06 = 2006 518 797 1509 4237 687 699 2254 2007 26 216 1239 783 2174 2231 613 25 1931 2192 265 1899 277 733 49 464 37 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0											22																	0	0
07 = 405 013 1221 2081 7834 1306 1183 4379 2838 24 10 24 12 24 10	05 en										7																	0	0
08 = 286 431 702 1416 4014 621 624 2171 2011 24 216 152 748 2085 1947 527 33 1915 1966 2765 789 266 605 65 379 24 0 0 0 0 0 0 0 = 1933 408 653 1063 379 575 571 7166 148 151 468 16 29 178 58 58 58 58 58 58 58 58 58 58 58 58 58																												0	0
00 - 1993 408 6053 1006 3173 575 517 1766 1648 16 146 881 629 1728 1698 442 20 1661 18076 2442 683 208 500 50 25 328 18 0 0 0 11 cm 1627 396 451 296 452 207 1807 1807 1807 1807 1807 1807 1807 18																												0	0
10 m 1077 399 481 977 643 1938 2690 477 409 1475 1106 7 131 789 506 1266 1369 125 23 1211 1344 1799 502 181 410 31 255 20 0 0 1 12 m 256 250 250 250 250 250 250 250 250 250 250																												0	0
11 cm 2275 437 643 1364 3790 610 644 2277 1830 16 217 1122 799 1833 1948 486 23 1720 1945 2424 787 246 632 20 457 39 0 0 12 cm 250 499 757 156 4331 677 675 65 2348 033 28 234 1102 746 2152 2105 581 291 291 2152 304 67 750 721 35 418 40 0 0 13 cm 4597 997 1462 2690 7963 1254 1201 4278 3634 39 42 2281 1493 3774 3911 1099 49 2577 3894 556 1179 437 1374 77 673 49 0 0 14 cm 450 450 450 450 450 450 450 450 450 450											16																	0	0
12 en 2560 489 757 1566 4331 677 650 2348 2033 28 234 1102 746 2125 2105 581 32 1939 2152 3046 750 278 721 35 418 40 0 0 0 13 en 4597 987 1462 2689 789 1104 2549 5049 3 412 2281 1493 3774 891 1109 49 35 369 3044 580 1104 377 673 49 0 0 14 en 4671 948 1439 2799 8179 135 1104 534 8259 36 427 2281 1548 4053 3999 1019 35 3699 3046 588 1890 539 3137 00 856 49 0 0											7																	0	0
13 <sup>-</sup> en 4597 987 1462 2698 7963 1254 1201 4278 3634 39 432 2281 1493 3774 3911 109 49 3577 3894 5540 1379 437 1374 77 673 49 0 0 0 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1																												0	0
14 en 4871 948 1439 2799 8179 1335 1140 4534 3829 36 427 2218 1534 4053 3989 1019 36 3689 3946 5858 1490 539 1377 90 856 49 0 0																												0	0
																												0	0
15_en 1119 229 335 683 1994 323 281 1108 912 9 112 579 351 924 1004 305 9 863 997 1330 310 108 330 14 150 9 0 0																												0	0
	15_en	1119	229	335	683	1994	323	281	1108	912	9	112	579	351	924	1004	305	9	863	997	1330	310	108	330	14	150	9	0	0

Table: Character counts per chapter, where the fr and en suffixes designate the language, either French or English

Each chapter is modeled by a vector of characters.

### Character Counts

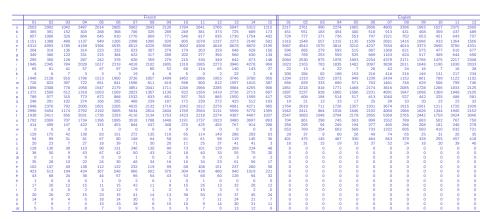


Table: Character counts per chapter in French, left part, and English, right part

Each characters is modeled by a vector of chapters.

## Singular Value Decomposition

There are as many as 40 characters: the 26 unaccented letters from a to z and the 14 French accented letters

**Singular value decomposition** (SVD) reduces these dimensions, while keeping the resulting vectors semantically close

**X** is the  $m \times n$  matrix of the letter counts per chapter, in our case, m = 30 and n = 40.

We can rewrite X as:

$$X = U \Sigma V^{\mathsf{T}}$$

where **U** is a matrix of dimensions  $m \times m$ ,  $\Sigma$ , a diagonal matrix of dimensions  $m \times n$ , and **V**, a matrix of dimensions  $n \times n$ .

The diagonal terms of  $\Sigma$  are called the **singular values** and are traditionally arranged by decreasing value.

We keep the highest values and set the rest to zero.

### Code Example

Jupyter Notebook 3.1-SVD



## Word Embeddings

We can extend singular value decomposition from characters to words. The rows will represent the words in the corpus, and the columns,

We can replace documents by a context of a few words to the left and to the right of the focus word:  $w_i$ .

A context  $C_j$  is then defined by a window of 2K words centered on the word:

$$W_{i-K}, W_{i-K+1}, ..., W_{i-1}, W_{i+1}, ..., W_{i+K-1}, W_{i+K},$$

where the context representation uses a bag of words.

We can even reduce the context to a single word to the left or to the right of  $w_i$  and use bigrams.

documents.

## Word Embeddings

We store the word-context pairs  $(w_i, C_j)$  in a matrix.

Each matrix element measures the association strength between word  $w_i$  and context  $C_j$ , for instance mutual information.

Mutual information, often called pointwise mutual information (the strength of an association) is defined as:

$$I(w_i, w_j) = \log_2 \frac{P(w_i, w_j)}{P(w_i)P(w_j)} \approx \log_2 \frac{N \cdot C(w_i, w_j)}{C(w_i)C(w_j)}.$$

D#\Words	$C_1$	$C_2$	<i>C</i> <sub>3</sub>	 Cn
$w_1$	$MI(w_1, C_1)$	$MI(w_1, C_2)$	$MI(w_1, C_3)$	 $MI(w_1, C_n)$
W <sub>2</sub>	$MI(w_2, C_1)$	$MI(w_2, C_2)$	$MI(w_2, C_3)$	 $MI(w_2, C_n)$
<i>W</i> 3	$MI(w_3, C_1)$	$MI(w_3, C_2)$	$MI(w_3, C_3)$	 $MI(w_3, C_n)$
				 about 1
Wm	$MI(w_m, C_1)$	$MI(w_m, C_2)$	$MI(w_m, C_3)$	 M. ( )
	•			000

## Word Embeddings

We compute the word embeddings with a singular value decomposition, where we truncate the matrix  $\mathbf{U}\Sigma$  to 50, 100, 300, or 500 dimensions. The word embeddings are the rows of this matrix.

We usually measure the similarity between two embeddings  ${\bf u}$  and  ${\bf v}$  with the cosine similarity:

 $\mathsf{cos}\big(u,v\big) = \frac{u \cdot v}{||u|| \cdot ||v||},$ 

ranging from -1 (most dissimilar) to 1 (most similar) or with the cosine distance ranging from 0 (closest) to 2 (most distant):

$$1 - \cos(\mathbf{u}, \mathbf{v}) = 1 - \frac{\mathbf{u} \cdot \mathbf{v}}{||\mathbf{u}|| \cdot ||\mathbf{v}||}.$$



### Popular Word Embeddings

Embeddings from large corpora are obtained with iterative techniques Some popular embedding algorithms with open source programs:

word2vec: https://github.com/tmikolov/word2vec

GloVe: Global Vectors for Word Representation

https://nlp.stanford.edu/projects/glove/

ELMo: https://allennlp.org/elmo

fastText: https://fasttext.cc/

To derive word embeddings, you will have to apply these programs on a very large corpus

Embeddings for many languages are also publicly available. You just

download them

gensim is a Python library to create word embeddings from a continuous https://radimrehurek.com/gensim/index.html