Exercie 1: Linear Decision Boundaries

Part A

Lets load and important the iris data set

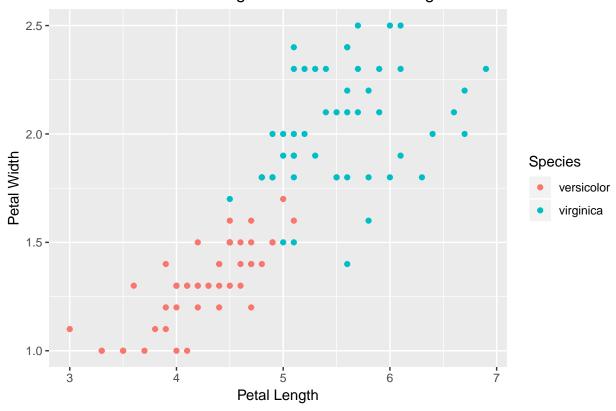
```
data(iris)
summary(iris)
##
     Sepal.Length
                     Sepal.Width
                                     Petal.Length
                                                      Petal.Width
                                            :1.000
##
   Min.
           :4.300
                    Min.
                           :2.000
                                    Min.
                                                     Min.
                                                            :0.100
##
   1st Qu.:5.100
                    1st Qu.:2.800
                                    1st Qu.:1.600
                                                     1st Qu.:0.300
##
  Median :5.800
                    Median :3.000
                                    Median :4.350
                                                     Median :1.300
           :5.843
                    Mean :3.057
                                          :3.758
## Mean
                                    Mean
                                                     Mean
                                                           :1.199
##
   3rd Qu.:6.400
                    3rd Qu.:3.300
                                    3rd Qu.:5.100
                                                     3rd Qu.:1.800
##
  \mathtt{Max}.
          :7.900
                    Max. :4.400
                                    Max. :6.900
                                                    Max.
                                                           :2.500
##
          Species
##
   setosa
              :50
  versicolor:50
##
   virginica:50
##
##
##
# Lets look at the head of the iris data set
head(iris)
     Sepal.Length Sepal.Width Petal.Length Petal.Width Species
## 1
              5.1
                          3.5
                                       1.4
                                                    0.2 setosa
## 2
              4.9
                          3.0
                                       1.4
                                                    0.2 setosa
                          3.2
## 3
              4.7
                                       1.3
                                                    0.2 setosa
              4.6
                          3.1
                                       1.5
                                                    0.2 setosa
## 5
              5.0
                          3.6
                                       1.4
                                                    0.2 setosa
                          3.9
              5.4
                                       1.7
                                                    0.4 setosa
# Number of rows of the iris dataset (number of individual observations)
nrow(iris)
## [1] 150
# All of the columns are numeric except for the species column
# They are continuous because they correspond to length and width (except for species) # The species ar
sapply(iris, class)
## Sepal.Length Sepal.Width Petal.Length Petal.Width
                                                             Species
                   "numeric"
                                                            "factor"
      "numeric"
                                "numeric"
                                              "numeric"
# The only categorical variable is species in this iris dataset
sapply(iris, class)
## Sepal.Length Sepal.Width Petal.Length Petal.Width
                                                             Species
      "numeric"
                   "numeric"
                                "numeric"
                                              "numeric"
                                                            "factor"
```

From our observations it looks like there are 50 samples of three species: setosa, versicolor and virginica. Each of the samples has measurements of sepal length, sepal width and petal length.

Let's plot the second and third iris classses:

```
# Lets pick the 2nd and 3rd classes: versicolor and virginica and let's plot the subset
plot1 <- iris %>% filter(Species == 'versicolor' | Species == 'virginica') %>%
ggplot(aes(x = Petal.Length, y = Petal.Width, color = Species)) + geom_point() +
labs(color = "Species") + xlab("Petal Length") + ylab("Petal Width") +
ggtitle("Petal Width vs Petal Length for Versicolor and Virginica")
plot1
```

Petal Width vs Petal Length for Versicolor and Virginica



Part B

The following function will take in five inputs (c0, c1, c2) which are constants that will be estimated later in this exercise and (x1, x2) which correspond to petal width and petal length. The output will return a value between a probability value between 0 and 1 where all values above 0.5 will correspond to the 3rd iris class and values below 0.5 to the 2nd iris class.

```
# inputs: c0, c1, c2, petal_width, petal_length
# outputs:

one_layer_neural_network <- function(c0, c1, c2, petal_width, petal_length) {

# Linear function
    z <- c0 + c1*x1 + c2*x2

#result
    result <- 1/(1 + exp(1)^(-z))</pre>
```

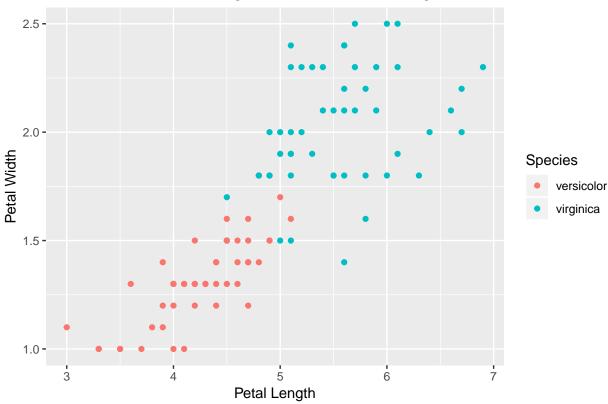
```
return(result)
}
```

Part C

We are going to estimate the constant values such as...

```
# Lets pick the 2nd and 3rd classes: versicolor and virginica and let's plot the subset
plot2 <- iris %>% filter(Species == 'versicolor' | Species == 'virginica') %>%
ggplot(aes(x = Petal.Length, y = Petal.Width, color = Species)) + geom_point() +
labs(color = "Species") + xlab("Petal Length") + ylab("Petal Width") +
ggtitle("Petal Width vs Petal Length for Versicolor and Virginica")
plot2
```

Petal Width vs Petal Length for Versicolor and Virginica



Part D### Part E