

A statistical perspective on fMRI analysis: Inferring neural activation from brain imaging data

28 Sept. 2022 – XXX Conference of the Italian Association of Psychology

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Overview

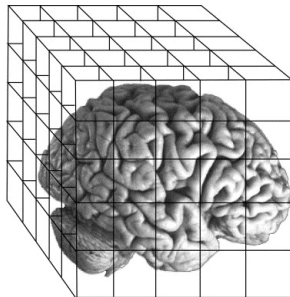
Functional Magnetic Resonance Imaging

fMRI measures **brain activation**
as changes in blood flow (BOLD)
under a sequence of stimuli

Activation is measured in **voxels**
 $\approx 200,000$ highly correlated volume units

Voxel i :

- **null hypothesis** H_i : *no activation in voxel i*
- **test statistic** T_i from first-level analysis

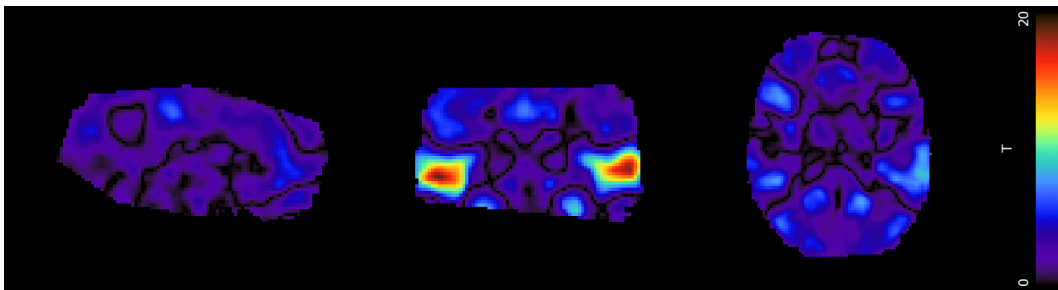


Auditory data

140 subjects passively listening to vocal and non-vocal sounds (168,211 voxels)¹

H_i : no activation in voxel i

T_i = one-sample t-statistic



¹Pernet et al. The human voice areas: spatial organisation and inter-individual variability in temporal and extra-temporal cortices. *OpenNeuro dataset*, 2019.

Functional Magnetic Resonance Imaging

Generally interest lies in **clusters**,
brain regions of (contiguous) voxels

Supra-threshold clusters:

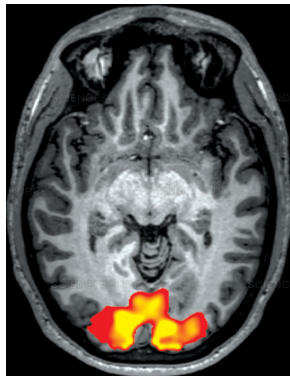
regions of connected voxels i with
 $T_i > \text{threshold}$

Clusters S :

- **null hypothesis**

$H_S = \bigcap_{i \in S} H_i$: no activation in cluster S

- **global test statistic** T_S



Multiple hypothesis testing

Single null hypothesis H_i :

- type I error = wrongly reject H_i when it is true
- significance level $\alpha = P(\text{type I error})$

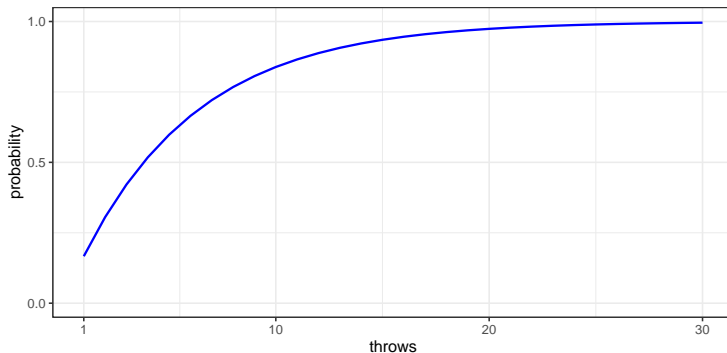
Multiple hypotheses together:

the probability of making at least one type I error can be much greater than α

Intuition: m throws of a dice

The probability of getting at least one 6 is

- $1/6 \approx 0.167$ for $m = 1$
- $1 - (5/6)^m$ in general



Cluster analysis

Standard method for cluster inference that controls the error at cluster level

H_S is rejected $\implies S$ contains at least one active voxel

No information on

- the proportion of active voxels (TDP)
- their spatial location

$\text{TDP}(S) = \text{proportion of truly active voxels in cluster } S$

Simultaneous lower $(1 - \alpha)$ -confidence bounds¹:

$$P(\text{TDP}(S) \geq \text{bound}(S) \text{ for each cluster } S) \geq 1 - \alpha$$

Allows for **post-hoc selection**

→ choosing clusters after seeing results

¹Goeman and Solari. Multiple testing for exploratory research. *Stat. Sci.*, 2011.

Computational complexity of closed testing:

exponential in the number of voxels

→ infeasible for high-dimensional data

We provide a **shortcut**¹:

- valid in many cases
- makes inference on the TDP of clusters

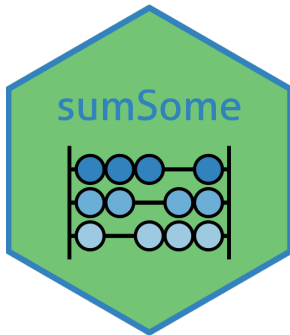
¹Vesely et al. Permutation-based true discovery guarantee by sum tests. *arXiv:2102.11759*, 2021.

Results

The method is implemented in the R package `sumSome`¹, with underlying code in C++.

```
permT <- brainScores(copes, alpha=0.05, ...)
```

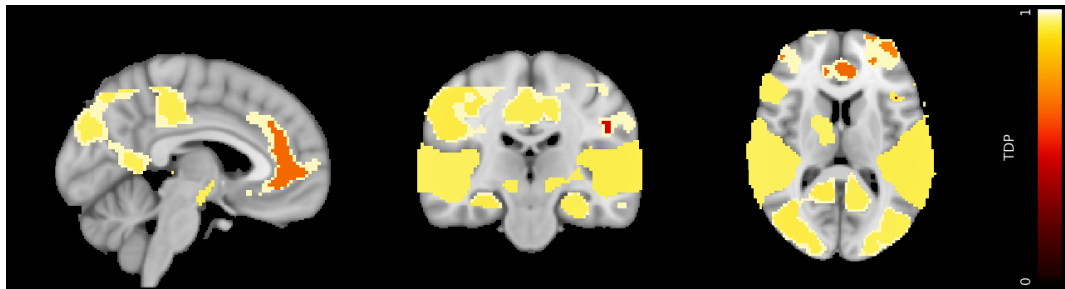
```
brainAnalysis(permT, clusters)
```



¹<https://CRAN.R-project.org/package=sumSome>

We obtain **simultaneous confidence bounds** for the TDP of clusters:

- clusters with $T_i > 3.2$
- sub-clusters with $T_i > 4$



Auditory data

cluster	threshold	size	TDP (%)	coordinates		
<i>S</i>	<i>thr</i>	<i>s</i>	lower conf. bound	<i>x</i>	<i>y</i>	<i>z</i>
FP/CG/SFG/TOF/LO/LG OFG/ITG/SG/AG/NA	3.2	40,094	98.21	-30	-34	-16
Left LO/TOF	4	8,983	94.79	-30	-34	-16
Right LO/LG/ITG	4	7,653	93.85	28	-30	-18
Left SFG/FP	4	1,523	69.67	-28	34	42
CG	4	1,341	65.62	6	40	-2
Right FP	4	1,327	66.01	30	56	28
Left SG/AG	4	859	47.85	-50	-56	36
Right STG/PT/MTG HG/PrG/T	3.2	12,540	95.41	60	-10	0
STG/PT/MTG/HG	4	9,533	95.17	60	-10	0
PrG	4	485	25.15	52	0	48
Left STG/PT/MTG/ HG/IFG/T	3.2	10,833	94.66	-60	-12	2
HG/PT/MTG/STG	4	7,894	94.20	-60	-12	2
IFG	4	667	38.98	-40	14	26

To quantify and localize brain activation in clusters → inference on the TDP

sumSome:

a general closed testing method to give

lower $(1 - \alpha)$ -confidence bounds for the TDP, simultaneously over all clusters

Results are valid even if the clusters of interest are chosen post hoc.

Questions



<https://github.com/annavesely/AIP2022>