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Cosine Similarity

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Today

Cosine Similarity

- Cosine Similarity
- Soft cosine similarity
 - Word embeddings
 - Implemention in Python
- Topic modelling
 - An introduction to LDA
 - Choosing the best (or a good) topic model
 - Using topic models
- Next steps

The CCS toolbox

Cosine Similarity

Methodological approach Counting and Supervised Unsupervised Dictionary Machine Learning Machine Learning Typical research interests visibility analysis frames frames and content features sentiment analysis topics topics subjectivity analysis gender bias Common statistical string comparisons support vector machines principal component analysis procedures counting naive Bayes cluster analysis latent dirichlet allocation semantic network analysis deductive inductive

Boumans and Trilling, 2016

Cosine Similarity

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Cosine Similarity

 A measure that helps you determine how similar two documents are, irrespective of their size

Applications in Communication Science

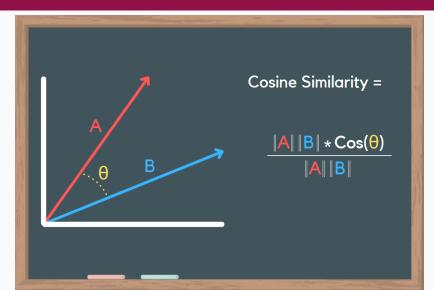
- For example, to map *linguistic alignment* of romantic couples over time (Brinberg and Ram, 2021)
- Or, in the political domain, agenda overlap between public opinion and political speech (Hager and Hilbig, 2020b)

Cosine Similarity

similarity =
$$\cos(\theta) = \frac{A \cdot B}{\|A\| \|B\|} = \frac{\sum_{i=1}^{n} A_i B_i}{\sqrt{\sum_{i=1}^{n} A_i^2} \sqrt{\sum_{i=1}^{n} B_i^2}}$$

- It measures the cosine of the angle between two vectors projected in a multi-dimensional space.
- 0 means orthogonal vectors (90 degrees); very dissimal
- 1 means vectors are the same (0 degrees); similar

Cosine Similarity



how can we calculate this in python?

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Let's review a practical application ².

²https://github.com/annekroon/CCS-2/blob/main/week04/exercises/cosine-similarity-basics.ipynb

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```
from sklearn.feature_extraction.text import CountVectorizer,
1

→ TfidfVectorizer

     import pandas as pd
3
     doc1 = "When I eat breakfast, I usually drink some tea".lower()
4
     doc2 = "I like my tea with my breakfast".lower()
5
     doc3 = "She likes cereal and coffee".lower()
     vec = CountVectorizer(stop_words='english')
8
     count matrix = vec.fit transform([doc1, doc2])
9
10
     print(pd.DataFrame(count_matrix.A,
11
         columns=vec.get_feature_names()).to_string())
```

```
        breakfast
        cereal
        coffee
        drink
        eat
        like
        likes
        tea
        usually

        0
        1
        0
        0
        1
        0
        0
        1
        1

        1
        1
        0
        0
        0
        1
        0
        1
        0

        2
        0
        1
        1
        0
        0
        0
        1
        0
        0
```

Implementation in Python

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```
The vector belonging to doc1: [1, 0, 0, 1, 1, 0, 0, 1, 1]
The vector belonging to doc2: [1, 0, 0, 0, 0, 1, 0, 1, 0]
```

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Now, lets populate the formula. 1.Execute the part of the formula in the numerator. Specifically, take the dot product of the vectors:

$$\sum_{i=1}^n A_i B_i$$

```
doc1: [1, 0, 0, 1, 1, 0, 0, 1, 1]
doc2: [1, 0, 0, 0, 0, 1, 0, 1, 0]
```

$$dot_product = (1 \cdot 1) + (0 \cdot 0) + (0 \cdot 0) + (1 \cdot 0) + (1 \cdot 0) + (0 \cdot 0) + (1 \cdot 1) + (1 \cdot 0)$$

Or, using Python:

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2.Execute the part of the formula in the denumerator. Take the cross product of the two vectors.

$$\sqrt{\sum_{i=1}^{n} A_i^2} \sqrt{\sum_{i=1}^{n} B_i^2}$$

Calculate this by hand:

$$doc1_{=}\sqrt{1^{2}+0^{2}+0^{2}+1^{2}+1^{2}+0^{2}+1^{2}+1^{2}}$$

 $doc1_{=}\sqrt{1^{2}+0^{2}+0^{2}+0^{2}+1^{2}+0^{2}+1^{2}+0^{2}}$

Implementation in Python:

```
import math
doc1_ = math.sqrt(sum( [i**2 for i in doc1_vector]) )
doc2_ = math.sqrt(sum( [i**2 for i in doc2_vector]) )
```

Implementation in Python

3. Finally:

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```
cos_sim = dot_product / (doc1_ * doc2_)
print(cos_sim)
```

0.5163977794943222

Implementation in Python

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We can, however, do this much faster using sklearn's cosine_similarity.

```
from sklearn.metrics.pairwise import cosine_similarity cosine_similarity([doc1_vector, doc2_vector])
```

```
array([[1. , 0.51639778], [0.51639778, 1. ]])
```

How to use this in practice

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What can you do with this?

- This is especially powerful if you want to compare different news articles, movies, song texts, etc.
- For example, which movies are most similair in terms of genre composition?

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	title	Avatar	Pirates of the Caribbean: At World's End	Spectre	The Dark Knight Rises	John Carter
	genre	action adventure fantasy science fiction	adventure fantasy action	action adventure crime	action crime drama thriller	action adventure science fiction
title	genres					
Avatar	action adventure fantasy science fiction	1.000000	0.691870	0.315126	0.084696	0.859850
Pirates of the Caribbean: At World's End	adventure fantasy action	0.691870	1.000000	0.455470	0.122417	0.366490
Spectre	action adventure crime	0.315126	0.455470	1.000000	0.473354	0.366490
The Dark Knight Rises	action crime drama thriller	0.084696	0.122417	0.473354	1.000000	0.098501
John Carter	action adventure science fiction	0.859850	0.366490	0.366490	0.098501	1.000000

Indentify movies that are similar in terms of genre ³

 $^{^3} https://www.learndatasci.com/glossary/cosine-similarity/\\$

Considering Cosine Similarity

Things to consider

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- What type of overlap are you interested in?
- What is the meaning of n-grams, stems, stopwords when considering your RQ? How you should preproces, depends on your RQ and aim.
- Computationally cheap and fast; works well in e.g., recommender systems (week 6!)

Drawbacks

An exact match in terms of words is needed. Is that realistic?

Implementation in Python

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```
doc1 = "When I eat breakfast, I usually drink some tea".lower()
doc2 = "I like my tea with my breakfast".lower()
doc3 = "She likes cereal and coffee".lower()
```

What do you expect here? Should there be some level of overlap?

Implementation in Python

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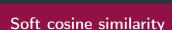
```
doc1 = "When I eat breakfast, I usually drink some tea".lower()
doc2 = "I like my tea with my breakfast".lower()
doc3 = "She likes cereal and coffee".lower()
```

```
print(cosine_similarity([doc1_vector, doc2_vector, doc3_vector]))
```

```
[[1. 0.51639778 0. ]
[0.51639778 1. 0. ]
[0. 0. 1. ]
```

Zero overlap between doc3 and the other documents. Is that correct?

Soft cosine similarity



Cosine Similarity

...enter soft cosine similarty (Sidorov et al., 2014)

"Soft Cosine Measure (SCM) is a method that allows us to assess the similarity between two documents in a meaningful way, even when they have no words in common. It uses a measure of similarity between words, which can be derived using [word2vec] vector embeddings of words." ⁴

⁴https:

^{//}radimrehurek.com/gensim//auto_examples/tutorials/run_scm.html

Soft Cosine Measure (SCM)

SCM

Cosine Similarity

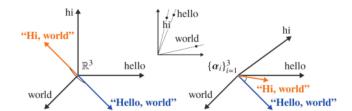
- Even if two sentences do not share the same words, we can calculate similarity by modelling synonym
- For example, the words 'play' and 'game' are different but related (Sidorov et al., 2014) ⁵
- How can we capture 'semantic' meaning?

How?

Convert words to word vectors and then compute similarities ⁶

⁵http://www.scielo.org.mx/pdf/cys/v18n3/v18n3a7.pdf

⁶https://www.machinelearningplus.com/nlp/cosine-similarity/



Soft cosine similarity ⁷

⁷https:

Word embeddings

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Word embeddings

• To use the SCM, you need word embeddings.

Soft cosine similarity

Word embeddings

Cosine Similarity

SCM estimates extracts similarity from word embeddings.

What are word embeddings?

- No technical details here, just the general idea
- Word embeddings help capturing the meaning of text
- Word embeddings are low-dimensional vector representations that capture semantic meaning
- State-of-the-art in NLP...
- "...a word is characterized by the company it keeps..." (Firth, 1957)

Soft cosine similarity

Implemention in Python

SCM in Python

Cosine Similarity

Calculating Soft Cosine Measure

- To use the SCM, you need embeddings.
- We can train embeddings on our own corpus (if we had a lot of data) . . .
- But for now we will use pre-trained models ⁸. . . .

```
import gensim.downloader as api
fasttext_model300 = api.load('fasttext-wiki-news-subwords-300')
```

⁸https://github.com/annekroon/CCS-2/blob/main/week04/exercises/
cosine-similarity-basics.ipynb

Create a dictionary

Let's review our 3 documents:

```
doc1 = "When I eat breakfast, I usually drink some tea".lower()
doc2 = "I like my tea with my breakfast".lower()
doc3 = "She likes cereal and coffee".lower()
```

Initialize a Dictionary. This step assigns a token_id to each word:

```
from gensim.utils import simple_preprocess
from gensim.corpora import Dictionary
dictionary = corpora.Dictionary([simple_preprocess(doc) for doc in [doc1, doc2, doc3]])
```

Now, let's check whether a specific word-for example coffee-is in our dictionary:

```
'coffee' in dictionary.token2id
```

True

Create a bag-of-words representation

Cosine Similarity

Next, let's represent each document by (token_id, token_count) tuples:

```
bag_of_words_vectors = [ dictionary.doc2bow(simple_preprocess(doc))

→ for doc in [doc1, doc2, doc3]]
```

Build a term similarity matrix and compute a sparse term similarity matrix:

```
from gensim.similarities import SparseTermSimilarityMatrix
from gensim.similarities import WordEmbeddingSimilarityIndex

similarity_index = WordEmbeddingSimilarityIndex(fasttext_model300)
similarity_matrix = SparseTermSimilarityMatrix(similarity_index,

dictionary)
```

Inspect results

Get SCM using .inner_product()::

```
#hetween doc1 and doc2:
      scm_doc1_doc2 = similarity_matrix.inner_product(bag_of_words_vectors[0],

    bag_of_words_vectors[1], normalized=(True, True))

3
4
      #hetween doc1 and doc3:
5
      scm_doc1_doc3 = similarity_matrix.inner_product(bag_of_words_vectors[0],

    bag_of_words_vectors[2], normalized=(True, True))

6
      #between doc2 and doc3:
      scm_doc2_doc3 = similarity_matrix.inner_product(bag_of_words_vectors[1],

→ bag of words vectors[2], normalized=(True, True))
9
10
      print(f"SCM between:\ndoc1 <-> doc2: {scm_doc1_doc2:.2f}\ndoc1 <-> doc3:
```

Do the results make more sense?:

```
SCM between:
doc1 <-> doc2: 0.29
doc1 <-> doc3: 0.15
doc2 <-> doc3: 0.28
```

Applications of cosine and soft cosine similarity

Applications of *cosine* and *soft cosine* in the field of Communication Science generally involve some overtime dynamics.

Trace convergence or agenda setting dynamics over time

- Beyond the scope this course to discuss it here, but if you are interested in how you can apply cosine and soft cosine in an overtime analysis, we have prepared a notebook that will help you do just that.
- https:

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//github.com/annekroon/CCS-2/blob/main/week04/
exercises/OPTIONAL_overtime_similarity.ipynb

Topic modelling

Cosine Similarity

Let's assume you want to know a bit more about the *content* you are investigating

Cosine and soft cosine do *not* inform us about substantive issues present in text.

- 1. Which topics can we extract from the corpus?
- 2. How present is each of these topics in each text in the corpus?

Recap: Document-term matrix

Document-term matrix

Cosine Similarity

These can be simple counts, but also more advanced metrics, like tf-idf scores (where you weigh the frequency by the number of documents in which it occurs), cosine distances, etc.

- given a term-document matrix, easy to do with any tool
- probably extremely skewed distributions

Recap: clustering

Cosine Similarity

• given a term-document matrix, we can easily find clusters of documents that resemble each other

- 1. model simultaneously (a) which topics we find in the whole corpus, and (b) which of these topics are present in which document; while at the same time
- 2. allowing (a) words to be part of multiple topics, and (b) multiple topics to be present in one document; and
- 3. being able to make connections between words "even if they never actually occured in a document together" (Maier et al., 2018)[p. 96]

Maier, D., Waldherr, A., Miltner, P., Wiedemann, G., Niekler, A., Keinert, A., ... Adam, S. (2018). Applying LDA Topic Modeling in Communication Research: Toward a Valid and Reliable Methodology. Communication Methods and Measures, 12(2-3), 93-118. doi:10.1080/19312458.2018.1430754

Topic modelling

An introduction to LDA

Enter topic modeling with Latent Dirichlet Allocation (LDA)

No mathematical details here, but the general idea

- There are k topics, $T_1 \dots T_k$
- Each document D_i consists of a mixture of these topics, e.g. $80\% T_1$, $15\% T_2$, $0\% T_3$, ... $5\% T_k$
- On the next level, each topic consists of a specific probability distribution of words

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- Thus, based on the frequencies of words in D_i , one can infer its distribution of topics
- Note that LDA is a Bag-of-Words (BOW) approach

We will use gensim (Rehurek and Sojka, 2010) for this (make sure you have version >4.0)

Let us assume you have a list of lists of documents called texts:

print(texts[0][:115])

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which looks something like:

'Stop the presses: CNN covered some actual news yesterday when it reported on the story of

medical kidnapping victim Alyssa Gilderhus at the Mayo Clinic. But was it actually InfoWars
and FreeMartyG which publicly shamed CNN into doing this real journalism? Cue the Mission
Impossible theme music for this one...\n\nThis mission, as we accepted it, began more than a
year ago during the baby Charlie Gard medical kidnapping scandal in the UK and we thought
that it had ended with an apparently unsuccessf'

Řehůřek, R., & Sojka, P. (2010). Software framework for topic modelling with large corpora.

Proceedings of the LREC 2010 Workshop on New Challenges for NLP Frameworks, pp. 45-50. Valletta,

Malta: ELRA. 35

Your preprocessing steps and feature engineering decisions *largely* affect your topics

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- 1. You can apply 'manual' preprocessing steps . . .
- 2. ... In isolation or combination with for example tfidf transformations

```
texts_clean = [text.lower() for text in texts]
      texts_clean=[" ".join(text.split()) for text in texts_clean] #remove dubble spaces
      texts clean = ["", join([1 for 1 in text if 1 not in punctuation]) for text in texts clean]

→ #remove punctuaction

      texts_clean[0][:500]
4
```

which looks something like:

'stop the presses cnn covered some actual news yesterday when it reported on the story of

Preprocessing

Cosine Similarity

Without stopword removal, tfidf transformation and/or pruning, you topics will not be very informative.

which looks something like:

'stop presses cnn covered actual news yesterday reported story medical kidnapping victim alyssa

gilderhus mayo clinic actually infowars freemartyg publicly shamed cnn real journalism cue

mission impossible theme music one mission accepted began year ago baby charlie gard medical

kidnapping scandal uk thought ended apparently unsuccessful april fools joke cnn sure many

recall charlie gard infant rare form otherwise notsorare condition mitochondrial disease

story went viral made international news '

Tokenization

Cosine Similarity

gensim expects a list of words (hence: tokenize your corpus)

```
tokenized_texts_clean = [TreebankWordTokenizer().tokenize(text) for text in texts_clean ] #

tokenize texts; convert all strings to a list of tokens
tokenized_texts_clean[0][:500]
```

which looks something like:

```
['stop',
'presses',
'cnn',
'covered',
'actual',
'news',
'yesterday',
'reported',
'story',
...
```

LDA implementation

Cosine Similarity

LDA implementation

```
raw_m1 = tokenized_texts_clean
 2
3
       # assign a token_id to each word
4
       id2word_m1 = corpora.Dictionary(raw_m1)
       # represent each text by (token id. token count) tuples
5
6
       ldacorpus m1 = [id2word m1.doc2bow(text) for text in raw m1]
8
       #estimate the model
9
       lda m1 = models.LdaModel(ldacorpus m1, id2word=id2word m1, num topics=10)
10
       lda_m1.print_topics()
```

```
[(0,
'0.015*"trump" + 0.012*"said" + 0.006*"president" + 0.006*"people" + 0.004*"cnn" + 0.004*"us" +

0.004*"house" + 0.004*"news" + 0.003*"also" + 0.003*"twitter"'),
(1,
'0.010*"said" + 0.008*"trump" + 0.004*"one" + 0.004*"people" + 0.004*"us" + 0.004*"president" +

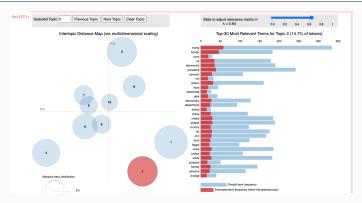
0.004*"would" + 0.003*"media" + 0.003*"also" + 0.003*"new"'),
(2,
'0.011*"trump" + 0.009*"said" + 0.007*"president" + 0.005*"would" + 0.004*"people" + 0.004*"us"

+ 0.003*"also" + 0.003*"like" + 0.003*"news" + 0.003*"state"'),
(3,
'0.010*"trump" + 0.006*"president" + 0.005*"said" + 0.004*"would" + 0.004*"us" + 0.003*"also" +
```

Visualization with pyldavis

Cosine Similarity

```
import pyLDAvis
import pyLDAvis.gensim_models as gensimvis
# first estiate gensim model, then:
vis_data = gensimvis.prepare(lda_m1,ldacorpus_m1,id2word_m1)
pyLDAvis.display(vis_data)
```



Code examples

https://github.com/annekroon/gesis-machine-learning/blob/main/day3/excercise-afternoon/lda.ipynb

Topic modelling

Choosing the best (or a good) topic model

Choosing the best (or a good) topic model

- There is no single best solution (e.g., do you want more coarse of fine-grained topics?)
- Non-deterministic

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- Very sensitive to preprocessing choices
- Interplay of both metrics and (qualitative) interpretability

See for more elaborate guidance:

Maier, D., Waldherr, A., Miltner, P., Wiedemann, G., Niekler, A., Keinert, A., . . . Adam, S. (2018). Applying LDA Topic Modeling in Communication Research: Toward a Valid and Reliable Methodology. Communication Methods and Measures, 12(2–3), 93–118. doi:10.1080/19312458.2018.1430754

Evaluation metrics

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qualitative: human judgement

Observation and interpretation based: observe the top N words in your topic, and evaluate the quality of the coherence of the topic. Can you identify words that do not belong to a topic?

quantitative: coherence

- mean coherence of the whole model: attempts to quantify the interpretability
- coherence per topic: allows to get topics that are most likely to be coherently interpreted (.top_topics())

So, how do we do this?

Cosine Similarity

- Estimate multiple models, store the metrics for each model, and then compare them (numerically, or by plotting)
- Idea: We select some candidate models, and then look whether they can be interpreted.
- But what can we tune?

Choosing k: How many topics do we want?

• Typical values: 10 < k < 200

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- Too low: losing nuance, so broad it becomes meaningless
- Too high: picks up tiny pecularities instead of finding general patterns
- There is no inherent ordering of topics
- We can throw away or merge topics later, so if out of k=50 topics 5 are not interpretable and a couple of others overlap, it still may be a good model

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- The higher α , the more topics per document
- Default: 1/k

Cosine Similarity

• But: We can explicitly change it, or – really cool – even learn α from the data (alpha = "auto")

```
mylda =LdaModel(corpus=tfidfcorpus[ldacorpus], id2word=id2word, num_topics=50, alpha='auto',
  passes=10)
```

Topic modelling

Using topic models

You got your model – what now?

- 1. Assign topic scores to documents
- 2. Label topics
- 3. Merge topics, throw away boilerplate topics and similar (manually, or aided by cluster analysis)
- 4. Compare topics between, e.g., outlets
- 5. or do some time-series analysis.

Example: Tsur, O., Calacci, D., & Lazer, D. (2015). A Frame of Mind: Using Statistical Models for Detection of Framing and Agenda Setting Campaigns. Proceedings of the 53rd Annual Meeting of the Association for Computational Linguistics and the 7th International Joint Conference on Natural Language Processing (pp. 1629-1638).

Next steps

Exercise for this week's lab session

- Work through the example notebook on cosine and soft cosine:
- https://github.com/annekroon/CCS-2/blob/main/week04/
- exercises/cosine-similarity-basics.ipynb Work through the example notebook on LDA:
- https://github.com/annekroon/CCS-2/blob/main/week04/ exercises/topic-modelling.ipynb

https://github.com/annekroon/CCS-2/blob/main/week04/

• Optional: overtime analysis of cosine or soft cosine:

exercises/OPTIONAL_overtime_similarity.ipynb

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Topic modellin 00000 0000000000 000000 Next steps

References

Have fun!

References i

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