

## CRYPTOGRAPHY HANDOUT 03

### SUBSTITUTION CIPHER

#### SUBSTITUTION EXAMPLE

The following example is from Douglas Stinson's Cryptography: Theory and Practice.

Given the ciphertext (encrypted with a substitution cipher):

YIFQFMZRWQFYVECFMDZPCVMRZWNMDZVEJBTXCDDUMJ  
NDIFEFMZCDMQZKCEYFCJMYRNCWJCSZREXCHZUNMXZ  
NZUCDRJXYYSMRTMEYIFZWDYVZVYFZUMRZCRWNZDZJJ  
XZWGCHSMRNMDHNCMFQCHZJMXJZWIEJYUCFWDJNZDIR

The following steps will walk through how to do the cryptanalysis.

1. Do a frequency count for the text.

| Letter | Count | Letter | Count |
|--------|-------|--------|-------|
| A      |       | N      |       |
| B      |       | O      |       |
| C      |       | P      |       |
| D      |       | Q      |       |
| E      |       | R      |       |
| F      |       | S      |       |
| G      |       | T      |       |
| H      |       | U      |       |
| I      |       | V      |       |
| J      |       | W      |       |
| K      |       | X      |       |
| L      |       | Y      |       |
| M      |       | Z      |       |

2. Which letter occurs most? This letter likely corresponds with e, the most frequency-occurring English letter.

3. The next set of most-frequent letters aren't as easy to match up. Let's look at the **bigrams** or digrams instead (pairs of letters). Count the following bigrams:

| Bigram | Count | Bigram | Count |
|--------|-------|--------|-------|
| DZ     |       | ZW     |       |
| NZ     |       | ZU     |       |

4. You should find that DZ and ZW occur the most often, so what are some guesses (based on the English language) that the letters corresponding to D and W are what? Use the bigram frequency table for reference:

|         |         |         |
|---------|---------|---------|
| th 1.52 | en 0.55 | ng 0.18 |
| he 1.28 | ed 0.53 | of 0.16 |
| in 0.94 | to 0.52 | al 0.09 |
| er 0.94 | it 0.50 | de 0.09 |
| an 0.82 | ou 0.50 | se 0.08 |
| re 0.68 | ea 0.47 | le 0.08 |
| nd 0.63 | hi 0.46 | sa 0.06 |
| at 0.59 | is 0.46 | si 0.05 |
| on 0.57 | or 0.43 | ar 0.04 |
| nt 0.56 | ti 0.34 | ve 0.04 |
| ha 0.56 | as 0.33 | ra 0.04 |
| es 0.56 | te 0.27 | ld 0.02 |
| st 0.55 | et 0.19 | ur 0.02 |

(From [https://en.wikipedia.org/wiki/Bigram#Bigram\\_frequency\\_in\\_the\\_English\\_language](https://en.wikipedia.org/wiki/Bigram#Bigram_frequency_in_the_English_language).)

5. We have a choice here. Suppose W corresponds to the plaintext letter of d. Since ZRW and RZW both occur at the beginning, and since RW occurs again later on and *nd* is a common digram, let's try saying that R corresponds to n. At this point, we have 3 letters deciphered. What does your text look like so far?

YIFQFMZRWQFYVECFMDZPCVMRZWNMDZVEJBTXCDDUMJ

NDIFEFMZCDMQZKCEYFCJMYRNCWJCSZREXCHZUNMXZ

NZUCDRJXYYSMRTMEYIFZWDYVZVYFZUMRZCRWNZDZJJ

XZWGCHSMRNMDHNCMFQCHZJMXJZWIEJYUCFWDJNZDIR

6. We can keep looking at bigrams and frequently-occurring letters to slowly fill in the rest of the letters until we get to the following message. Can you fill in the final letters?

o-r-riend-ro--arise-a-inedhise--t---ass-it  
hs-r-riseasi-e-a-orationhadta-en--ace-hi-e  
he-asnt-oo-in-i-o-redso-e-ore-ineandhesett  
-ed-ac-inhischair-aceti-ted--to-ardsthes-n