# Analysis of SARSA on Windy Gridworld

Sushant Shambharkar - 153050081

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# 1 Introduction

This report involve analysis of variants of SARSA applied on Windy Girdworld.

Following figure shows a standard gridworld, with start and goal states, but with one difference: there is a crosswind upward through the middle of the grid. The actions are the standard four—up, down, right, and left—but in the middle region the resultant next states are shifted upward by a "wind," the strength of which varies from column to column. The strength of the wind is given below each column, in number of cells shifted upward. For example, if you are one cell to the right of the goal, then the action left takes you to the cell just above the goal. Let us treat this as an undiscounted episodic task, with constant rewards of until the goal state is reached.[1]

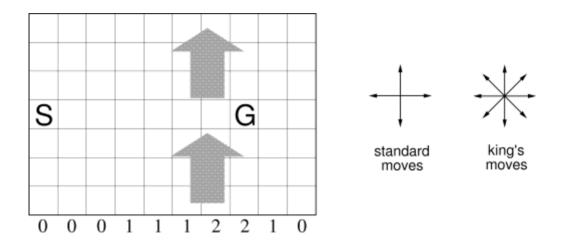


Figure 1: Gridworld in which movement is altered by a location-dependent, upward "wind." [1]

## 2 Observations

UCB and  $\epsilon$ -soft performed equally where major efficiency found in SARSA( $\lambda$ ) with  $\lambda = 0.1$ . Combination of SARSA( $\lambda$ ) and UCB performed well in "Stochastic Wind with Kings Moves" almost coverged at 500th Episode.

# 2.1 Data "D1.txt"

# Non-Stochastic Wind with Standard Moves 200 Time-Steps SARSA(0), $\varepsilon$ -Soft $\alpha$ =0.5 $\gamma = 1.0$ ε=0.1 150 Episodes 100 50 0 4000 Time Steps 1000 2000 3000 5000 6000 7000 8000

Figure 2: Episodes Vs Time-Step : Standard move

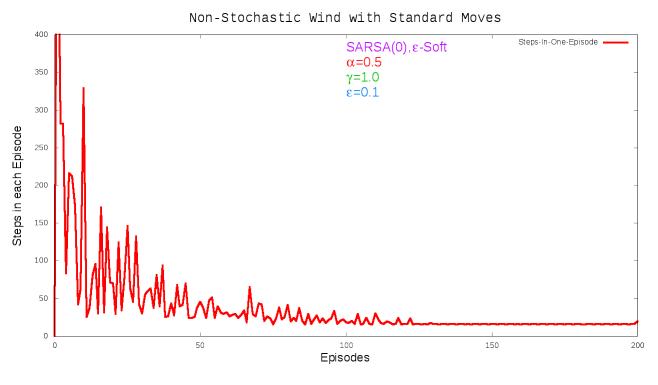


Figure 3: Episodes Vs Steps-in-each-episode : Standard move

- -13.91 -13.45 -12.84 -12.0 -11.0 -10.0 -09.0 -08.0 -07.0 -06.0
- -13.99 -13.51 -12.87 -11.99 -11.0 -10.0 -09.0 -08.0 -07.0 -05.0
- $\hbox{-}14.0 \hbox{ -}14.0 \hbox{ -}13.0 \hbox{ -}12.0 \hbox{ -}11.0 \hbox{ -}9.99 \hbox{ -}8.99 \hbox{ -}3.62 \hbox{ -}04.8 \hbox{ -}04.0$
- $-15.0 \ -14.0 \ -13.0 \ -12.0 \ -10.95 \ -9.94 \ -08.9 \ 00000 \ -3.13 \ -3.04$
- $\hbox{-}14.2\hbox{ --}13.49\hbox{ --}12.62\hbox{ --}11.87\hbox{ --}10.78\hbox{ --}9.73\hbox{ }00000\hbox{ --}00.5\hbox{ --}01.0\hbox{ --}02.0$
- $\hbox{-}13.46 \hbox{-}12.96 \hbox{-}12.25 \hbox{-}11.56 \hbox{-}10.37 \hbox{-}00000 \hbox{-}00000 \hbox{-}00000 \hbox{-}0.94 \hbox{-}01.5$
- $\hbox{-}12.95 \hbox{-}12.43 \hbox{-}11.7 \hbox{-}10.96 \hbox{-}00000 \hbox{-}00000 \hbox{-}00000 \hbox{-}00000 \hbox{-}00000 \hbox{-}0.88$

## 2.2 Data "D2.txt"

## Non-Stochastic Wind with King's Moves

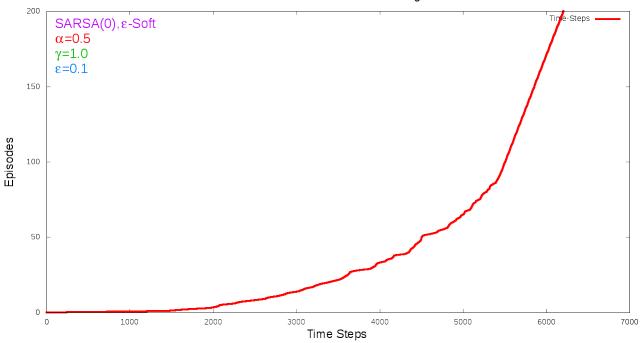


Figure 4: Episodes Vs Time-Step: King's move

## Non-Stochastic Wind with King's Moves

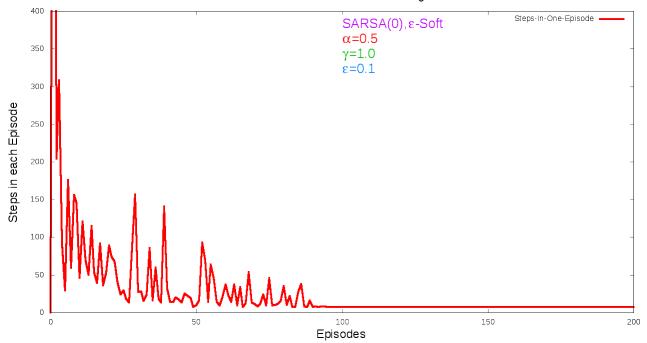


Figure 5: Episodes Vs Steps-in-each-episode: King's move

- -5.69 -5.76 -6.34 -6.97 -7.36 -6.91 -5.99 -05.0 -4.72 -3.97
- -5.66 -5.79 -5.78 -6.05 -06.0 -6.17 -5.65 -05.0 -04.0 -03.0
- $-5.71 \, -06.0 \, -5.46 \, -5.46 \, -5.46 \, -5.34 \, -4.85 \, -4.92 \, -3.49 \, -2.51 \, -02.0$
- $\hbox{-06.0 -} 5.36 \hbox{-05.0 -} 5.11 \hbox{-4.52 -} 3.85 \hbox{-3.63 00000 -} 01.0 \hbox{-1.22}$
- -5.34 -5.24 -4.52 -04.0 -03.0 -02.0 -01.0 00000 -00.5 -00.5
- -4.97 -4.81 -4.38 -3.78 -2.85 -1.91 -0.94 00000 00000 00000
- $\hbox{-}4.88 \hbox{-}4.67 \hbox{-}4.24 \hbox{-}3.48 00000 00000 00000 00000 00000 00000}$

# 2.3 Data "D3.txt"

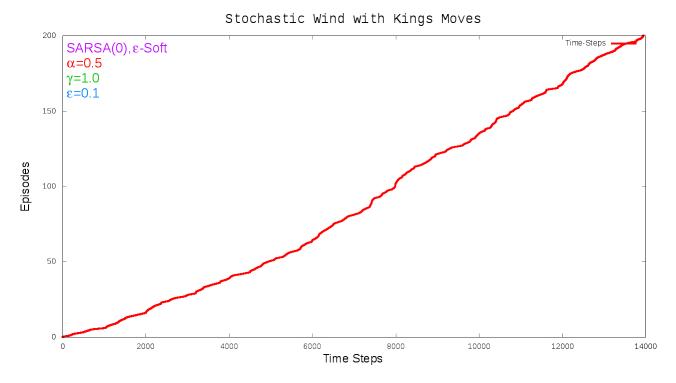


Figure 6: Episodes Vs Time-Step : Stochastic King's move

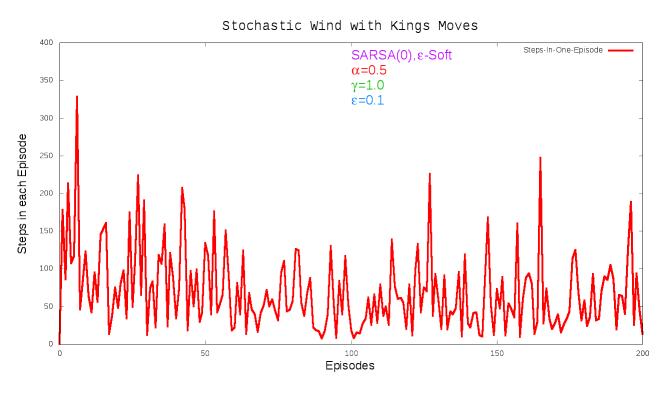


Figure 7: Episodes Vs Steps-in-each-episode : Stochastic King's move

- $\hbox{-}11.53 \hbox{-}11.74 \hbox{-}11.87 \hbox{-}11.93 \hbox{-}12.46 \hbox{-}11.37 \hbox{-}11.82 \hbox{-}10.44 \hbox{-}11.45 \hbox{-}10.23$
- $\hbox{-}11.6 \hbox{-}11.58 \hbox{-}11.57 \hbox{-}11.91 \hbox{-}11.81 \hbox{-}12.17 \hbox{-}6.49 \hbox{-}11.17 \hbox{-}10.65 \hbox{-}9.18$
- $\hbox{-}11.44 \hbox{-}11.9 \hbox{-}11.3 \hbox{-}11.5 \hbox{-}11.12 \hbox{-}11.36 \hbox{-}11.12 \hbox{-}11.25 \hbox{-}9.48 \hbox{-}8.33$
- $\hbox{-}11.64 \hbox{-}11.22 \hbox{-}11.14 \hbox{-}11.15 \hbox{-}10.69 \hbox{-}10.4 \hbox{-}10.05 \hbox{-}00000 \hbox{-}9.14 \hbox{-}8.38$
- -11.01 -10.9 -10.54 -9.78 -9.67 -7.03 -7.27 -9.84 -2.82 -7.88
- $\hbox{-}10.77 \hbox{-}10.49 \hbox{-}10.25 \hbox{-}9.59 \hbox{-}6.36 \hbox{-}6.57 \hbox{-}06.4 \hbox{-}6.43 \hbox{-}7.53 \hbox{-}7.15$
- -10.6 10.42 9.97 8.86 6.79 5.07 3.28 3.77 6.85 6.81

## 2.4 Data "D4.txt"

#### Non-Stochastic Wind with Standard Moves

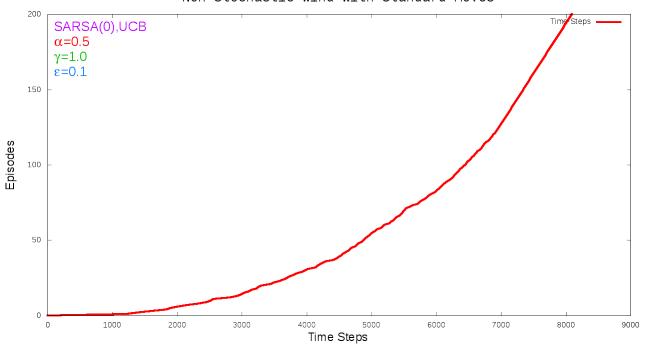


Figure 8: Episodes Vs Time-Step: Standard move

#### Non-Stochastic Wind with Standard Moves

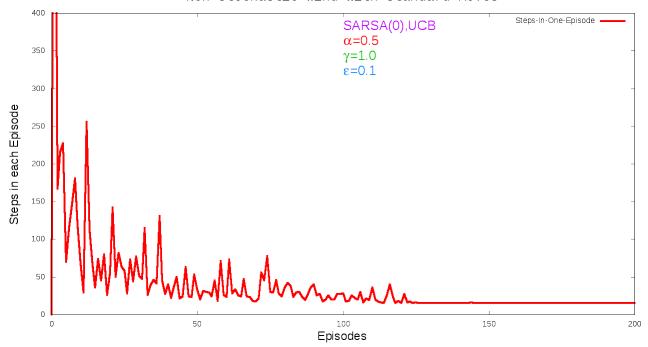


Figure 9: Episodes Vs Steps-in-each-episode: Standard move

- $\hbox{-}13.9 \hbox{-} 13.85 \hbox{-} 13.24 \hbox{-} 12.52 \hbox{-} 11.39 \hbox{-} 10.15 \hbox{-} 09.0 \hbox{-} 08.0 \hbox{-} 07.0 \hbox{-} 06.0$
- $\hbox{-}14.1 \hbox{ -}13.69 \hbox{ -}13.3 \hbox{ -}12.31 \hbox{ -}11.06 \hbox{ -}10.0 \hbox{ -}9.35 \hbox{ -}8.24 \hbox{ -}7.22 \hbox{ -}05.0$
- -14.34 -14.3 -13.18 -12.07 -11.0 -10.53 -9.26 -6.37 -5.75 -04.0
- $\hbox{-}15.0\hbox{ }\hbox{-}14.0\hbox{ }\hbox{-}13.0\hbox{ }\hbox{-}12.0\hbox{ }\hbox{-}11.6\hbox{ }\hbox{-}9.98\hbox{ }\hbox{-}9.05\hbox{ }00000\hbox{ }\hbox{-}4.92\hbox{ }\hbox{-}03.0$
- $\hbox{-}14.39 \hbox{-}13.67 \hbox{-}12.78 \hbox{-}12.24 \hbox{-}10.88 \hbox{-}9.56 \hbox{-}00000 \hbox{-}0.97 \hbox{-}01.0 \hbox{-}02.0$
- -13.83 -13.2 -12.25 -11.78 -10.37 00000 00000 00000 -1.81 -2.34
- -13.32 -12.57 -11.72 -10.93 00000 00000 00000 00000 -0.75 -1.71

# 2.5 Data "D5.txt"

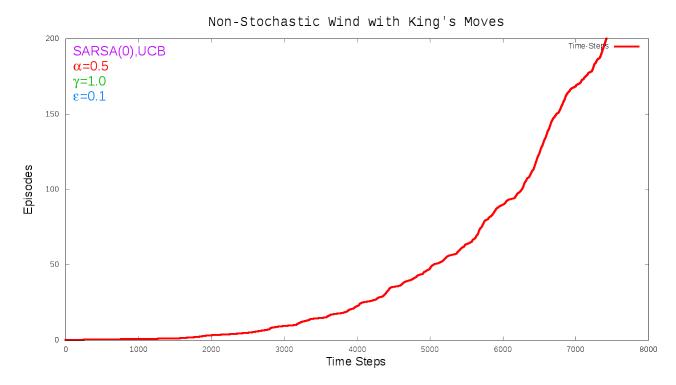


Figure 10: Episodes Vs Time-Step : King's move

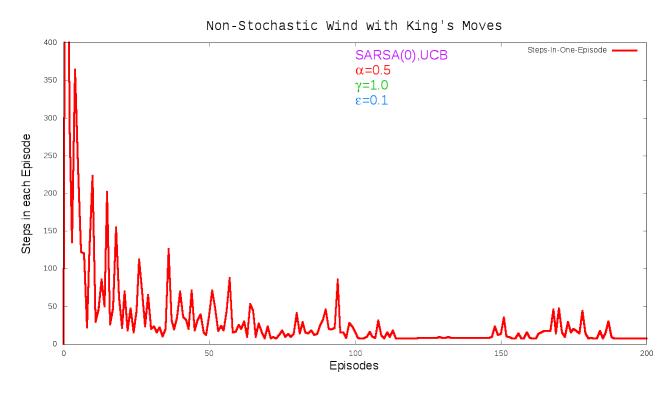


Figure 11: Episodes Vs Steps-in-each-episode : King's move

- -7.54 -7.58 -7.73 -8.18 -07.9 -07.0 -06.0 -05.0 -5.25 -04.1
- -7.31 -7.23 -07.5 -7.72 -7.28 -6.93 -06.0 -5.08 -04.0 -03.0
- -7.43 -7.69 -7.03 -07.3 -6.85 -6.33 -5.83 -04.6 -3.35 -02.0
- $\hbox{-}7.07 \hbox{-}6.93 \hbox{-}6.52 \hbox{-}6.66 \hbox{-}06.0 \hbox{-}5.23 \hbox{-}5.01 \hbox{00000} \hbox{-}01.0 \hbox{-}1.65$
- -06.7 -6.03 -5.19 -5.64 -4.63 -02.0 -01.0 -00.5 -0.75 -0.88
- -6.36 -6.11 -5.01 -04.0 -03.0 -1.91 -0.97 00000 00000 00000
- $\hbox{-}6.38 \hbox{-}5.91 \hbox{-}5.27 \hbox{-}4.64 \hbox{00000} \hbox{00000} \hbox{00000} \hbox{00000} \hbox{00000} \hbox{00000}$

## 2.6 Data "D6.txt"

# Stochastic Wind with Kings Moves

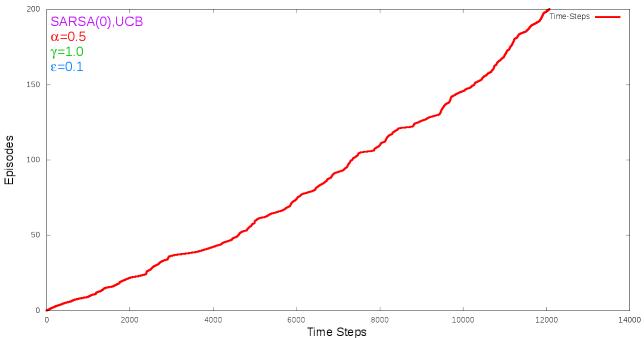


Figure 12: Episodes Vs Time-Step: Stochastic King's move)

## Stochastic Wind with Kings Moves

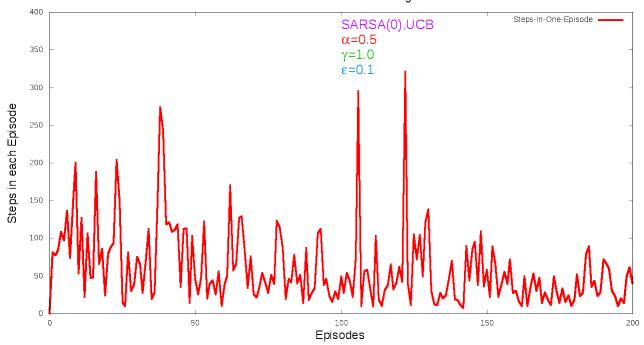


Figure 13: Episodes Vs Steps-in-each-episode : Stochastic King's move)

- $\hbox{-}11.05 \hbox{-}11.13 \hbox{-}11.28 \hbox{-}11.35 \hbox{-}11.24 \hbox{-}9.29 \hbox{-}9.32 \hbox{-}9.19 \hbox{-}9.01 \hbox{-}7.35$
- $\hbox{-}10.84 \hbox{-}10.73 \hbox{-}10.74 \hbox{-}10.84 \hbox{-}10.34 \hbox{-}10.7 \hbox{-}8.81 \hbox{-}8.86 \hbox{-}8.44 \hbox{-}6.84$
- $\hbox{-}10.81 \hbox{-}11.29 \hbox{-}10.47 \hbox{-}10.57 \hbox{-}9.83 \hbox{-}9.68 \hbox{-}8.53 \hbox{-}6.77 \hbox{-}3.89 \hbox{-}07.5$
- $\hbox{-}11.3 \hbox{-} 9.19 \hbox{-} 10.41 \hbox{-} 10.13 \hbox{-} 09.3 \hbox{-} 09.0 \hbox{-} 8.65 \hbox{-} 00000 \hbox{-} 7.01 \hbox{-} 06.5$
- $\hbox{-}10.33 \hbox{-}10.16 \hbox{-}8.71 \hbox{-}9.36 \hbox{-}9.28 \hbox{-}7.05 \hbox{-}5.91 \hbox{-}7.22 \hbox{-}6.27 \hbox{-}5.42$
- $-9.98 \; -9.92 \; -9.27 \; -8.07 \; -6.72 \; -3.59 \; -3.56 \; -01.9 \; -03.8 \; -05.0$
- $\hbox{-}9.82 \hbox{-}09.8 \hbox{-}9.35 \hbox{-}8.15 \hbox{-}6.25 \hbox{-}1.55 \hbox{-}00000 \hbox{-}2.11 \hbox{-}4.44 \hbox{-}4.46$

# 2.7 Data "D7.txt"

# Non-Stochastic Wind with Standard Moves 200 SARSA( $\lambda$ ), $\epsilon$ -Soft $\alpha$ =0.5 $\gamma = 1.0$ $\dot{\epsilon}$ =0.1 $\lambda = 0.1$ 150 100 50 1000 2000 3000 4000 5000 6000 7000 8000 Time Steps

Figure 14: Episodes Vs Time-Step : Standard move

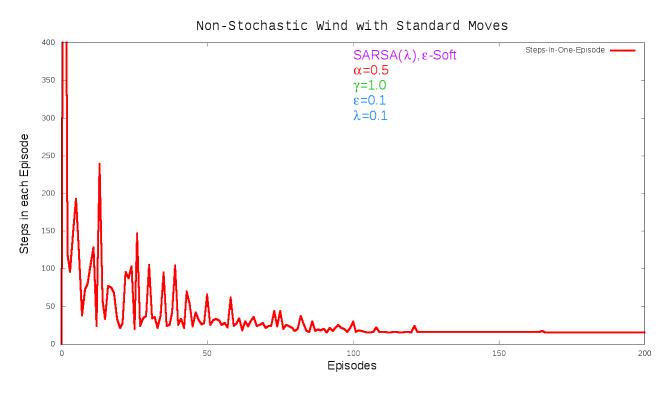


Figure 15: Episodes Vs Steps-in-each-episode : Standard move

- -13.81 -13.68 -12.96 -12.05 -11.02 -10.0 -09.0 -08.0 -07.0 -06.0
- -13.84 -13.59 -13.0 -12.03 -11.0 -10.0 -9.04 -8.03 -7.03 -05.0
- $\hbox{-}14.03 \hbox{-}14.0 \hbox{-}13.0 \hbox{-}12.0 \hbox{-}11.0 \hbox{-}10.05 \hbox{-}9.02 \hbox{-}2.72 \hbox{-}3.94 \hbox{-}04.0$
- $\hbox{-}15.0 \hbox{-}14.0 \hbox{-}13.0 \hbox{-}12.0 \hbox{-}11.05 \hbox{-}9.94 \hbox{-}8.76 \hbox{-}000.0 \hbox{-}3.35 \hbox{-}03.0$
- $\hbox{-}14.19 \hbox{-}13.51 \hbox{-}12.74 \hbox{-}12.02 \hbox{-}10.76 \hbox{-}9.41 \hbox{-}000.0 \hbox{-}000.0 \hbox{-}01.0 \hbox{-}02.0$
- $\hbox{-}13.57 \hbox{-}12.93 \hbox{-}12.15 \hbox{-}11.47 \hbox{-}10.18 \hbox{-}000.0 \hbox{-}000.0 \hbox{-}000.0 \hbox{-}0.87 \hbox{-}1.41$
- -13.17 -12.48 -11.83 -11.04 000.0 000.0 000.0 000.0 000.0 -1.06

# 2.8 Data "D8.txt"

## Non-Stochastic Wind with King's Moves

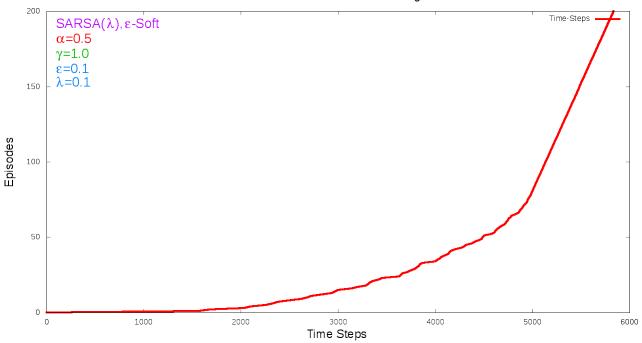


Figure 16: Episodes Vs Time-Step: King's move

## Non-Stochastic Wind with King's Moves

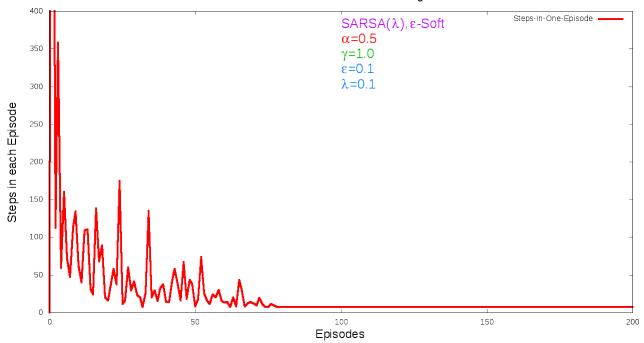


Figure 17: Episodes Vs Steps-in-each-episode : King's move

- -5.74 -5.88 -6.55 -7.15 -7.53 -7.02 -6.04 -5.05 -5.06 -04.2
- -5.63 -5.76 -5.71 -6.11 -06.3 -6.33 -5.94 -5.05 -4.04 -3.04
- $\hbox{-05.7 -06.0 -5.47 -5.54 -5.49 -05.2 -4.41 -3.67 -02.8 -2.04}$
- -06.0 -5.48 -05.0 -4.98 -4.36 -3.92 -3.59 000.0 -1.03 -1.12
- $\hbox{-}5.32 \hbox{-}5.13 \hbox{-}4.52 \hbox{-}04.0 \hbox{-}03.0 \hbox{-}02.0 \hbox{-}01.0 \hbox{-}000.0 \hbox{-}000.0 \hbox{-}0.57$
- -4.88 -4.69 -4.41 -3.61 -2.67 -1.78 -00.9 000.0 000.0 000.0
- $\hbox{-}4.67 \hbox{ -}4.52 \hbox{ -}04.2 \hbox{ -}3.52 \hbox{ }000.0 \hbox{ }000.0 \hbox{ }000.0 \hbox{ }000.0 \hbox{ }000.0 \hbox{ }000.0$

# 2.9 Data "D9.txt"

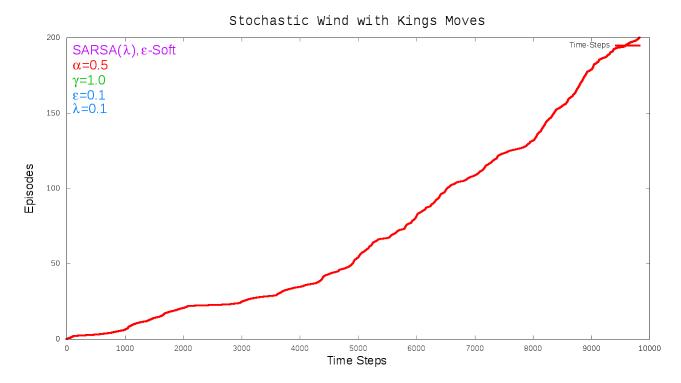


Figure 18: Episodes Vs Time-Step : Stochastic King's move

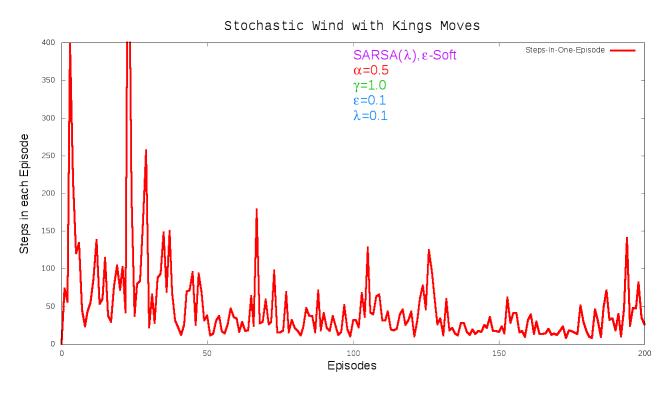


Figure 19: Episodes V<br/>s Steps-in-each-episode : Stochastic King's move

# $\begin{array}{c} \text{State Values} \\ -9.23 \ -9.16 \ -9.48 \ -9.61 \ -09.6 \ -9.03 \ -8.76 \ -7.55 \ -08.4 \ -8.24 \\ -9.11 \ -9.17 \ -9.01 \ -9.02 \ -9.09 \ -8.52 \ -6.57 \ -8.24 \ -8.19 \ -7.38 \\ -9.06 \ -9.49 \ -08.8 \ -8.49 \ -8.14 \ -8.16 \ -7.75 \ -02.5 \ -7.03 \ -6.85 \\ -9.47 \ -8.67 \ -8.61 \ -7.98 \ -08.0 \ -6.96 \ -7.86 \ 000.0 \ -6.64 \ -6.18 \\ -8.74 \ -8.68 \ -7.96 \ -7.73 \ -7.19 \ -6.93 \ -5.53 \ -6.17 \ -3.45 \ -5.43 \\ -8.37 \ -8.15 \ -7.89 \ -7.83 \ -5.38 \ -5.93 \ -1.42 \ -3.91 \ -2.86 \ -4.77 \\ -7.82 \ -7.85 \ -7.46 \ -7.04 \ -5.44 \ -2.46 \ -0.77 \ -0.56 \ -4.26 \ -4.18 \end{array}$

## 2.10 Data "D10.txt"

## Non-Stochastic Wind with Standard Moves

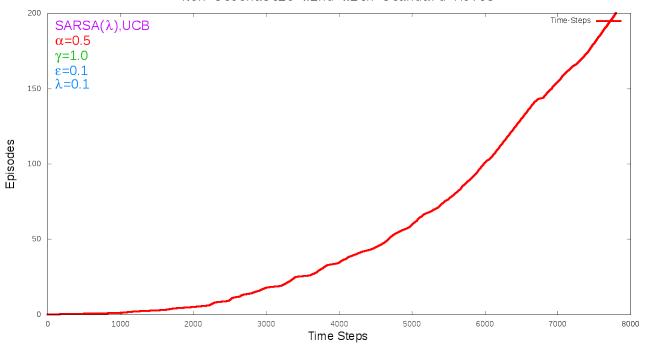


Figure 20: Episodes Vs Time-Step: Standard move

#### Non-Stochastic Wind with Standard Moves

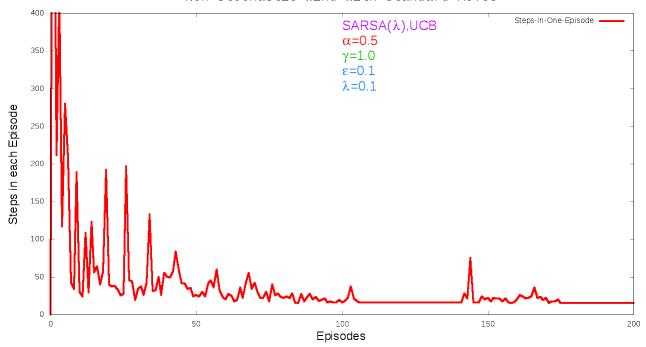


Figure 21: Episodes Vs Steps-in-each-episode: Standard move

- $\hbox{-}14.29 \hbox{-}14.27 \hbox{-}13.49 \hbox{-}12.32 \hbox{-}11.09 \hbox{-}10.02 \hbox{-}09.0 \hbox{-}08.0 \hbox{-}07.0 \hbox{-}06.0$
- $\hbox{-}14.5 \hbox{-} 14.37 \hbox{-} 13.48 \hbox{-} 12.37 \hbox{-} 11.46 \hbox{-} 10.0 \hbox{-} 9.83 \hbox{-} 8.67 \hbox{-} 7.48 \hbox{-} 05.0$
- $-14.69 \ -14.99 \ -13.81 \ -12.71 \ -11.0 \ -10.87 \ -9.13 \ -6.15 \ -6.36 \ -04.0$
- $\hbox{-}15.04 \hbox{-}14.02 \hbox{-}13.01 \hbox{-}12.0 \hbox{-}11.76 \hbox{-}10.27 \hbox{-}8.44 \hbox{-}000.0 \hbox{-}5.69 \hbox{-}03.0$
- $\hbox{-}14.93 \hbox{-}14.19 \hbox{-}13.36 \hbox{-}12.7 \hbox{-}10.84 \hbox{-}8.92 \hbox{-}000.0 \hbox{-}0.88 \hbox{-}01.0 \hbox{-}02.0$
- $\hbox{-}14.02 \hbox{-}13.5 \hbox{-}12.56 \hbox{-}11.86 \hbox{-}9.68 \hbox{-}000.0 \hbox{-}000.0 \hbox{-}000.0 \hbox{-}1.67 \hbox{-}2.68$
- $-13.53 12.91 11.94 10.75 \ 000.0 \ 000.0 \ 000.0 \ 000.0 \ -1.15 1.93$

# 2.11 Data "D11.txt"

# Non-Stochastic Wind with King's Moves 200 $\begin{array}{l} \text{SARSA}(\lambda), \overset{\ }{\text{UCB}} \\ \alpha = 0.5 \end{array}$ Time-Steps $\gamma = 1.0$ $\dot{\epsilon}$ =0.1 $\lambda = 0.1$ 150 100 50 1000 2000 3000 4000 5000 6000 7000 Time Steps

Figure 22: Episodes Vs Time-Step : King's move

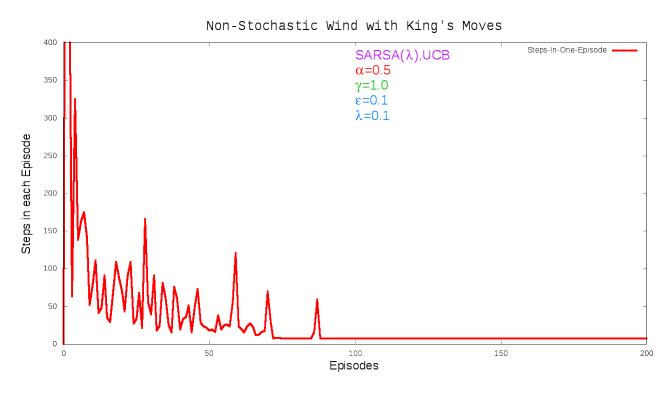


Figure 23: Episodes V<br/>s Steps-in-each-episode : King's move

# $\begin{array}{c} {\rm State\ Values} \\ \phantom{-} -7.35\phantom{-} -7.27\phantom{-} -8.06\phantom{-} -8.72\phantom{-} -8.83\phantom{-} -8.08\phantom{-} -7.05\phantom{-} -6.16\phantom{-} -5.05\phantom{-} -4.05\phantom{-} \\ \phantom{-} -6.93\phantom{-} -6.82\phantom{-} -6.96\phantom{-} -7.46\phantom{-} -07.8\phantom{-} -7.92\phantom{-} -7.27\phantom{-} -6.04\phantom{-} -5.12\phantom{-} -3.05\phantom{-} \\ \phantom{-} -6.74\phantom{-} -06.0\phantom{-} -6.51\phantom{-} -6.74\phantom{-} -6.54\phantom{-} -6.78\phantom{-} -06.2\phantom{-} -4.23\phantom{-} -3.65\phantom{-} -2.03\phantom{-} \\ \phantom{-} -06.0\phantom{-} -6.18\phantom{-} -05.0\phantom{-} -6.06\phantom{-} -5.46\phantom{-} -5.16\phantom{-} -4.33\phantom{-} 000.0\phantom{-} -1.01\phantom{-} -1.97\phantom{-} \\ \phantom{-} -6.11\phantom{-} -5.97\phantom{-} -5.34\phantom{-} -04.0\phantom{-} -03.0\phantom{-} -02.0\phantom{-} -01.0\phantom{-} 000.0\phantom{-} -0.97\phantom{-} -1.07\phantom{-} \\ \phantom{-} -5.73\phantom{-} -5.31\phantom{-} -4.87\phantom{-} -4.09\phantom{-} 03.06\phantom{-} -1.53\phantom{-} -0.52\phantom{-} 000.0\phantom{-} 000.0\phantom{-} 000.0\phantom{-} 000.0\phantom{-} \\ \phantom{-} -5.78\phantom{-} -5.47\phantom{-} -04.8\phantom{-} -4.09\phantom{-} 000.0\phantom{-} 000.0\phantom{-} 000.0\phantom{-} 000.0\phantom{-} 000.0\phantom{-} 000.0\phantom{-} 000.0\phantom{-} \\ \phantom{-} -5.78\phantom{-} -5.47\phantom{-} -04.8\phantom{-} -4.09\phantom{-} 000.0\phantom{-} 000.0\phantom{-} 000.0\phantom{-} 000.0\phantom{-} 000.0\phantom{-} 000.0\phantom{-} \\ \phantom{-} -5.78\phantom{-} -5.47\phantom{-} -04.8\phantom{-} -4.09\phantom{-} 000.0\phantom{-} 000.0\phantom{-} 000.0\phantom{-} 000.0\phantom{-} 000.0\phantom{-} 000.0\phantom{-} \\ \phantom{-} -5.78\phantom{-} -5.47\phantom{-} -04.8\phantom{-} -4.09\phantom{-} 000.0\phantom{-} 000.0\phantom{-} 000.0\phantom{-} 000.0\phantom{-} 000.0\phantom{-} 000.0\phantom{-} \\ \phantom{-} -5.78\phantom{-} -5.47\phantom{-} -04.8\phantom{-} -4.09\phantom{-} 000.0\phantom{-} 000.0\phantom{-} 000.0\phantom{-} 000.0\phantom{-} 000.0\phantom{-} 000.0\phantom{-} 000.0\phantom{-} 000.0\phantom{-} \\ \phantom{-} -5.78\phantom{-} -5.47\phantom{-} -04.8\phantom{-} -4.09\phantom{-} 000.0\phantom{-} 000.0\phantom{$

## 2.12 Data "D12.txt"

## Stochastic Wind with Kings Moves

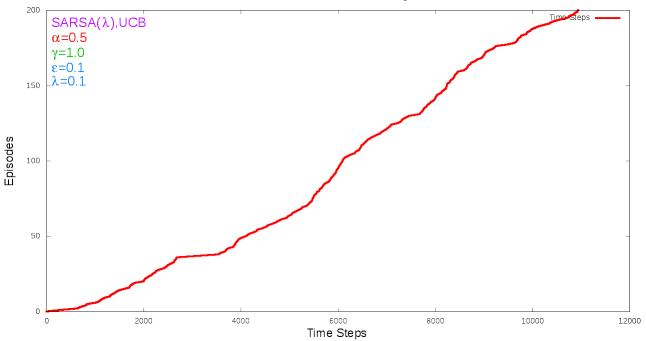


Figure 24: Episodes Vs Time-Step: Stochastic King's move

## Stochastic Wind with Kings Moves

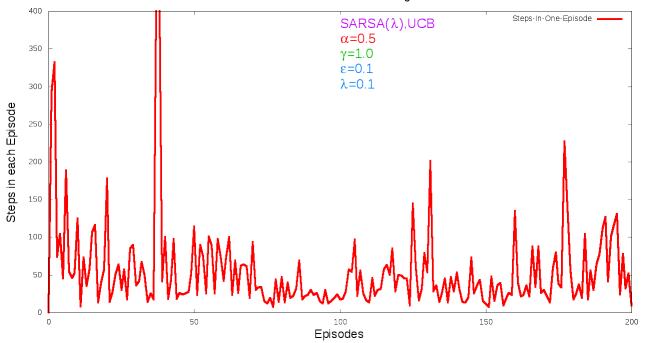


Figure 25: Episodes Vs Steps-in-each-episode: Stochastic King's move

#### State Values

- -10.38 -10.42 -10.91 -11.01 -11.3 -11.33 -10.54 -10.29 -10.36 -10.04
- -10.36 -10.29 -10.52 -10.93 -11.32 -10.35 -10.51 -10.05 -10.28 -8.87
- -10.35 -10.13 -10.14 -10.04 -10.06 -9.39 -3.13 -9.91 -7.98 -6.88
- $\hbox{-}10.32 \hbox{-}09.0 \hbox{-}8.77 \hbox{-}09.9 \hbox{-}09.2 \hbox{-}8.95 \hbox{-}8.73 \hbox{-}000.0 \hbox{-}8.27 \hbox{-}4.59$
- $\hbox{-}9.93 \hbox{-}9.57 \hbox{-}7.78 \hbox{-}9.16 \hbox{-}7.54 \hbox{-}6.89 \hbox{-}5.44 \hbox{-}7.15 \hbox{-}5.35 \hbox{-}5.84$
- -09.5 -8.94 -7.99 -6.73 -4.55 -03.7 -4.67 -5.06 -4.95 -4.85
- $\hbox{-}09.1 \hbox{-}08.8 \hbox{-}7.58 \hbox{-}7.79 \hbox{-}3.86 \hbox{-}02.8 \hbox{-}1.27 \hbox{-}0.64 \hbox{-}3.15 \hbox{-}4.35$

# 3 Conclusion

 $SARSA(\lambda)$  performs better than SARSA(0) at the cost of higher complexity.

## References

[1] Sarsa: On-policy td control.