

# Modeling Household Carbon Footprints: Methods, Metrics, and Estimation Frameworks

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# Overview

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- ① Introduction
- ② Methods & Applications
- ③ Responsibility & Policy Implications
- ④ Conclusion

# Motivation

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- **Contribution:** This study systematically compares four models, namely the GHG Protocol, Life-Cycle Assessment, Environmentally Extended Input-Output Analysis, and general equilibrium model of Hakenes–Schliephake to assess attribution differences, empirical consequences, and policy alignment.

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- ③ How do attribution methods shape policy and equity outcomes?

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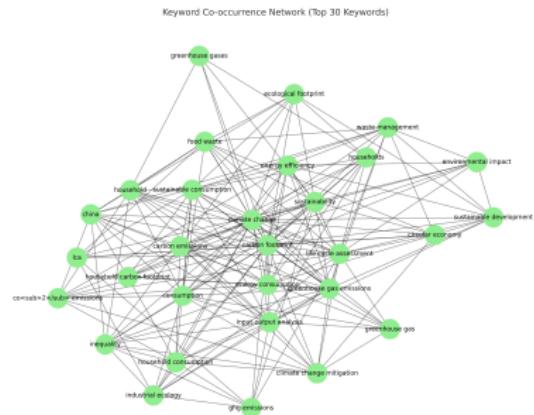
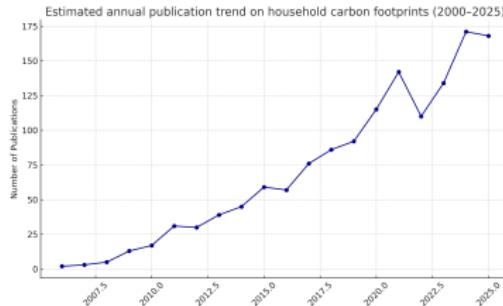
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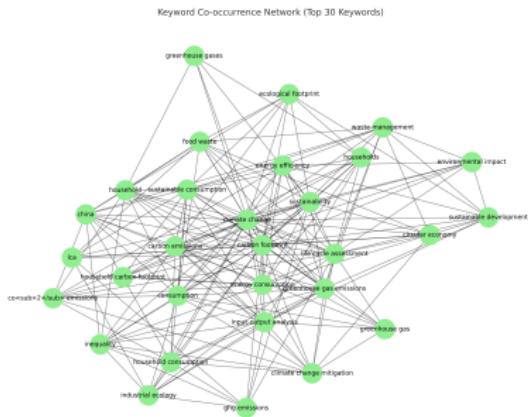
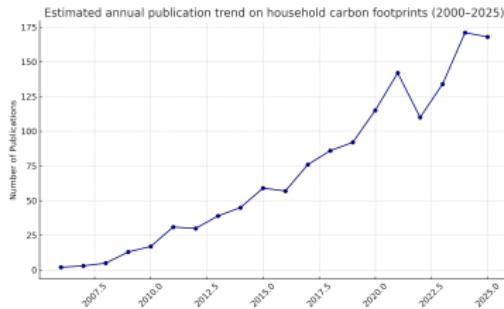
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- Top Journals: *Journal of Cleaner Production*, *Science of the Total Environment*, and *Environmental Science & Technology*
- Top institutions: University of Tokyo, Sun Yat-sen University, University of Maryland.

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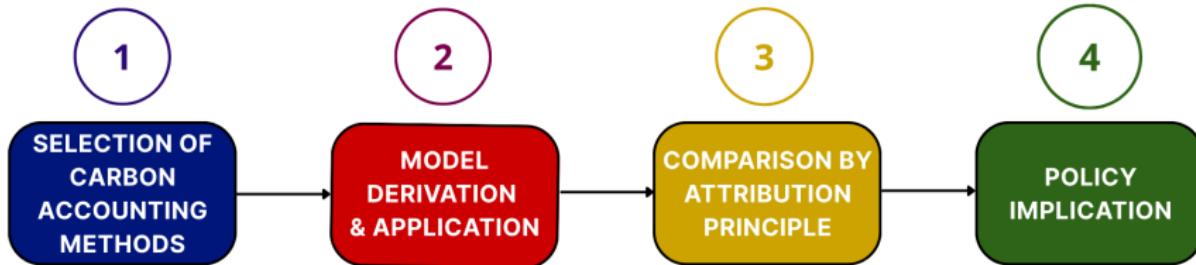
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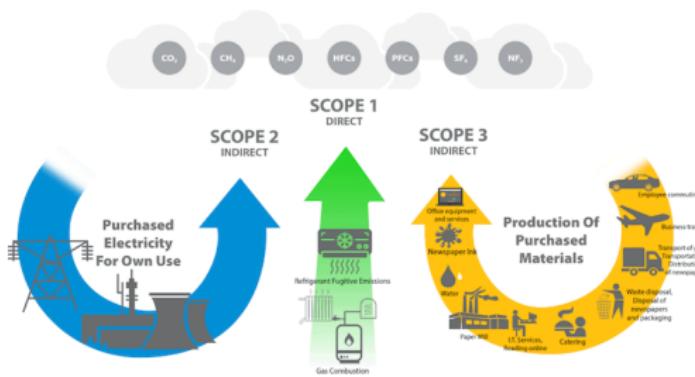


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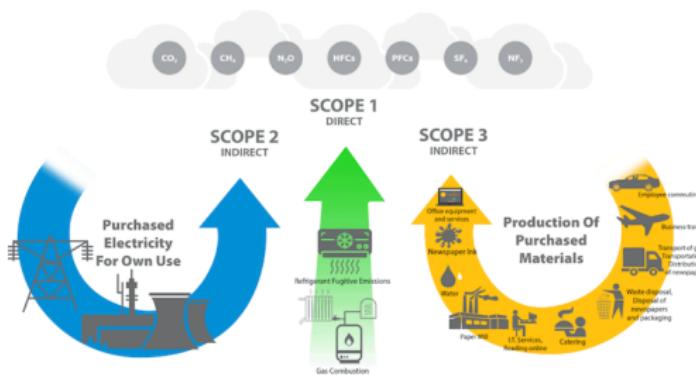
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## Formulation:

$$CF_{\text{household}} = E_{\text{Scope 1}} + E_{\text{Scope 2}} + E_{\text{Scope 3}}, \quad E_i = \sum_j Q_{ij} \cdot EF_{ij}$$

where  $Q_{ij}$  is the activity level and  $EF_{ij}$  is the emission factor for activity  $j$  under scope  $i$ .

# GHG Protocol – Empirical Application (Spain, 2022)

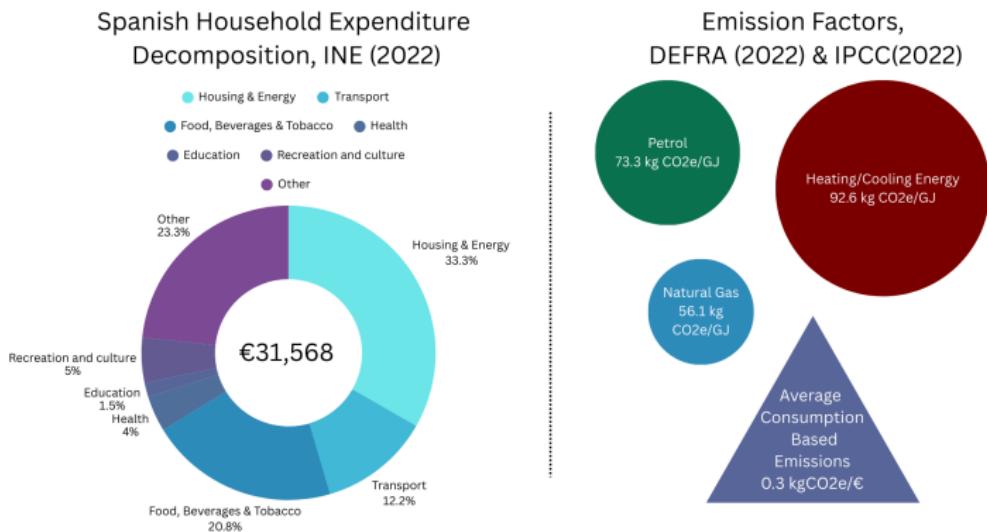
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Scope 1	Direct fuel use (transport + heating)	1,114.83	9.4%
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**Conclusion:** The GHG Protocol effectively captures direct emissions but underestimates total responsibility unless Scope 3 is comprehensively integrated.

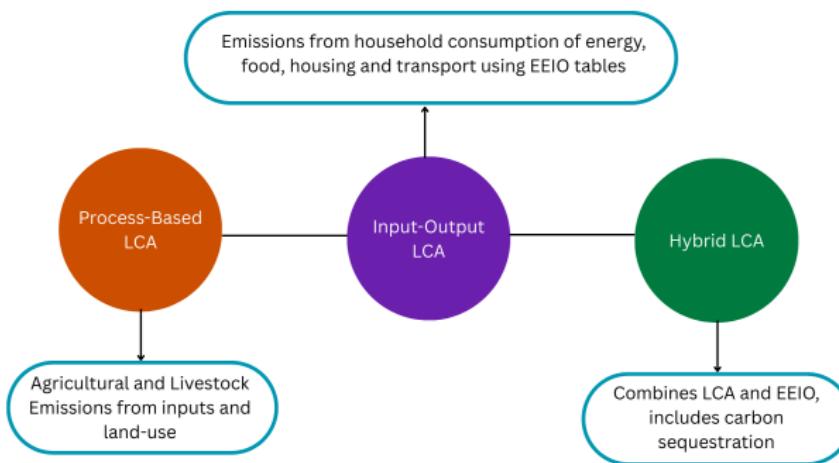
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- This method captures both direct and embodied emissions by integrating three complementary approaches:



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**Implication:** The Hybrid LCA structure reduces truncation error and better reflects household-level carbon responsibility particularly in domains such as food, housing, and land use.

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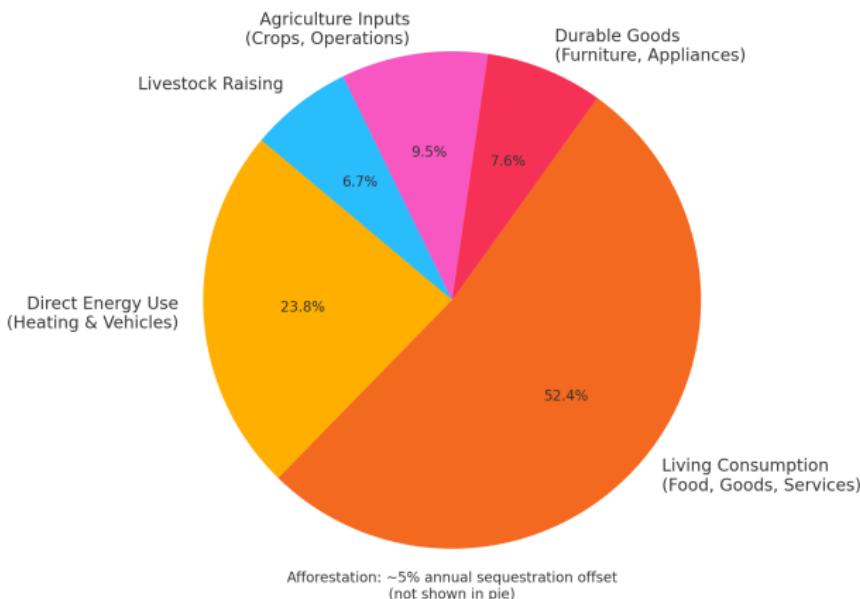
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Illustrative Breakdown of Household Carbon Footprint  
(adapted from Peng et al. 2021 & Notarnicola et al. 2017)



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**Core Identity:**

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**Components:**

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## Model Assumptions and Stability:

- Fixed production coefficients (Leontief structure)
- No substitution across sectors or inputs
- The matrix **A** must satisfy  $\rho(\mathbf{A}) < 1$  for stability
- Empirically:  $\sum_i A_{ij} < 1$  for all  $j$

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## Tier 3 – Indirect Supply Chain:

$$\mathbf{E}_3 = \mathbf{C} \cdot [(\mathbf{I} - \mathbf{M})(\mathbf{I} - \mathbf{A})]^{-1} \cdot [(\mathbf{I} - \mathbf{M}) \cdot \mathbf{F} + \mathbf{EX}]$$

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**Note:** Import-adjusted tiers ensure that emissions are attributed to domestic demand.

Enables national-scale footprint analysis with high coverage.

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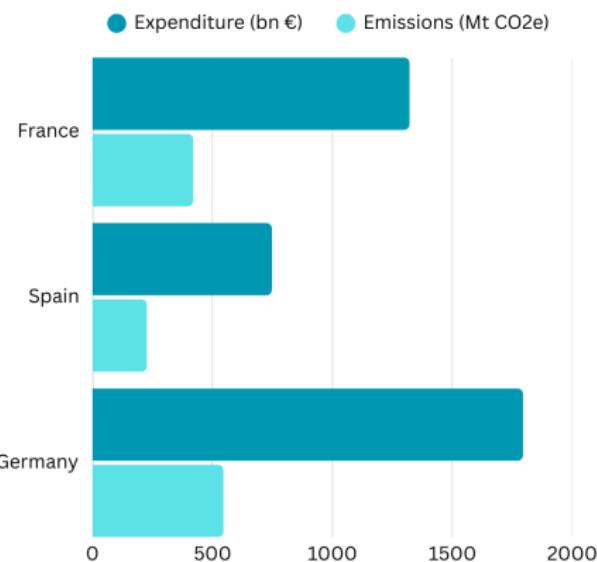
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Total Estimated Household Carbon Footprints (2021)



Source: Eurostat (2021), EXIOBASE (2025);  
Author's calculations.

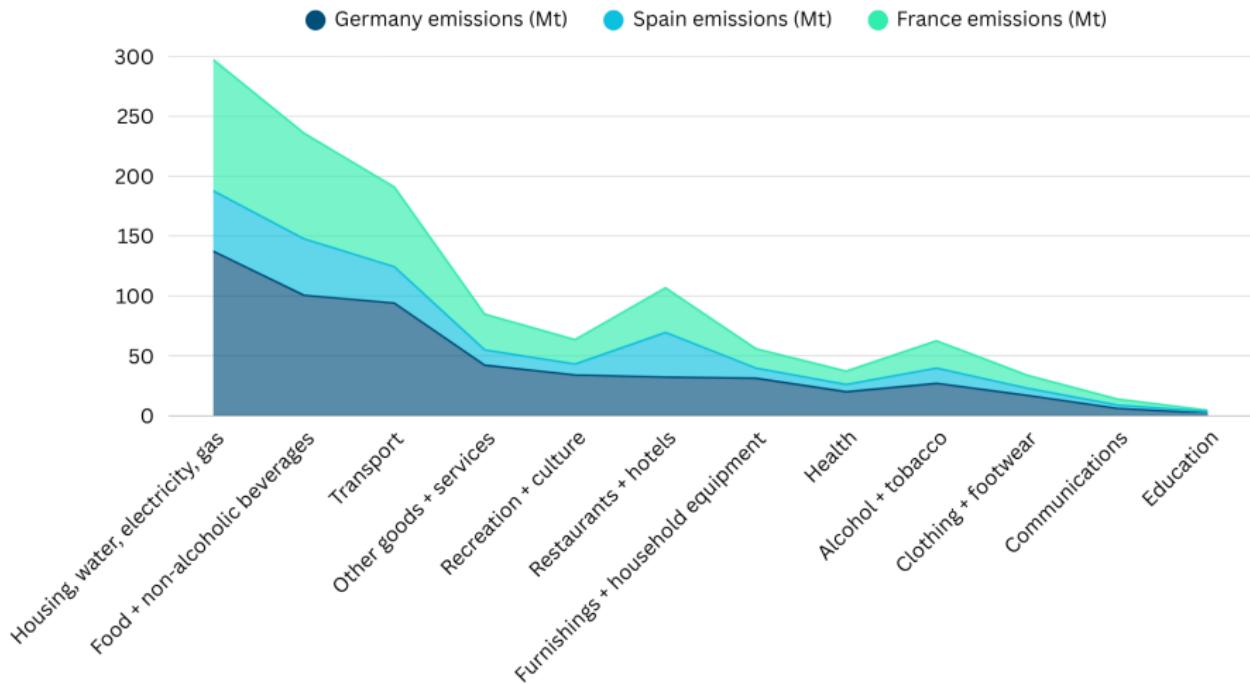
# EEIO Illustration: Interpretation of Results

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# The Hakenes & Schliephake Model

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- One homogeneous good produced with capital only, constant returns to scale.
- Linear technology:  $I = cQ$
- Firms raise  $I$  from households, repay with  $r = \frac{P}{c} + \lambda + \varepsilon$ , with  $\varepsilon \sim \mathcal{N}(0, \sigma^2)$ .
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- Wealth  $w$  allocated to consumption  $q_h$  and investment  $i_h$ , residual in risk-free asset ( $r_f$ ):  $m_h = ri_h + r_f(w - i_h) - Pq_h$ .
- Expected Utility:

$$\mathbb{E}[U_h] = -\exp \left\{ -\alpha \left[ (a - P)q_h - \frac{b}{2}q_h^2 + r_f w + \left( \frac{P}{c} + \lambda - r_f \right) i_h - \frac{\alpha}{2}\sigma^2 i_h^2 - xQ \right] \right\}$$

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## First-Order Conditions:

$$q_h = \frac{a - x - P}{b}, \quad i_h = \frac{1}{\alpha\sigma^2} \left( \frac{P}{c} + \lambda - r_f \right)$$

# Market Equilibrium and Footprint Derivation

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**Solving Supply & Demand:**

$$Q = (n - 1) \frac{a - x - c(r_f - \lambda)}{b + c^2\alpha\sigma^2} + \phi q_h + (1 - \phi) \frac{i_h}{c}$$

where:

$$\phi = \frac{b}{b + c^2\alpha\sigma^2}$$

**Total Household Carbon Footprint:**

$$fp_h = x \left( \phi q_h + (1 - \phi) \frac{i_h}{c} \right), \quad \sum_h fp_h = xQ$$

# Empirical Illustration: U.S. Wheat Market

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$$P(Q) = c(r_f - \lambda) + \frac{c^2 \alpha \sigma^2}{n-1} Q$$

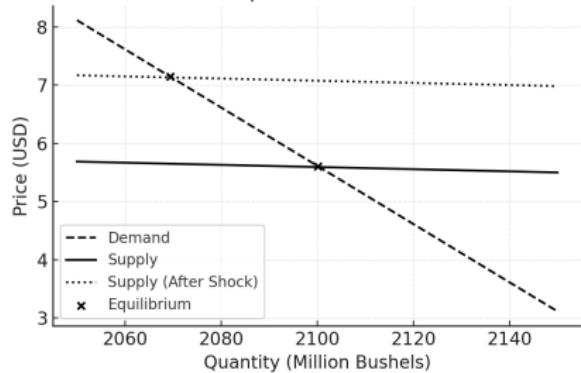
- Parameters:  $c = 4$ ,  $r_f = 0.05$ ,  $\lambda = 0.01$ ,  $\alpha = 0.5$ ,  $\sigma = 0.4$ ,  $n = 100,000$ .
- Demand curve identical to empirical case.

# Carbon Footprint under Empirical & Theoretical Model

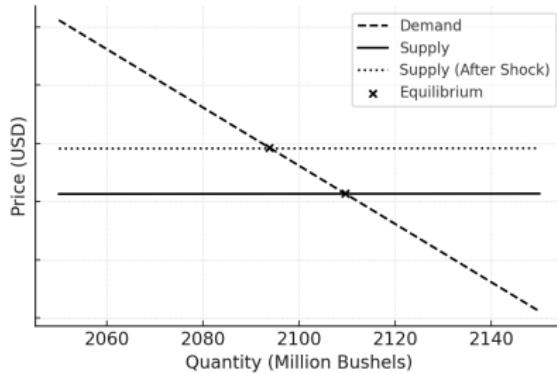
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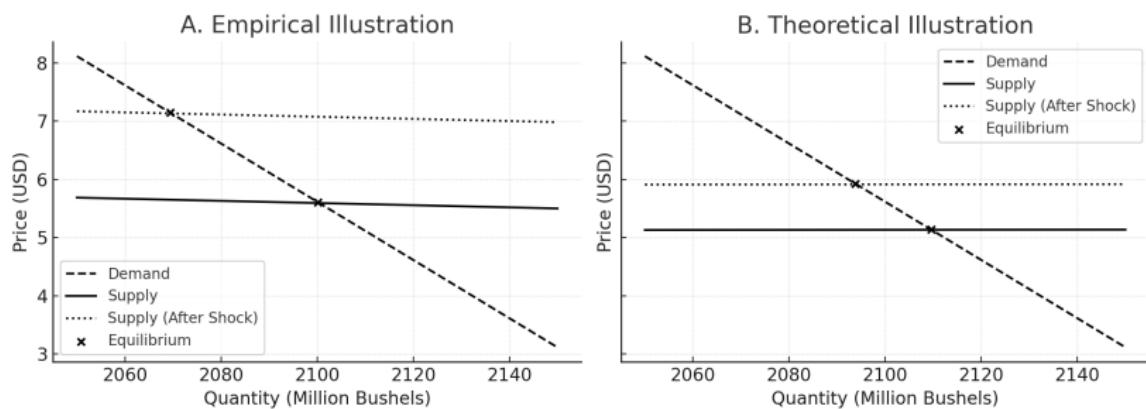
A. Empirical Illustration



B. Theoretical Illustration



# Carbon Footprint under Empirical & Theoretical Model



Scenario	Qty (M bu)	CF (M kg CO <sub>2</sub> e)		
			Empirical Model	Theoretical Model
Before	2100.71	22859.68		22983.46
After	2068.38	22500.32		22808.40
Δ	—	-359.36		-175.06

Source: Author's calculations based on USDA (2010–2017) and FAO data.

# Responsibility for Household Carbon Emissions

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**Central Question:** How should household responsibility for climate change be defined, measured, and fairly attributed?

# Attribution Logics



## OPERATIONAL CONTROL (GHG PROTOCOL)

- Emissions assigned based on operational responsibility.
- Typically attributes emissions to households from direct fuel use and purchased heat/electricity (Scopes 1 and 2).
- Households not held accountable for upstream emissions embodied in consumption of purchased goods and services (Scope 3).
- Production-based attribution, leads to underestimation of household responsibility.
- Only 10-20% of national emissions assigned to households



## CONSUMPTION-BASED (LCA & EEIO)

- Assigns responsibility of emissions to end users.
- LCA quantifies emissions over a product's life-cycle.
- EEIO links household expenditure data with environmental accounts using input-output tables, assigning emissions in proportion to spending categories.
- Results in high attribution to households, typically between 60-70% in high-income countries.



## CONSEQUENTIALIST (HAKENES & SCHLIEPAKE)

- Aggregate emissions of an economy depend on the marginal decisions of a household.
- Weighting parameter determines the relative attribution of emission between consumption and investment.
- Includes both product and financial market and accounts for spillovers through capital reallocation, risk preference and price mechanism.
- Avoids double counting and over-attribution.

# Policy Implications of Attribution Logics



## OPERATIONAL CONTROL (GHG PROTOCOL)

- Suitable for direct emission reduction policies like emission caps, carbon pricing, and corporate responsibility interventions for supply-side decarbonization.
- May incentivize offshoring emissions rather than reducing them.



## CONSUMPTION-BASED (LCA & EIO)

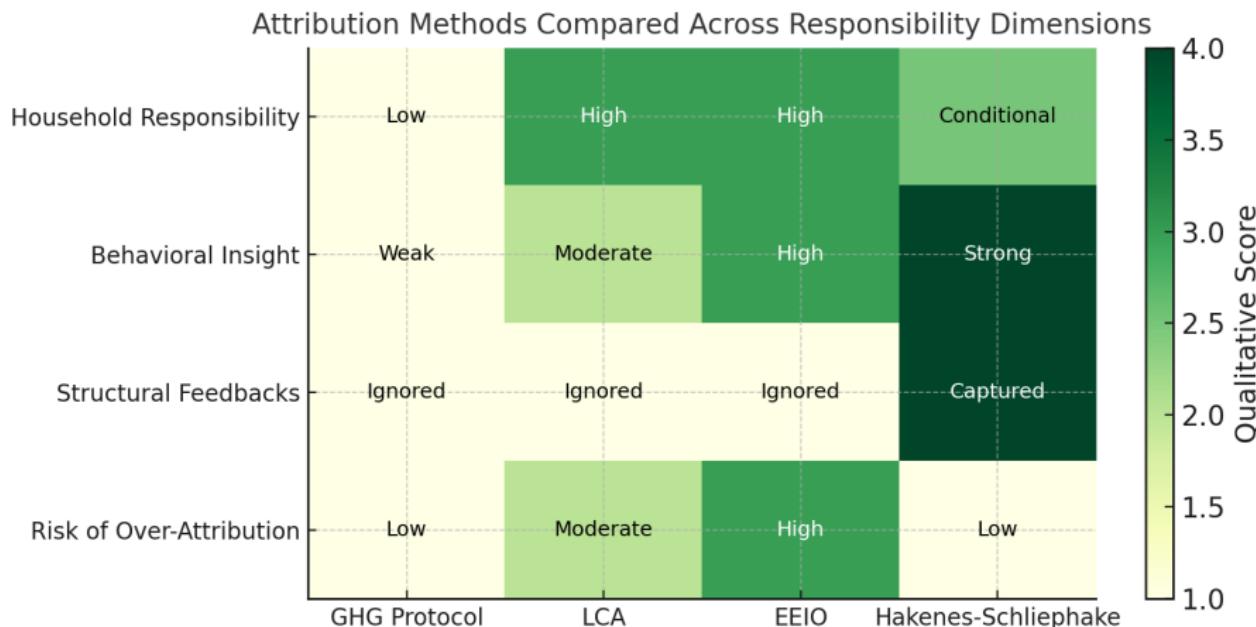
- Encourages individual climate responsibility through policies that use behavioral nudges to encourage sustainable consumption.
- Risks overstating household agency by ignoring structural and supply-side constraints.



## CONSEQUENTIALIST (HAKENES & SCHLIEPAKE)

- Aligns with structural mechanisms such as green financial regulation or carbon-intensity weighting of investment portfolios.
- Differentiates between symbolic and substantive household climate action.

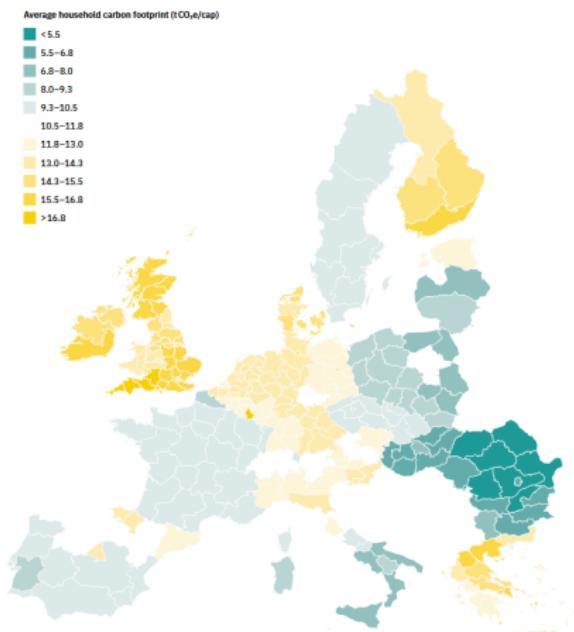
# Comparative Analysis of Attribution Principles



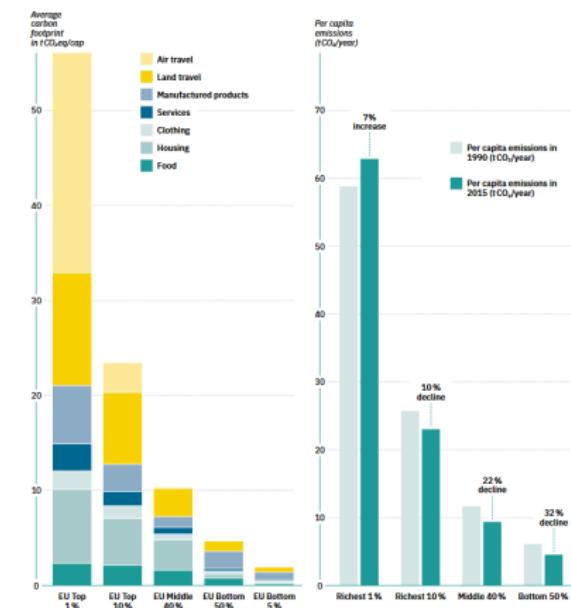
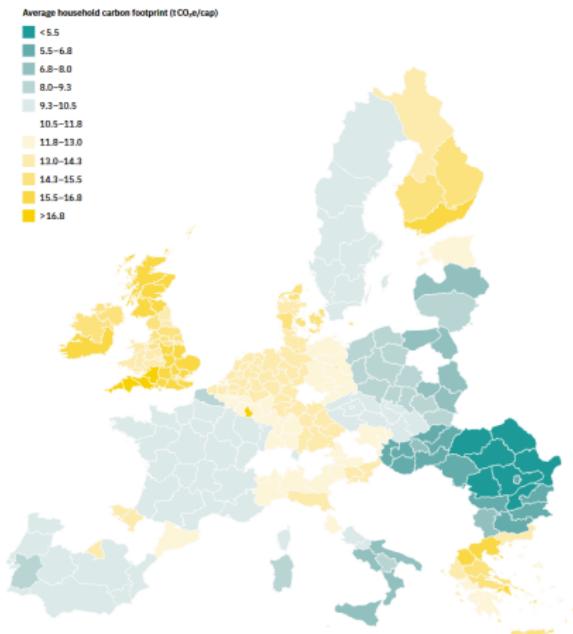
# Household Carbon Footprint Disparities

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# Comparative Overview of Mitigation Instruments

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Instrument	Methodological Basis	Example Implementations	Features
Carbon Taxes	GHG Protocol (Scopes 1–2); EEIO for consumption-based pricing	Sweden: 130+ USD/tCO <sub>2</sub> ; Canada federal backstop; EU Border Carbon Adjustment	Internalises marginal social cost; scalable; regressive without revenue recycling; leakage risk if embedded emissions excluded

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AI-Enabled Platforms	Hybrid EEIO–LCA with transaction-level data integration	Moneythor tracker; Svalna app; Klima app	Real-time, marginal behaviour targeting; adaptive feedback; digital divide and privacy governance concerns

# Optimal Mitigation Portfolio

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**Strategic implication:** No single instrument optimises efficiency, equity, and political feasibility. An optimal portfolio integrates complementary tools, each grounded in the correct attribution logic, to maximise mitigation while maintaining fairness and public acceptance.

# Policy Recommendations

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- **Expand carbon pricing coverage:** Combine GHG Protocol-based taxes on direct fuel and electricity use with EEIO-informed upstream pricing (e.g. border carbon adjustments) to capture embedded emissions in imports.
- **Integrate investment-linked accounting:** Attribute portfolio emissions to households via mandatory financial institution reporting, carbon-intensity metrics in retail products, and differentiated capital gains tax rates, linking investment to market wide externalities.
- **Deploy AI-enabled carbon tracking:** Develop open-source, transaction-linked digital tools integrating banking, utility, and purchasing data to deliver real-time household carbon feedback and tie results to incentive programs.
- **Strengthen product standards:** Ecodesign and efficiency labels extended to cover embodied carbon and lifetime emissions, with mandatory inclusion in public procurement and consumer labeling.
- **Advance hybrid modelling:** Combine dis-aggregated EEIO, dynamic general equilibrium modelling, and behavioral segmentation to simulate differentiated policy impacts across income, asset ownership, and urban-rural contexts.



# Conclusion

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- Overall, the study concludes that household decarbonization strategies must be methodologically consistent, equity sensitive and operationally scalable.
- **Limitations and future work:** This analysis uses stylized data, a static equilibrium model, and omits behavioral heterogeneity; future research should integrate microdata, dynamic modelling, and machine learning for digital tracking tools.

# Thank you!

